

# Incentives towards Economic Integration as the Second-Best Tariff Policy \*

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October, 2007

## Abstract

Economic integration such as free trade areas (FTA) and customs unions (CU) allows importing countries to circumvent the constraint of non-discriminatory tariffs posed by the most favored nation clause in WTO and to employ (incomplete) tariff discrimination. Thus the second-best choice for the importing country, if it does regional integration, is to choose as the partner the exporting country which would have been subject to the lower tariff under the full tariff discrimination. Regardless of the mode of competition, we will find that such a partner tends to be less efficient than other exporting countries, which implies that voluntary regional integration leads the world economy to less efficient resource allocations.

**Keywords:** economic integration, tariff discrimination, second-best policy, conjectural variations, oligopoly

**JEL classification:** F12, F13, F15

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\*This is the modified version of Kiyono (2006a). The author thanks an anonymous referee as well as Eden Yu, Hong Hwang and all the participants of the seminars at Hong Kong City University, Hitotsubashi University and Shiga University for their valuable comments and suggestions.

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## Abstract

Economic integration such as free trade areas (FTA) and customs unions (CU) allows importing countries to circumvent the constraint of non-discriminatory tariffs posed by the most favored nation clause in WTO and to employ (incomplete) tariff discrimination. Thus the second-best choice for the importing country, if it does regional integration, is to choose as the partner the exporting country which would have been subject to the lower tariff under the full tariff discrimination. Regardless of the mode of competition, we will find that such a partner tends to be less efficient than other exporting countries, which implies that voluntary regional integration leads the world economy to less efficient resource allocations.

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## 1 Introduction

Since the seminal article by Viner (1950), there has been a vast literature on theories of economic integration. Somewhat problematic concepts of “trade creation” and “trade diversion” have been reexamined in various frameworks when discussing the welfare effects of integration. Although Meade elucidated those concepts within a framework of a small country and the partial equilibrium approach, there are many other studies casting doubts on those conceptual tools such as Bhagwati and Panagariya (1996). Even without agreement on how to use the two concepts, the economists have also extended the theory of economic integration to imperfect competition as well as economic growth.<sup>1</sup>

However there is another question for research, often less focused in this literature. That is, what country is chosen as the FTA partner? From the viewpoint of the exporting country, it would welcome any economic integration leading to the preferential removal of the currently imposed import tariffs. However from the viewpoint of the importing country, it is vital which exporting country’s tariff to remove, for the change in its terms of trade greatly depends on its choice of economic integration partners.<sup>2</sup>

For the large importing country, the best trade policy is tariff discrimination or import-price discrimination by making the best of its monopsony power in trade. As is implied by the application of the price discrimination to monopsony, when the marginal import costs differ among the exporting countries, the importing country can maximize its welfare by equating those marginal import costs and thus minimizing the total import costs. Put differently, from the viewpoint of the standard optimal tariff theory, the international monopsonist should set the lower import price or equivalently the higher import tariff to the exporting country with the smaller price elasticity of supply. But such tariff discrimination is disallowed in WTO under the most favored nation clause. The only ways to circumvent this constraint are formations of free trade areas (FTA’s) and customs unions (CU’s). Since such economic

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<sup>1</sup>See the extensive surveys by Panagariya (2000) and Baldwin and Venables (1995).

<sup>2</sup>For example, McMillan and MacCann (1981) explores this problem from the viewpoint of complementarity and substitution of goods traded in perfect competition. But there are little research explicitly dealing with the FTA partner choice in imperfect competition except Kiyono (1993) and Raff (2001), though Raff (2001) discusses the problem from the viewpoint of tariff revenue maximization.

integration allows the importing country to employ incomplete but discriminatory tariffs, we may pose the problem of choosing the partner for economic integration as the one of removing the tariffs on either the exporting country subject to the higher or lower tariff under the full tariff discrimination.

Since lowering the higher optimal discriminatory tariff to zero tends to cause the greater costs to the importing country, the intuition tells us that the importing country has the greater incentive to choose the exporting country with the lower optimal discriminatory tariff as its partner. In this paper, we deal with FTA formation and discuss how this intuition holds not only in perfect competition but also in more general imperfect competition.<sup>3</sup> As we will see later, the marginal import cost tends to be lower for the exporting country with the less efficient technologies, which makes the optimal discriminatory tariff lower. This implies that the importing country tends to choose the less efficient technology as its FTA partner.

In section 2, we review the puzzle of welfare-worsening FTA formations with an exporting country having the lower marginal cost posed by Bhagwati and Panagariya (1996) and elucidate the problem of tariff discrimination governing the welfare effect of FTA formation. In section 3, we construct the basic model of FTA formation as the second-best discriminatory policy in perfect competition, and establish the basic principle for the importing country's choosing the FTA partner. In section 4, we extend the model to imperfect competition described by the conjectural variations equilibria, and demonstrate that the results in perfect competition still hold. Lastly in section 5, we extend the analysis by incorporating the domestic production in the importing country. We will find its effect on the tariff discrimination and the choice of the FTA partners with some more remarks on future possible directions for the research.

## 2 FTA Formation for a Large Importing Country

Let us make a brief review over the examples of Bhagwati and Panagariya (1996), illustrated by Figures 1 and 2, which show the complicated welfare effects of FTA formation by a large country importing from two exporting countries in perfect competition.

### 2.1 Ambiguous Welfare Effects of FTA Formation?

In each of the two figures, the downward sloping curve  $DD'$  represents the import demand curve of the importing country while the upward sloping line  $c_L c'_L$  indicates the export supply curve of country  $L$  and the horizontal line  $c_H c'_H$  that of country  $H$ . Initially the importing country imposes the nondiscriminatory or uniform specific import tariff  $t^U$  on the imports from both exporting countries. Thus the total supply curve facing the private sector in the importing country is given by the kinked curve  $c_L^T U c_H^{T'}$ , leading to the equilibrium shown by point  $E$ . Of the total import  $c_H^T E$ ,  $c_H^T U$  comes from country  $L$  and  $UE$  from country  $H$ . The trade surplus for the private sector in the importing country is given by the triangle  $Dc_H^T E$ ,

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<sup>3</sup>The approach is essentially the same as Kiyono (1993) discussing the importing country's choice on the FTA partner within a homogenous Cournot oligopoly market. But the present paper makes clear how the second-best approach covers not only perfect competition but also imperfect competition and generalizes the discussion in two directions. First, the paper covers the case of non-constant marginal costs. Second, it deal with the quasi-Cournot oligopoly market in which the firms hold non-Cournot conjectural variations. And the last but most important difference lies in the analysis using the concept of marginal import costs applied to imperfect competition, by which we can fully characterize the optimal tariff discrimination.



The situation is a little more complicated in Figure 2. The market supply curve facing the private sector in the importing country is now given by the kinked curve  $c_L F c_H^T$ , so that the new equilibrium is given by point  $L$ . All the imports come from country  $L$  with the lower domestic price  $p_L$  and more consumption  $p_L L$ . The importing country gains from more consumption as much as  $\square c_H^T p_L F E$  (the trade creation effect), while it loses all the tariff revenue earned before FTA formation, i.e.,  $c_H^T c_H E' E$  (the trade diversion effect). Thus its net welfare gain is given by  $\Delta EAL$  minus  $\square p_L c_H E' A$ , or equivalently the gains from trade creation minus the costs from trade diversion. The welfare effect of FTA formation now depends on which effect of trade creation and diversion dominates the other.

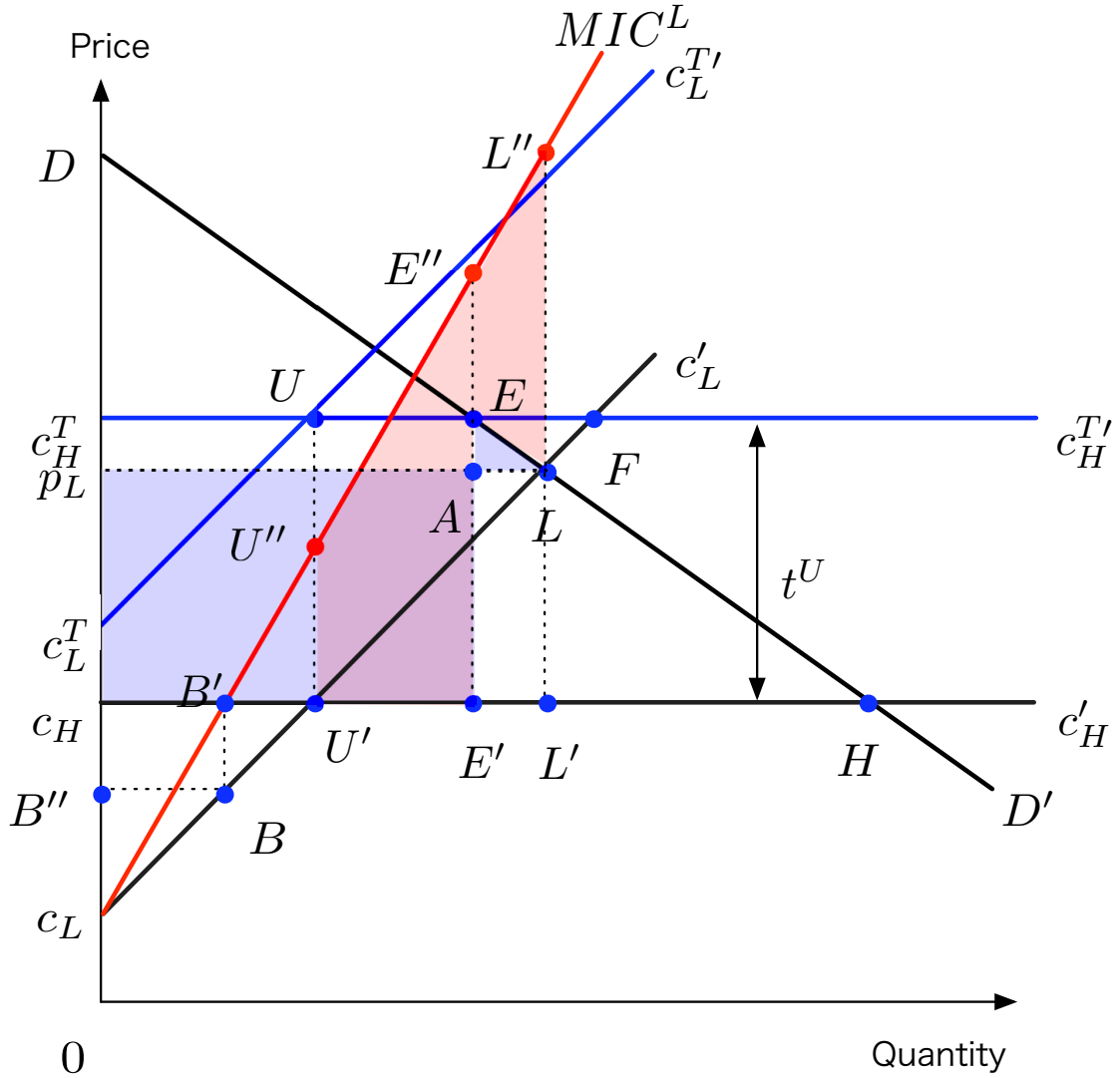


Figure 2: Bhagwati-Panagariya Example 2

## 2.2 Tariff Discrimination as Import-Price Discrimination

This familiar discussion overlooks the important status of the importing country in the world market, i.e., the monopsonist. Since it faces upward-sloping export supply curves, the importing country can make the best of its monopsony power.

And as the monopsonist, the best strategy for the importing country is price discrimination over the exporters. It first minimizes the total import costs by equating the marginal import costs from each country and then decides on the amount of the total import by equating the own marginal benefit of consumption with the equalized marginal import costs between the two exporting countries.

In each of Figures 1 and 2, the marginal import cost from country  $L$ , given by curve  $MIC^L$ , is located above the upward-sloping export supply curve  $c_L c'_L$ , while that of country  $H$  coincides its horizontal export supply curve  $c_H c'_H$ . Thus the marginal import cost curve for the price-discriminating importing country is given by the kinked curve  $c_L B' c'_H$ . It is the best for the importing country to import as much as  $c_H H$ , of which  $c_H B'$  comes from country  $L$  and  $B' H$  from country  $H$ . To achieve this first-best state, the importing country should impose the discriminatory tariffs to the two exporting countries,  $BB'$  on country  $L$  and zero tariff on country  $H$ . Import-price discrimination involves *tariff discrimination*. The total welfare is then given by the trade surplus of the private sector measured by  $\Delta D c_H H$  and the tariff revenue  $\square c_H B'' B B'$ . That is, FTA formation with country  $H$ , rather than with country  $L$ , should be chosen by the importing country.

## 2.3 Choice of FTA Partners

However, when the country is subject to the most favored nation clause, it cannot undertake full tariff discrimination. It can enforce only an imperfect one through economic integration such as FTA and CU by providing preferential zero tariffs to the partner countries. The available alternative policies for the importing country is either uniform tariffs to all the exporting countries or imperfect tariff discrimination through economic integration. Let us take FTA as an example of economic integration throughout the rest of the paper.

The intuition tells us that it is better for the importing country to form a FTA with the exporting country whose optimal discriminatory tariff is lower than the other, for the costs of required tariff reduction should be smaller than the FTA with the other exporting country.

In fact, as the two Figures show, the marginal import cost of country  $L$ , whose optimal discriminatory tariff is the higher, is greater than that of country  $H$ , so that the import substitution from country  $H$  to country  $L$  after FTA formation with country  $L$  increases the total import costs and thus makes the importing country worse off. For example, in Figure 1, although the total import volume is kept unchanged, the import substitution raises the total import costs as much as the trapezoid shape of  $U'' U' L' L''$ , which is another expression for the country's welfare loss from FTA formation with country  $L$ .

And in Figure 2, the importing country suffers from two types of welfare loss. The first is the increased import costs from import substitution, measured by  $\square U'' U' E' E''$ , and the second is the excessive consumption due to the marginal import cost greater than the marginal benefit of consumption, measured by the trapezoid shape of  $E'' E L L''$ . Thus, the importing country is strictly worse off by FTA formation with country  $L$  though the FTA formation entails the trade-creation. Because we have not carefully used the marginal import costs, we have long been unaware of this mechanism of welfare-worsening trade creation.

### 3 FTA Formation in Perfect Competition

Let us generalize the analysis in the previous section, and elucidate further the properties of the candidates as FTA partners.

#### 3.1 Competitive Model

As in the previous section, consider a country totally depending on the imports from two exporting countries,  $H$  and  $L$ , for consumption of a certain good. There are  $n_i$  identical competitive firms in each exporting country  $i \in \{H, L\}$  with the total export cost function  $C_i(x_i)$  where  $x_i$  denotes the individual output for export in country  $i$ . Let  $X_i := n_i x_i$  denote the total export of country  $i$ ,  $X_T := \sum_k X_k$  the total exports, and  $p$  the domestic price in the importing country. Then the profit of an individual firm in country  $i$  is given by

$$\pi^i := px_i - C_i(x_i) - t_i x_i,$$

where  $t_i$  denotes the specific tariff imposed by the importing country's government on exporting country  $i$ . We assume

**Assumption 1** *The marginal cost of each firm in each country is increasing in the output, i.e.,  $C_i''(x_i) > 0$  for  $i = H, L$ .*

Since each exporting firm maximizes its profit by equating the marginal cost with the gross-tariff export price, denoted by  $v_i = p - t_i$ . The condition defines the individual firm's export supply price function given by

$$v_i = v^i(x_i) := C_i'(x_i). \quad (1)$$

Its inverse is the individual export supply function  $s^i(v_i)$ , and the total export supply by country  $i$  expressed by  $S^i(X_i : n_i) := n_i s^i(v_i)$ .

There are two remarks in order here. First, the price elasticity of country  $i$ 's export supply is the same as that of the individual export supply, which we denote by  $\varepsilon_i^S(v_i)$ . Second, since this price elasticity is equal to the inverse of the output elasticity of marginal cost, there holds

$$\varepsilon_i^S(v_i) = \frac{1}{\sigma_i(s^i(v_i))} \quad (2)$$

where  $\sigma_i(x_i) := d \ln C_i'(s^i(v_i)) / d \ln x_i$  denotes the output elasticity of country  $i$ 's marginal cost or equivalently the output elasticity of the export supply price,  $d \ln v^i(x_i) / d \ln x_i$ . The two countries differ with respect to the price elasticity of export or the output elasticity of the marginal cost as follows.

**Assumption 2** *There holds  $\varepsilon_H^S(v) > \varepsilon_L^S(v)$  for all common export price  $v$ . Or equivalently, there holds  $\sigma_H(x_H) < \sigma_L(x_L)$  for all  $(x_H, x_L)$  satisfying  $C_H'(x_H) = C_L'(x_L)$ .*

The total import costs, denoted by  $TIC$ , is then given by

$$TIC(X_H, X_L; n_H, n_L) := \sum_k v^k \left( \frac{X_k}{n_k} \right) X_k. \quad (3)$$

The marginal import cost from country  $i$ , denoted by  $MIC^i$ , is given by

$$MIC^i(X_i) := \frac{\partial TIC(X_H, X_L)}{\partial X_i} = v^i \left( \frac{X_i}{n_i} \right) + x_i C_i''(x_i) = C_i'(x_i) (1 + \sigma_i(x_i)), \quad (4)$$

which is independent of the import from the other exporting country.<sup>4</sup>

Let us denote by  $u(X)$  the total consumption benefit of the importing country and by  $P(X) := u'(X)$  the associated inverse demand function. The welfare of the importing country is expressed by

$$W = u \left( \sum_k X_k \right) - P \left( \sum_k X_k \right) \cdot \sum_k X_k + \sum_k t_k X_k,$$

which can be rewritten as

$$W(\mathbf{X}) = u \left( \sum_k X_k \right) - TIC(X_H, X_L), \quad (5)$$

where  $\mathbf{X} := (X_H, X_L)$  and use was made of (1). Without loss of generality, we assume that  $W(\mathbf{X})$  is strictly concave.

### 3.2 Optimal Tariff Discrimination

Let us first explore the policy of optimal tariff discrimination as import-price discrimination. Let us express the equilibrium values with superscript  $D$ . Then the optimal import from each country should satisfy the following conditions for welfare maximization.<sup>5</sup>

Condition 1: Minimization of the total import costs given the total import volume, i.e.,  $MIC^H(X_H^D) = MIC^L(X_L^D)$ .

Condition 2: Equality between the marginal consumption benefit and the equalized marginal import costs, i.e.,  $P(X_T^D) = MIC^H(X_i^D)$  for  $i = H, L$ .

Since  $MIC^i(X_i) = C_i'(x_i) + x_i C_i''(x_i)$  and the specific tariff rate is equal to the difference between the domestic price (=the marginal consumption benefit) and the export price, Condition 2 above implies that the optimal discriminatory tariff on country  $i$ , denoted by  $t_i^D$ , is given by

$$t_i^D = C_i'(x_i^D) \sigma_i(x_i^D). \quad (6)$$

This is the specific-tariff version of the familiar optimal tariff formula. The examples of Bhagwati and Panagariya (1996) are based on the marginal cost function given by

$$C_i'(x_i) = c_i + \frac{x_i}{s_i}, \quad (\text{BP-MC})$$

<sup>4</sup>As we will see later, this independence property fails to hold in imperfect competition.

<sup>5</sup>We assume here, though not stated explicitly in the text,

$$MIC^i(X_i^m) > MIC^j(0) \quad (i, j = H, L; j \neq i),$$

where  $X_i^m := \max_{\{X_i\}} \{W(\mathbf{X}) | X_j = 0\}$ . If this condition fails, then the first-best tariff rate is given by  $t_i^m := P(X_i^m) - v^i(X_i^m)$ , which automatically prevents the import from country  $j$ . Then FTA formation is definitely worse than this optimal uniform tariff policy.



where  $c_i$  and  $s_i$  are positive constants. The marginal import cost from each country is then equal to  $MIC^i(X_i) = c_i + 2\frac{x_i}{s_i}$ , so that Condition 2 implies

$$x_i^D C_i''(x_i^D) = \frac{x_i^D}{s_i} = \frac{1}{2} (p^D - c_i),$$

where  $p^D := P(X_T^D)$ . Thus, the optimal discriminatory tariff is equal to

$$t_i^D = \frac{1}{2} (p^D - c_i) \quad (i = H, L)$$

by virtue of (6). Therefore for the marginal cost functions (BP-MC) discussed by Bhagwati and Panagariya (1996), the difference in the optimal discriminatory tariffs depends only on each country's choke price for export,  $c_i$ , and thus country  $L$  faces the higher tariff under the optimal tariff discrimination.

**Proposition 1** *When both exporting countries are subject to the marginal costs given by (BP-MC) under perfect competition, the exporting country with the lower choke price faces the higher optimal discriminatory import tariff.*

### 3.3 Optimal Uniform Tariff Policy

Now consider the optimal uniform tariff policy, i.e., the non-discriminatory import-pricing to both exporting countries. As both exporting countries face the same tariff and thus the same export price, their marginal costs should be equal, i.e.,  $C_H' \left( \frac{X_H}{n_H} \right) = C_L' \left( \frac{X_L}{n_L} \right)$ . This equality governs the export by country  $L$  as a function of the export by country  $H$  for any rate of uniform tariffs, which we express by  $X_L = \gamma_H(X_H)$ . This function satisfies

$$\gamma_H'(X_H) = \frac{n_L C_H''(x_H)}{n_H C_L''(x_L)} = \frac{X_L \sigma_H(x_H)}{X_H \sigma_L(x_L)} > 0. \quad (7)$$

Using this function  $\gamma_H(X_H)$ , we may express the optimal uniform-tariff policy problem faced by the importing country as  $\max_{\{X_H\}} W(X_H, \gamma_H(X_H))$  where we assume that  $W(X_H, \gamma_H(X_H))$  is strictly concave in  $X_H$ . For characterizing this equilibrium, the following lemma is of a great use.

**Lemma 1** *In perfect competition, for any uniform tariff, there holds  $\frac{\partial W(X_H, X_L)}{\partial X_H} > \frac{\partial W(X_H, W_L)}{\partial X_L}$ , or equivalently  $MIC^H(X_H) < MIC^L(X_L)$ .*

This follows straightforward from the following inequality based on the definition of the marginal import costs.

$$\begin{aligned} & \frac{\partial W(\mathbf{X})}{\partial X_H} - \frac{\partial W(\mathbf{X})}{\partial X_L} \\ &= \{p - C_H'(x_H)(1 + \sigma_H(x_H))\} - \{p - C_L'(1 + \sigma_L(x_L))\} \\ &= C_H'(x_H) \{\sigma_L(x_L) - \sigma_H(x_H)\} > 0 \\ & \quad (\because C_H'(x_H) = C_L'(x_L) \text{ under the uniform tariffs, and Assumption 2}) \end{aligned}$$

Now we characterize the optimal uniform tariff policy equilibrium as the solution to  $\max_{\{X_H\}} W(X_H, \gamma_H(X_H))$ . Let us represent the variables associated with the resulting optimal uniform tariff policy equilibrium with superscript “ $U^*$ ”. Then the associated first-order condition for welfare maximization is given by

$$\begin{aligned} 0 &= \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_H} + \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_L} \gamma'_H(X_H^{U^*}) \\ &= \{P(X_T^{U^*}) - MIC^H(X_H^{U^*})\} + \{P(X_T^{U^*}) - MIC^L(X_L^{U^*})\} \gamma'_H(X_H^{U^*}) \\ &< (1 + \gamma'_H(X_H^{U^*})) \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_H} \quad (\because \gamma'_H(X_H) > 0 \text{ and Lemma 1}), \end{aligned}$$

which implies  $\frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_H} > 0$ , and thus  $\frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_L} < 0$  due to  $\gamma'_H(X_H) > 0$ . Therefore we have established

**Lemma 2** *In perfect competition, at the optimal uniform tariff policy equilibrium, there holds  $\frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_H} > 0 > \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_L}$ .*

### 3.4 FTA Formation

What if the importing country abandons the optimal uniform tariff policy and forms a FTA with either exporting country? Let us denote by  $X_k^i (i, k \in \{H, L\})$  the import from country  $k$ , by  $W^i$  the importing country's welfare when a FTA is formed with country  $i$ , and by  $W^{U^*}$  the welfare under the optimal uniform tariff policy. Since the welfare function is strictly concave, there holds the following inequality governing the welfare between the two states.

$$\begin{aligned} W^i - W^{U^*} &\leq \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_H} (X_H^i - X_H^{U^*}) + \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_L} (X_L^i - X_L^{U^*}). \end{aligned} \quad (8)$$

Then it is straightforward to derive the following proposition by virtue of the above inequality and Lemma 2.<sup>6</sup>

**Proposition 2** *In perfect competition, when the FTA formation with country  $i$  gives rise to either (i)  $X_H^i \leq X_H^{U^*}, X_L^i \geq X_L^{U^*}$ , or/and (ii)  $X_T^i \leq X_T^{U^*}$ , then the importing country cannot get better off by the FTA formation.*

This proposition indicates two sets of conditions for welfare-worsening FTA formation compared with the optimal uniform tariff policy. Condition (i) is immediate from (8) by virtue of Lemma 2. It implies that insofar as the FTA expands the import from the partner but reduces the import from the non-partner, then the importing country gets worse off by the FTA formation with country  $L$ .

Condition (ii) can be obtained by rewriting (8) as follows.

$$W^i - W^* \leq \frac{\partial W(X_H^{U^*}, \gamma_H(X_H^{U^*}))}{\partial X_H} \{(X_H^i - X_H^{U^*}) + (X_L^i - X_L^{U^*})\},$$

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<sup>6</sup>The second part of Proposition 2 is similar to the result for the third-degree price discrimination obtained by Schmalensee (1981) and elegantly discussed by Varian (1985). However their studies discuss the closed markets in which the social surplus includes the profits earned by the firms, while those profits do not contribute to the importing country's welfare in this paper.

where use was again made of Lemma 2. The condition implies that when the total import volume does not exceed after the FTA formation, then the importing country gets worse off than under the optimal uniform tariff policy.

In view of Proposition 2, when the importing country finds FTA formation better than the optimal uniform tariff policy, then the partner should be country  $H$  facing the higher optimal discriminatory tariff and the FTA should expand the total import volume.

## 4 FTA Formation in Imperfect Competition

Let us extend our analysis towards imperfect competition à la Cournot.<sup>7</sup> For simplicity of exposition, we additionally assume

**Assumption 3** *The inverse demand function  $P(X_T)$  is concave, i.e.,  $P''(X_T) \leq 0$ .*

This assumption ensures the individual output to be always a strategic substitute to the others' and the equilibrium, whenever it exists, to be unique and globally stable.<sup>8 9</sup>

On the other hand, we relax Assumption 1 as follows so that we can take account of the case of constant marginal costs, too.

**Assumption 4** *The marginal cost of each firm in each country is non-decreasing in the output, i.e.,  $C_i''(x_i) \geq 0$  for  $i = H, L$ .*

We also discuss more general mode of competition than the standard Cournot model, by employing the conjectural variations approach.<sup>10</sup>

**Assumption 5** *Each firm in country  $i (\in \{H, L\})$  has the same constant value of conjectural variations  $\lambda_i (> 0)$ , which represents how much it expects the total output to increase along with its output expansion.*

Then the first-order condition for profit maximization is

$$0 = P(X_T) + \lambda_i x_i P'(X_T) - C_i'(x_i) - t_i,$$

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<sup>7</sup>The model framework is essentially the same as Brander and Spencer (1984).

<sup>8</sup>As is defined by Bulow et al. (1985), a firm's output is called a *strategic substitute* to the rivals' if an increase in the rivals' outputs decreases the firm's best-response output.

<sup>9</sup>This assures the so-called "Hahn condition" for stability of Cournot equilibrium (Hahn (1962)). See also the modern approach to the problem of uniqueness and stability of Cournot equilibrium discussed by Kolstad and Mathiesen (1987), Okuguchi (1976) and Gaudet and Salant (1991) for instance. Their discussion can be readily applied to the present conjectural variations approach. For existence, if we disregard the integer problem associated with the number of firms, it suffices to assume that the marginal cost at zero output of any group of firms  $i \in \{H, L\}$ , i.e.,  $C_i'(0)$ , is strictly lower than the equilibrium price at which only the other group of firms are active. This condition for the existence of equilibrium is not stated here clearly, for it does not play any critical role in the succeeding analysis.

<sup>10</sup>Compared with the previous studies such as Kiyono (1989), Gatsios (1990), Hwang and Mai (1991), Kiyono (1993), Raff (2001) and Saggi (2004), conjectural variations allow us to explore various modes of competition covering perfect competition equilibria, Cournot-Nash equilibria, and complete or incomplete joint profit maximization. See Kamien and Schwartz (1983) and Cabral (1995) for the usefulness of this concept. We also note that consideration of the conjectural variations in addition to the number of active firms makes sense in the analysis only if the marginal production cost is not constant. For otherwise, the number of active firms governing the industry equilibrium becomes the so-called *effective number* of firms,  $n_i/\lambda_i$ , which implies that the equilibrium with  $n_i$  firms and conjectural variations  $\lambda_i$  is in fact equivalent to the one with the effective number of firms  $n_i/\lambda_i$ .

which implies that the equilibrium individual outputs are the same for all the firms located in the same country. Thus, the equilibrium condition for the industry as a whole in country  $i$  is expressed by

$$0 = P(X_T) + \frac{\lambda_i}{n_i} X_i P'(X_T) - C'_i \left( \frac{X_i}{n_i} \right) - t_i. \quad (9)$$

As in perfect competition,  $v_i := P(X_T) - t_i$  represents the import price from country  $i$  (or the export price facing country  $i$ ). (9) then defines the export supply price function of each exporting country as

$$v^i(X_i, X_T; n_i, \lambda_i) := C'_i \left( \frac{X_i}{n_i} \right) + IMR^i \left( X_i, X_T \frac{\lambda_i}{n_i} \right), \quad (10)$$

where

$$IMR^i \left( X_i, X_T; \frac{\lambda_i}{n_i} \right) := -\frac{\lambda_i}{n_i} X_i P'(X_T) \quad (11)$$

represents the *individual monopoly rent* required to be earned per unit of output by the individual firm in country  $i$  and satisfies

$$\frac{\partial IMR^i(X_i, X_T)}{\partial X_i} = -\frac{\lambda_i}{n_i} P'(X_T) = \frac{1}{X_i} \left( v^i(X_i, X_T; n_i, \lambda_i) - C'_i \left( \frac{X_i}{n_i} \right) \right) > 0, \quad (12)$$

$$\frac{\partial IMR^i(X_i, X_T)}{\partial X_T} = -P''(X_T) \frac{\lambda_i}{n_i} X_i \geq 0, \quad (13)$$

where use was made of Assumption 3, (9) and (10). As expressed by (10), the export price of each country now depends not only on its own output but also on the other's, and exceeds the marginal cost by the individual monopoly rent. In view of (12) and (13), one should also note that the required individual monopoly rent of each firm is increasing in both its own output and the industry output.

Let  $\mathbf{X} := (X_H, X_L)$  represent the import vector. Then the total import cost function, denoted by  $TIC(\mathbf{X}; \mathbf{n}, \boldsymbol{\lambda}) := \sum_k v^k(X_k, X_T) X_k$ , is also expressed as follows.

$$TIC(\mathbf{X}; \mathbf{n}, \boldsymbol{\lambda}) = \sum_k X_k \cdot C'_k \left( \frac{X_k}{n_k} \right) + \sum_k X_k \cdot IMR^k(X_k, X_T) \quad (14)$$

$$= \sum_k X_k \cdot C'_k \left( \frac{X_k}{n_k} \right) - P' \left( \sum_k X_k \right) \sum_k \frac{\lambda_k}{n_k} X_k^2. \quad (15)$$

The marginal import cost from country  $i$ , denoted by  $MIC^i(X_i, X_j)$ , is now given by <sup>11</sup>

$$\begin{aligned} MIC^i(X_i, X_j) &:= v^i(X_i, X_T) + x_i C''_i(x_i) \\ &\quad + X_i \frac{\partial IMR^i(X_i, X_T)}{\partial X_i} + \sum_k X_k \frac{\partial IMR^k(X_k, X_T)}{\partial X_T}, \end{aligned} \quad (MIC)$$

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<sup>11</sup>More specifically, as with country  $H$  for instance, its marginal import cost function is defined as

$$MIC^H(X_H, X_L) := \frac{dTIC(X_H, X_H + X_L)}{dX_H} = \frac{\partial TIC(X_H, X_H + X_L)}{\partial X_H} + \frac{\partial TIC(X_H, X_H + X_L)}{\partial X_T}.$$

where the first two terms are just the same as in perfect competition as expressed by (4) while the third and fourth terms are specific to imperfect competition and both are positive by virtue of (12) and (13). They represent the increased monopoly rents due to country  $i$ 's output increase. In the following analysis, the following alternative expression for the marginal import costs is of a great use.

$$MIC^i(X_i, X_j) = 2v^i(X_i, X_T; n_i, \lambda_i) + x_i C_i''(x_i) - C_i'(x_i) - P''(X_T) \sum_k \frac{\lambda_k}{n_k} X_k^2, \quad (\text{MIC-ALT})$$

where use was made of (12) and (13).

As in perfect competition, the welfare of the importing country, denoted by  $W(\mathbf{X}; \mathbf{n}, \boldsymbol{\lambda})$ , is then given by

$$W(\mathbf{X}; \mathbf{n}, \boldsymbol{\lambda}) := U\left(\sum_k X_k\right) - TIC(\mathbf{X}; \mathbf{n}, \boldsymbol{\lambda}), \quad (16)$$

which is essentially the same as (5) in perfect competition. As in perfect competition, we assume the following for making the succeeding analysis meaningful.<sup>12</sup>

**Assumption 6** *The welfare function  $W(\mathbf{X}; \mathbf{n}, \boldsymbol{\lambda})$  is strictly concave in  $\mathbf{X}$ .*

This completes the description of the model. As has already been discussed, the critical difference in the welfare expression between perfect and imperfect competition is that the import cost from each exporting country,  $v_i X_i$ , depends on the amount of export by the other exporting country in imperfect competition.<sup>13</sup>

Hereafter we extend the previous analysis in perfect competition to imperfect competition. First, we explore the properties of the optimal tariff discrimination,

#### 4.1 Optimal Tariff Discrimination in Imperfect Competition

As in perfect competition, the import vector  $\mathbf{X}^D := (X_H^D, X_L^D)$  associated with the optimal tariff discrimination equilibrium, should satisfy<sup>14</sup>

Condition 1': Minimization of the total import costs given the total import volume, i.e.,  $MIC^H(X_H^D, X_L^D) = MIC^L(X_L^D, X_H^D)$ ,

Condition 2': Equality between the marginal consumption benefit and the equalized marginal import costs, i.e.,  $P(X_T^D) = MIC^i(X_i^D, X_j^D)$  for  $i, j = H, L (j \neq i)$ .

<sup>12</sup>The previous studies formulate the importing country's welfare as a function of the tariff vector and assume that it is concave in the tariff vector. However, the condition to ensure this concavity is more complicated than when we use the welfare as a function of the import vector as formulated below. In fact, given concavity of the gross consumption benefit function  $U(X_T)$ , concavity of the inverse demand function  $P(X_T)$ , and increasing marginal costs of each firm's export, the welfare function given by (16) is concave in the import vector when there hold  $C'''(x) \geq 0$  for  $i = H, L$ , and  $P'''(X_T) \leq 0$ .

<sup>13</sup>In perfect competition, country  $i$ 's export supply function is solely determined by its own exports, i.e.,  $\partial v^i(X_i, X_j)/\partial X_j = 0$ . This in fact holds when  $\lambda_i = 0$ .

<sup>14</sup>We also assume essentially the same condition as in perfect competition mentioned in footnote 5. That is,

$$MIC^i(X_i^m, 0) > MIC^j(0, X_i^m) \quad (i, j \in \{H, L\}; j \neq i),$$

where  $X_i^m := \arg \max_{\{X_i\}} \{W(\mathbf{X}) | X_j = 0\}$ .

Let us make clear first by using Condition 1' what governs the difference in the optimal discriminatory tariffs on the exporting countries as in the case of perfect competition. This Condition 1', coupled with (MIC-ALT), yields

$$x_H^D C_H''(x_H^D) - C_H'(x_H^D) - 2t_H^D = x_L^D C_L''(x_L^D) - C_L'(x_L^D) - 2t_L^D$$

which gives rise to

$$t_L^D - t_H^D = \frac{1}{2} \{ C_H'(x_H^D) (1 - \sigma_H(x_H^D)) - C_L'(x_L^D) (1 - \sigma_L(x_L^D)) \}. \quad (17)$$

When the marginal cost functions are given by (BP-MC), then the above tariff difference is reduced to

$$t_L^D - t_H^D = \frac{1}{2}(c_H - c_L).$$

Surprisingly enough, the difference in the optimal discriminatory tariffs is just the same as in perfect competition.<sup>15</sup>

**Proposition 3** *When the marginal costs are expressed by (BP-MC), i.e.,  $C_i'(x_i) = c_i + \frac{x_i}{s_i}$ , then there holds  $t_L^D - t_H^D = \frac{1}{2}(c_H - c_L)$ , and the exporting country with the lower choke price  $c_i$  is subject to the higher discriminatory tariff.*

By Condition 2' coupled with (MIC), we can obtain the general formula for optimal discriminatory specific tariffs which holds both in perfect and imperfect competition as follows.

$$t_i^D = x_i^D C_i''(x_i^D) + X_i^D \frac{\partial IMR^i(X_i^D, X_T^D)}{\partial X_i} + \sum_k X_k \frac{\partial IMR^k(X_k^D, X_T^D)}{\partial X_T},$$

where use was made  $t_i = P(X_T) - v^i(X_i, X_T)$ .

The first term on the right hand side is the effect of increasing marginal costs working both in perfect and imperfect competition. Since  $x_i C_i''(x_i) = C_i'(x_i) \sigma_i(x_i)$  and  $\sigma_i(x_i)$  corresponds to the inverse of the price elasticity of export supply, we may call it the *elasticity effect*.

On the other hand, as we have discussed on the marginal import costs, the second and third terms are specific to imperfect competition and both are positive. The second term shows

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<sup>15</sup>Gatsios (1990) and Hwang and Mai (1991) derives the following result for the importing country importing from two countries, each of which has a single exporting firm, whereas Kiyono (1993) discusses for the case in which there are more than two symmetric firms in each exporting country, and Saggi (2004) proves it for the importing country importing from more than two countries. All these studies assume Cournot competition, i.e.,  $\lambda_i = 1$  for all the firms in question. One should also note that the result depends on the assumption of specific import tariffs. Given the ad valorem tariffs, the discriminatory ad valorem tariff rate  $\tau_i^D$  on exporting country  $i$  should satisfy

$$\tau_i^D = \frac{\partial C_i'(x_i^D)}{\partial \ln x_i} + \frac{\partial \ln \rho^i(X_i^D, X_T^D)}{\partial X_i} + \frac{\bar{v}(\mathbf{X}^D)}{v^i(X_i^D, X_T^D)} \sum_k \theta^k(X_k^D, X_T^D) \frac{\partial \ln \rho^k(X_k^D, X_T^D)}{\partial \ln X_T}.$$

where  $v_i = v^i(X_i, X_T) := \rho^i(X_i, X_T) C_i'(\frac{X_i}{n_i})$  represents the export price of country  $i$  (exp price), and  $\rho^i(X_i, X_T) := \frac{P(X_T)}{P(X_T) + \frac{\lambda_i}{n_i} X_i P'(X_T)}$  the monopoly-rent ratio,  $\bar{v}(\mathbf{X}) := \sum_k v^k(X_k, X_T) X_k / X_T$  the average import price, and  $\theta^k(X_k, X_T) := \frac{X_k v^k(X_k, X_T)}{X_T \bar{v}(\mathbf{X})}$  the share of the imports from country  $k$  in the total imports. See Kiyono (2006b) for the detail.

the effect of increased individual monopoly rents, and the third term the effect of increased industry monopoly rents. Unlike the standard literature on taxing oligopoly firms in trade, the above formula indicates that the optimal tariff does extract not the foreign monopoly rents but the increased monopoly rents as well as the increased marginal costs of the exporters. More specifically, as is shown in the above derivation of the optimal tariff formula, the optimal import policy requires the domestic price to be equal to the marginal import cost, which implies that the optimal tariff is equal to the difference between the marginal import cost and the average one (which is equal to the export price). In this sense, the rule to set optimally the import tariff is the same in imperfect competition as in perfect competition.

**Proposition 4** *When the importing country enforces the optimal discriminatory tariff policy, then the associated specific tariff on exporting country  $i$ , denoted by  $t_i^D$ , is equal to the difference between the marginal import cost and the average one, and it is given by*

$$t_i^D = x_i^D C_i''(x_i^D) + X_i^D \frac{\partial IMR^i(X_i^D, X_T^D)}{\partial X_i} + \sum_k X_k \frac{\partial IMR^k(X_k^D, X_T^D)}{\partial X_T}, \quad (i = H, L).$$

Note that the formula above holds even when we allow the country importing from more than two exporting countries.

## 4.2 Optimal Uniform Tariffs and FTA Formation

We may apply the same logic as in perfect competition and obtain the condition for welfare-worsening FTA formation compared with the optimal uniform tariff policy. But there are new problems specific to imperfect competition.

First, Assumption 2 does not enable us to get  $MIC^H(\cdot) < MIC^L(\cdot)$  at uniform tariff equilibria. In perfect competition, equality of the export prices given uniform tariffs requires equality of the marginal production costs between the exporting countries, so that Assumption 2 is enough to establish  $MIC^H(\cdot) < MIC^L(\cdot)$ . However in imperfect competition, the marginal production costs are not equalized in general across the exporters given uniform tariffs. In fact, (MIC-ALT) indicates

$$\begin{aligned} & MIC^L(X_L, X_H) - MIC^H(X_H, X_L) \\ &= x_L C_L''(x_L) - C_L'(x_L) - x_H C_H''(x_H) + C_H'(x_H) \\ &= C_L'(x_L) (\sigma_L(x_L) - 1) - C_H'(x_H) (\sigma_H(x_H) - 1) \end{aligned} \quad (18)$$

given uniform tariffs.<sup>16</sup>

Second, even if there holds  $MIC_H < MIC_L$ , it does not necessarily mean  $\frac{\partial W(\mathbf{X}^{U*})}{\partial X_H} > 0 > \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L}$  at the optimal uniform tariff equilibrium. This is because the raise in the uniform tariff rate, having reduced the individual output in perfect competition, does not generally

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<sup>16</sup>However the same inequality as in perfect competition holds when the marginal costs are given by (BP-MC), for we have  $C_i'(x_i) = c_i + x_i C_i''(x_i)$  and thus (18) implies

$$MIC^H(X_H, X_L) - MIC^L(X_L, X_H) = c_L - c_H < 0,$$

by virtue of  $c_H > c_L$ . This also implies  $\frac{\partial W(\mathbf{X})}{\partial X_H} > \frac{\partial W(\mathbf{X})}{\partial X_L}$ . These results constitute the counterpart of Lemma 2 in imperfect competition.

decrease all the firms' outputs in imperfect competition.<sup>17</sup> But despite this result, since the welfare function is concave, we can apply the same approach as in perfect competition and obtain the following inequality, essentially the same as (8).

$$W^i - W^{U*} \leq \frac{\partial W(\mathbf{X}^{U*})}{\partial X_H} (X_H^i - X_H^{U*}) + \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} (X_L^i - X_L^{U*}),$$

which is equivalent to

$$\begin{aligned} W^i - W^{U*} &\leq \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} (X_T^i - X_T^{U*}) + \left( \frac{\partial W(\mathbf{X}^{U*})}{\partial X_H} - \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} \right) (X_H^i - X_H^{U*}) \\ &= \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} (X_T^i - X_T^{U*}) + (MIC^L(\cdot) - MIC^H(\cdot)) (X_H^i - X_H^{U*}) \end{aligned}$$

Therefore when the marginal import cost is higher from country  $L$ , the total import-augmenting FTA formation hurts the importing country when it decreases the import from country  $H$  with the lower marginal import cost and the marginal benefit of import from country  $L$  is non-positive. This is because the import substitution from country  $H$  to country  $L$  given the total import increases the total import cost and the increase in the total import enabled by more imports from country  $L$  further damages the import country due to the worsened terms of trade.

Thus there holds the following result with more reservations than in Proposition 2.

**Proposition 5** *Suppose that the switch from the optimal uniform tariff policy to the FTA formation with country  $L$  increases the total output but decreases the import from country  $H$ , i.e.,  $X_T^L > X_T^{U*}$  but  $X_H^L < X_H^{U*}$ . Then the importing country gets worse off under the FTA formation with country  $L$  than under the optimal uniform tariff policy if there hold (i)  $\frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} < 0$  and (ii)  $\frac{\partial W(\mathbf{X}^{U*})}{\partial X_H} - \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} > 0$ .*

### 4.3 FTA Partner Switch and Changes in Welfare

As has been made clear, we are unable to wholly extend the analysis in perfect competition to imperfectly competitive markets. In particular, it is generally hard to get clear-cut welfare comparison between the optimal uniform tariff policy and the FTA formation.

However once we confine ourselves to the marginal costs given by (BP-MC), i.e.,  $C'_i(x_i) = c_i + \frac{x_i}{s_i}$ , which allows us to fully characterize the optimal discriminatory tariff policy, then we can obtain several interesting conditions for the better FTA candidate by using the following useful property of the equilibrium given any tariff policies.

**Lemma 3** *Assume that the marginal cost function in each exporting country is given by (BP-MC). Then given the conjectural variations and the numbers of active firms in the exporting*

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<sup>17</sup>Let us express with  $\widehat{X}_i^U(t_U)$  the equilibrium aggregate output by exporting country  $i \in \{H, L\}$ , with  $\widehat{X}_T^U(t_U) := \widehat{X}_H^U(t_U) + \widehat{X}_L^U(t_U)$  the equilibrium total output, and with  $\widehat{W}^U(t_U) := W(\widehat{X}_H^U(t_U), \widehat{X}_L^U(t_U))$  the associated welfare of the importing country. Then at the optimal uniform tariff rate  $t_U^*$ , there holds

$$0 = \widehat{W}'_U(t_U^*) = \frac{\partial W(\mathbf{X}^{U*})}{\partial X_H} \frac{d\widehat{X}_H^U}{dt_U} + \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} \frac{d\widehat{X}_L^U}{dt_U}.$$

Therefore unless the outputs by both countries are decreasing in the uniform tariff rates, there does not hold in general  $\frac{\partial W(\mathbf{X}^{U*})}{\partial X_H} \frac{\partial W(\mathbf{X}^{U*})}{\partial X_L} < 0$ .



countries, the equilibrium total output  $X_T$  is kept constant if  $\sum_k n_k \cdot \frac{t_k}{\frac{1}{s_k} - \lambda_k P'(X_T)}$  is constant given  $X_T, \mathbf{n} = (n_H, n_L)$ , and  $\boldsymbol{\lambda} = (\lambda_H, \lambda_L)$ .

This can be proven as follows. First, when the marginal costs are given by (BP-MC), the first-order condition for profit maximization by each exporting firm, (9), is rewritten as

$$P(X_T) + \frac{\lambda_i}{n_i} X_i P'(X_T) - \left( c_i + \frac{X_i}{s_i n_i} + t_i \right) = 0, \quad (19)$$

which gives rise to the following quasi-reaction function of exporting country  $i$ .

$$X_i = R^i(X_T, t_i) = n_i \cdot \frac{P(X_T) - (c_i + t_i)}{\frac{1}{s_i} - \lambda_i P'(X_T)}.$$

The market equilibrium requires

$$X_T = \sum_k n_k \cdot \frac{P(X_T) - c_k}{\frac{1}{s_k} - \lambda_k P'(X_T)} - \sum_k n_k \cdot \frac{t_k}{\frac{1}{s_k} - \lambda_k P'(X_T)},$$

which establishes Lemma 3 above.

Using this Lemma 3, we directly compare the welfare between the FTA formation with country  $H$  and the one with country  $L$ , where one should remember that the optimal discriminatory tariff is higher for country  $L$  than for country  $H$ . We do this job by supposing that the importing country, initially having a FTA with country  $L$ , switches the partner to country  $H$  keeping the same total import volume.

For making the analysis sensible enough, we focus our attention on the case in which the initial FTA with country  $L$  imposes a strictly external tariff,  $t_H^L > 0$ . Then the import substitution from the old partner  $L$  to the new partner  $H$  requires adjustments in the tariff policies  $\mathbf{t} = (t_H, t_L)$ . In view of Lemma 3, the tariff policies associated with this import substitution must satisfy

$$\sum_k n_k \cdot \frac{t_k}{\frac{1}{s_k} - \lambda_k P'(X_T)} = n_H \cdot \frac{t_H^L}{\frac{1}{s_H} - \lambda_H P'(X_T^L)}. \quad (20)$$

Then as the total output is unchanged at  $X_T^L$ , our marginal import cost from each country can be replaced with what we may call the *constrained marginal import cost*, which shows the marginal import cost from each exporting country when the total import volume is kept constant.

As is shown by (10), given the marginal cost (BP-MC), the export price of each exporting country, given by

$$v^i(X_i, X_T) = C'_i \left( \frac{X_i}{n_i} \right) - \frac{\lambda_i}{n_i} X_i P'(X_T) = c_i + \left( \frac{1}{s_i n_i} - \frac{\lambda_i}{n_i} P'(X_T) \right) X_i,$$

depends only on its export and it is linear in the own export when the total import volume  $X_T$  is constant. and thus we may define its associated constrained marginal import cost, denoted by  $\overline{MIC}^i(X_i, X_T)$ , by

$$\begin{aligned} \overline{MIC}^i(X_i, X_T) &:= C'_i \left( \frac{X_i}{n_i} \right) + \frac{X_i}{n_i} C''_i \left( \frac{X_i}{n_i} \right) - 2 \frac{\lambda_i}{n_i} X_i P'(X_T) \\ &= c_i + 2 \left( \frac{1}{s_i n_i} - P'(X_T) \frac{\lambda_i}{n_i} \right) X_i. \end{aligned}$$

Note that in general this constrained marginal import cost has the following relation to the unconstrained one given by (MIC).

$$MIC^i(X_i, X_j) = \overline{MIC}^i(X_i, X_j) - P''(X_T) \sum_k \frac{\lambda_k}{n_k} X_k^2,$$

so that (MIC-ALT) implies

$$\overline{MIC}^i(X_i, X_T) = -c_i - 2t_i + 2P(X_T). \quad (21)$$

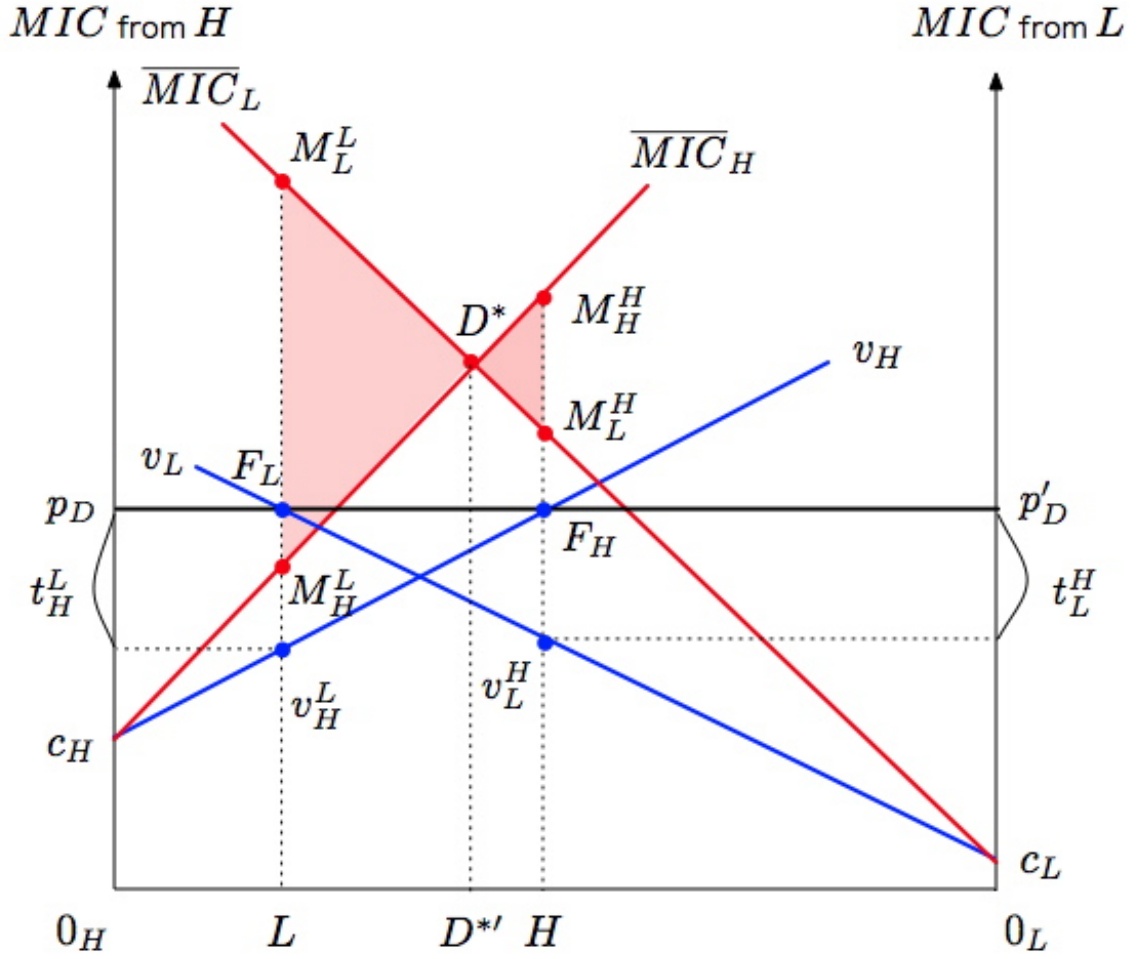


Figure 3: FTA Partner Switch – Case 1

Each country's constrained marginal cost curve is thus linear and strictly upward sloping as illustrated by Figures 3 and 4. In each, the line segment  $0_H 0_L$  is equal to the total import given by  $X_T^L$  associated with the domestic price  $p_D$  in the importing country. The import from country  $H$  is measured rightward from point  $0_H$ , while the import from country  $L$  is measured leftward from point  $0_L$ . The upward sloping curve  $c_i v_i (i = H, L)$  shows the export price of exporting country  $i$  and the upward sloping curve  $c_i \overline{MIC}_i (i = H, L)$  its associated constrained marginal import cost curve.

The equilibrium of FTA with country  $L$  is shown by point  $F_L$ , where the domestic price line  $p_D p_{D'}$  crosses the export price curve of country  $L$ . Of the total import,  $L0_L$  comes from country  $L$ , and  $0_H L$  from country  $H$ . The tariff imposed on country  $H$ ,  $t_H^L$ , is measured by the difference between its export price (measured by  $Lv_H^L$ ) and the domestic price, i.e., the line segment  $v_H^L F_L$ .

Now take the case illustrated by Figure 3 first and consider the switch of the FTA partner to country  $H$  given the total amount of imports. This requires the export price of country  $H$  to be equal to the domestic price, which is shown by point  $F_H$ . More import of  $0_H H$  comes from country  $H$ , and the import from country  $L$  decreases to  $0_L H$  facing the tariff of  $F_H v_L^H$ .

The change in the total import costs are measured by the areas  $\Delta M_L^L M_H^L D^*$  (showing the decreased costs) and  $\Delta M_L^H M_H^H D^*$  (showing the increased costs), where point  $D^*$  shows the equalized marginal import costs from the two exporting countries. When the importing country expands its import from country  $H$  up to  $0_H H$ , the increased imports  $LD^*$  increases the import costs from country  $H$  as much as the trapezoid shape of  $M_H^L LD^* D^*$  but decreases as much as the trapezoid shape of  $M_L^L LD^* D^*$ , which gives rise to net decrease in the total costs as much as  $\Delta M_L^L M_H^L D^*$ . But the further import from country  $H$  raises the import cost from country  $H$  as much as  $D^* D^* H M_H^H$  but reduces the import cost from country  $L$  as much as  $D^* D^* M_L^H$ , which amounts to net increase in the total import costs by  $\Delta M_L^H M_H^H D^*$ . Therefore the importing country gains from the FTA partner switch as much as  $\Delta M_L^L M_H^L D^*$  minus  $\Delta M_L^H M_H^H D^*$ . As one can verify in view of the figure, the importing country is actually better off if and only if the following condition holds.

♣ **Welfare-improving condition:** The sum of country  $H$ 's marginal import cost minus country  $L$ 's at two FTA equilibria is strictly positive, i.e.,

$$\left( \overline{MIC}^L(X_L^L, X_T^L) - \overline{MIC}^H(X_H^L, X_T^L) \right) + \left( \overline{MIC}^L(X_L^H, X_T^L) - \overline{MIC}^H(X_H^H, X_T^L) \right) > 0.$$

Unlike Figure 3, Figure 4 indicates the case in which the export price of country  $H$  supplying the total import, measured by  $\bar{v}_H$ , is lower than the domestic price  $p_D$ , so that the FTA formation with country  $H$  requires the total import to increase. When the market demand curve of the importing country is given by the downward-sloping curve  $DD'$ , then the FTA formation requires the market equilibrium to settle at point  $F_H$  and to totally exclude the import from country  $L$ . The associated increase in the import costs is now measured by  $\Delta D^* \bar{M}_H c_L$  plus the trapezoid area  $\square \bar{M}_H p_D' F_H M_H^H$ . Note that when we extend the constrained marginal import cost curve of country  $L$  up to what is shown by the curve  $\overline{MIC}^L c_L'$  and thus literally follow the above welfare-improving, then the increased import cost amounts to the area  $\Delta D^* M_L^H M_H^H$ , which is larger than what is actually incurred. Thus if the condition is satisfied, then the switch of the FTA partner is definitely welfare-improving for the importing country. For this reason, we hereafter employ the above condition for evaluating whether the switch of the FTA partner improves the importing country's welfare.

Let us give a more precise expression for this welfare-improving condition. By virtue of (21), the difference in the marginal import costs is equal to

$$\overline{MIC}^L(X_L, X_T) - \overline{MIC}^H(X_H, X_T) = c_H - c_L + 2(t_H - t_L), \quad (22)$$

so that there hold

$$\overline{MIC}^L(X_L, X_T) - \overline{MIC}^H(X_H, X_T) = \begin{cases} c_H - c_L + 2t_H^L & \text{under the FTA with country } L \\ c_H - c_L - 2t_L^H & \text{under the FTA with country } H \end{cases}$$

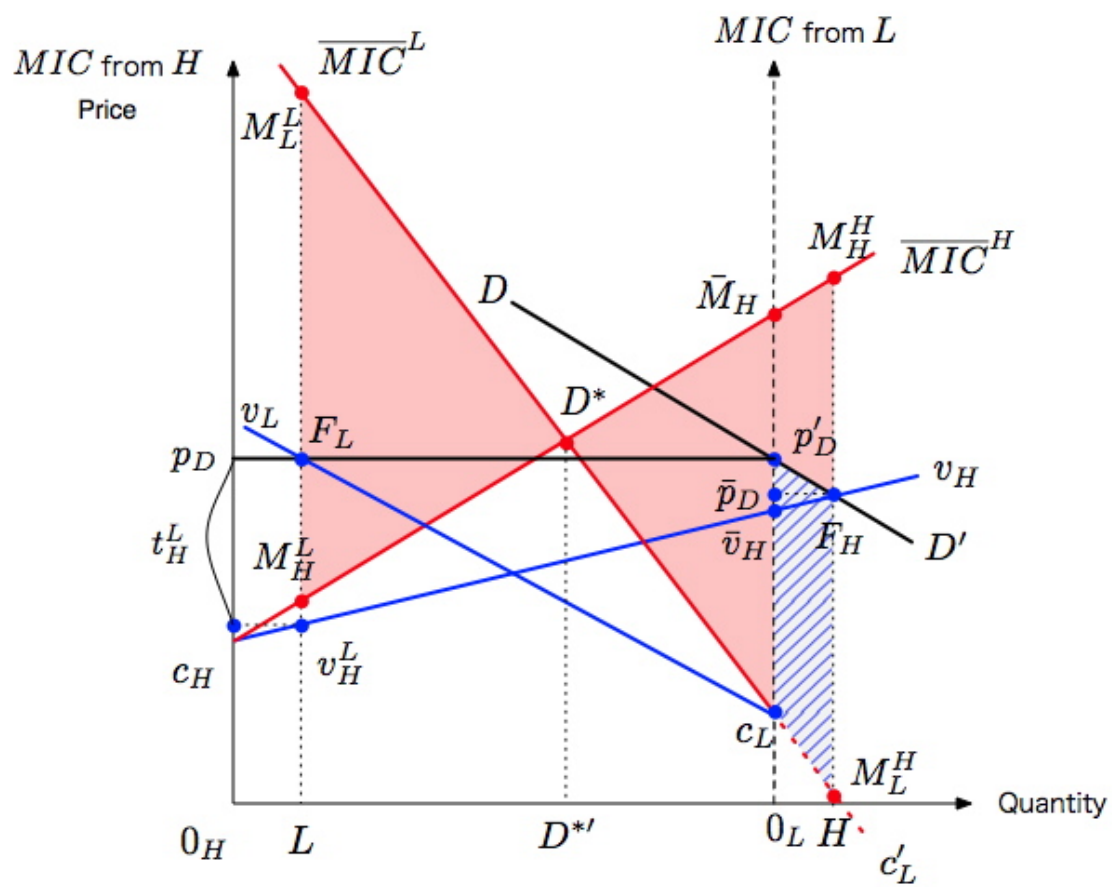


Figure 4: FTA Partner Switch – Case 2

Then the welfare-improving condition is given by

$$c_H > c_L + (t_L^H - t_H^L). \quad (23)$$

The tariff rate required,  $t_H^L$ , leading to the same total import volume as in the FTA with country  $L$ , should satisfy (20), i.e.,

$$t_L^H = \frac{n_H}{n_L} \cdot \frac{\frac{1}{s_L} - \lambda_L P'(X_T)}{\frac{1}{s_H} - \lambda_H P'(X_T)} t_H^L,$$

which allows us to rewrite the welfare-improving condition (23) as follows.

**Proposition 6** *Suppose that the marginal costs are given by (BP-MC). When the importing country initially forms a FTA with country  $L$  with the external tariff  $t_H^L$  to country  $H$ , then its switch in the FTA partner to country  $H$  while keeping the total import constant makes the importing country's welfare better off if there holds*

$$c_H > c_L + \left\{ \frac{n_H}{n_L} \cdot \frac{\frac{1}{s_L} - \lambda_L P'(X_T)}{\frac{1}{s_H} - \lambda_H P'(X_T)} - 1 \right\} t_H^L.$$

There are a couple of interesting special cases for discussion. First, consider the case discussed by Bhagwati and Panagariya (1996), i.e.,  $c_H > c_L$  and  $0 < s_L < s_H = +\infty$ . Then the welfare-improving condition is given by

$$c_H > c_L + \left\{ \frac{n_H}{n_L} \cdot \frac{\frac{1}{s_L} - \lambda_L P'(X_T)}{(-\lambda_H P'(X_T))} - 1 \right\} t_H^L.$$

As the braced term on the right hand side is strictly positive for  $n_H \geq n_L$ , the importing country finds it more beneficial to form a FTA with the exporting country having the higher export-choke price and more firms, i.e., the country which is less efficient but more competitive in the sense that it has more active firms.

The second is the case in which the two exporting countries are symmetric except the export choke price  $c_i$ , then the welfare-improving condition in the above proposition reduces to  $c_H > c_L$ . Thus it is more preferable for the importing country to form a FTA with country  $H$  having the higher export-choke price than with country  $L$ .

Now we can further extend the present approach to welfare comparison between any two tariff policies,  $\mathbf{t}' := (t_H', t_L')$  and  $\mathbf{t}'' := (t_H'', t_L'')$ . In view of (21), we may rewrite the welfare-improving condition above and establish

**Proposition 7** *Suppose that the marginal costs are given by (BP-MC), and consider any two tariff policies  $\mathbf{t}' := (t_H', t_L')$  and  $\mathbf{t}'' := (t_H'', t_L'')$  satisfying*

$$\sum_k n_k \cdot \frac{t_k'}{\frac{1}{s_k} - \lambda_k P'(X_T)} = \sum_k n_k \cdot \frac{t_k''}{\frac{1}{s_k} - \lambda_k P'(X_T)} > 0, \quad (\text{TC})$$

where  $X_T$  is the equilibrium total import volume associated with the tariff policy  $\mathbf{t}'$ . When the change in the tariff policies from  $\mathbf{t}'$  to  $\mathbf{t}''$  entails import expansion from country  $H$ , then the importing country gets better off by such a policy switch if there holds

$$c_H - c_L > (t_L' + t_L'') - (t_H' + t_H''). \quad (\text{BT})$$

*If the change in the tariff policies entails import expansion from country  $L$ , the welfare-improving condition is given by (BT) where the inequality is reversed.*

Proposition 6 is a special case of the above proposition where the two tariff policies are those associated with FTA formations. We may also use this proposition to compare the welfares between the uniform tariff policy and the FTA formation. Consider any uniform tariff rate  $t^U$  as the initial tariff policy. Then Proposition 7 indicates that, given the total import volume under the uniform tariff policy, the FTA formation with country  $H$  is better for the importing country than the uniform tariff policy if there holds  $c_H - c_L > t_L^H$  where  $t_L^H > 0$  follows from (TC), which holds when  $c_H$  is sufficiently greater than  $c_L$ .<sup>18</sup>

On the hand, what if the importing country forms a FTA with country  $L$  instead of employing the uniform tariff policy. Then the welfare-improving condition is given by  $c_H - c_L < -t_H^L$ , where  $t_H^L > 0$  follows from (TC). Since this never holds, the importing country gets strictly worse off than under the uniform tariff policy after forming a FTA with country  $L$ . Of course, the proposition never denies the possibility of the importing country's welfare improvement by adjusting the external tariff and thus the total import volume, though such a possibility is extremely limited.

**Corollary 1** *Suppose that the marginal costs are given by (BP-MC) in both exporting countries. Then when the importing country switch the trade policy from any uniform tariff  $t^U (> 0)$  to a FTA formation by keeping the total import volume, it always gets worse off by choosing country  $L$  as the FTA partner, while it gets better off by choosing country  $H$  when there the choke price of country  $H$  is greater than that of country  $L$  plus the external tariff  $t_L^H$  required under the FTA.*

As with the welfare-improving FTA formation with country  $H$  mentioned in the above corollary, there are two remarks in order here. First, when the initial uniform tariff policy is the optimal one maximizing the importing country's welfare, the welfare improvement discussed above implies that the FTA formation with country  $H$  is further beneficial because the importing country can adjust the external tariff rate.

Second, the switch in the trade policy mentioned in Proposition 7 implies that the post-FTA external tariff rate becomes higher than the initial uniform tariff rate. But as pointed above, the importing country can realize further welfare improvement by the external tariff rate, so that it may be better off even with the lower external tariff than under the optimal uniform tariff policy. In fact, this is likely enough to happen if the initial uniform tariff rate is not optimal but sufficiently higher than the optimal level.

## 5 Extensions of Analysis and Concluding Remarks

Our analysis in the preceding sections has elucidated that the importing country, when it forms a FTA, has an incentive to choose the exporting country with the smaller marginal import costs. And when we confine ourselves to either constant or linearly increasing marginal costs, the marginal cost from the country with the lower choke price (i.e., the smaller  $c_i$ ) becomes smaller. In this sense, the importing country tends to choose the less efficient exporting country as its FTA partner.

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<sup>18</sup>Of, this cost difference should be too large, for the importing country finds it optimal to exclude the imports from country  $H$  even when it is constrained to employ uniform tariff policies. See footnotes 5 and 14.

## 5.1 Tariff Discrimination with Domestic Production

There are several possible directions for extending the analysis. The most important is incorporation of domestic production by the importing country. Insofar as we confine ourselves to perfect competition, it is immediate to apply our discussion to such a case, for we may replace the gross consumption benefit function with the gross import benefit one.<sup>19</sup> Extension to imperfect competition is not so hard, either.

For the convenience of description, we hereafter call the importing country the “home country” with super- or sub-scripts  $M$ . Let us denote by  $x_M$  the individual output of the domestic firms, by  $C_M(x_M)$  its total cost function, by  $n_M$  the number of firms, by  $\lambda_M$  its conjectural variations and by  $X_M := n_M x_M$  the total domestic output in the home country. Then its welfare is now expressed by

$$W = U(Z_T) - n_M C_M \left( \frac{X_M}{n_M} \right) - \sum_{k=H,L} X_k \cdot IMR^k(X_k, Z_T),$$

where  $Z_T := \sum_{k=H,L,M} X_k$  denotes the total output. The equilibrium condition for each industry in each country is still expressed by (9) where  $X_T$  is now replaced with  $Z_T$  and we newly introduced  $t_M$  denoting the specific production tax on the domestic firms. The analysis can be easily compared to the previous one once we devise the quasi-reaction function of the domestic industry which represents its equilibrium total output against the total imports  $X_T$  as follows.

Let  $R^M(Z_T, t_M)$  indicate the quasi-reaction function of the domestic industry, and consider the market equilibrium condition given  $X_T$ , i.e.,

$$Z_T = R^M(Z_T, t_M) + X_T,$$

which defines the total output as a function of the total import given the tax on the domestic firms, i.e.,  $Z_T = \hat{Z}^T(X_T, t_M)$ . Substitute this for  $Z_T$  in  $R^M(Z_T, t_M)$  and let  $\hat{R}^M(X_T, t_M) := R^M(\hat{Z}^T(X_T, t_M), t_M)$  express its new quasi-reaction function. Then we may rewrite the welfare of the home country as below.

$$\begin{aligned} \widehat{W}(\mathbf{X}, t_M) &= U \left( X_T + \hat{R}^M(X_T, t_M) \right) - n_M C_M \left( \frac{\hat{R}^M(X_T, t_M)}{n_M} \right) \\ &\quad - \sum_{k=H,L} X_k \cdot \widehat{IMR}^k(X_k, X_T, t_M), \end{aligned}$$

where  $\mathbf{X} := (X_H, X_L)$  and  $\widehat{IMR}^i(X_i, X_T, t_M) := IMR^i(X_i, X_T + \hat{R}^M(X_T, t_M))$ . The opti-

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<sup>19</sup>Insofar as the domestic market is perfectly competitive, the consumption benefits minus the domestic production depends only on the domestic price, which also uniquely determines the total import demand. Taking the inverse of the import demand function, we can then express the consumption benefits minus the domestic production costs as a function of the total import volume, which serves as our  $U(X_T)$  in the text.

mal tariff discrimination then requires  $\frac{\partial \widehat{W}(\mathbf{X}^D, t_M)}{\partial X_i} = 0$ , which gives rise to

$$t_i^D = x_i^D C_i''(x_i^D) + X_i^D \frac{\partial \widehat{IMR}^i(X_i^D, X_T^D, t_M)}{\partial X_i} + \sum_{k=H,L} X_k^D \frac{\partial \widehat{IMR}^i(X_i^D, X_T^D, t_M)}{\partial X_T} \\ + \widehat{IMR}^M(X_M^D, X_T^D, t_M) \left( -\frac{\partial \widehat{R}^M(X_T^D, t_M)}{\partial X_T} \right),$$

where  $X_M^D := \widehat{R}^M(X_T^D, t_M)$  and use was made of (9) for the domestic firms. Compared with the case of no domestic production mentioned in Proposition 4, the last positive common term, showing the effect of the individual monopoly rent earned by the domestic industry, is newly added to the optimal tariff formula. And, given the production tax on the domestic firms,  $t_M$ , the difference in the optimal discriminatory tariffs is still characterized by Proposition 3.

One possible difference compared with the previous discussion can be found when the marginal cost of each firm is constant and we allow the government of the home country to optimally set the production tax on the domestic firms and maximize the welfare. The government tries to preclude any imports from the country with the greater marginal costs than the domestic firms. This can be shown as follows.

First, when the marginal costs are constant, the optimal discriminatory tariff on the import from country  $i$  is given by

$$t_i^D = -\frac{\lambda_i}{n_i} X_i P'(Z_T^D) - P''(Z_T^D) \left\{ 1 + \frac{\widehat{R}^M}{\partial X_T} \right\} \sum_{k=H,L} \frac{\lambda_k}{n_k} X_k^{D2} + (P(Z_T^D) - c_M) \left( -\frac{\widehat{R}^M}{\partial X_T} \right)$$

where use was made of  $IMR^i(X_i, Z_T) = -\frac{\lambda_i}{n_i} X_i P'(Z_T)$ .

Second, the optimum condition for choosing the domestic production tax, i.e.,  $\frac{\partial \widehat{W}}{\partial t_M} = 0$ , yields

$$P(Z_T^D) - c_M = -P''(Z_T^D) \sum_{k=H,L} \frac{\lambda_k}{n_k} X_k^{D2} < 0,$$

which implies that the government actually heavily subsidizes the domestic production.

Put this into the previous tariff formula, and obtain  $t_i^D = (P(Z_T^D) - c_i - t_i^D) + P(Z_T^D) - c_M$ , or equivalently

$$\frac{t_i^D}{2} = P(Z_T^D) - \frac{c_i + c_M}{2}.$$

Thus in view of (9), there holds

$$-\frac{\lambda_i}{n_i} X_i^D P'(Z_T^D) = P(Z_T^D) - c_i - t_i^D = \frac{c_M - c_i}{2} \leq 0,$$

which implies  $X_i^D = 0$ .

**Proposition 8** *Suppose that the marginal costs of firms are constant in each country. Then when the home country's government sets the optimal tax-cum-subsidies on the domestic industry as well as the tariffs on the imports from abroad, the optimal tariff discrimination precludes the imports from the exporting country with the greater marginal costs than the domestic industry.*



## 5.2 FTA Formation and Gains from Export Expansion

The second extension is the model to take account of the gains as the FTA partners. FTA agreements give mutual tariff reduction between the partners, so that each country as the exporter to the partner can also gain the benefits from export expansion. By extending our model in the previous section to the familiar reciprocal dumping model discussed by Brander and Krugman (1983), we can explore this problem.<sup>20</sup>

More specifically, consider the world of three countries,  $M, H, L$ , where  $M$  denotes now simply the third country  $M$ . Each country has the identical demand function,  $n_i$  identical firms with conjectural variation  $\lambda_i$  and constant marginal costs  $c_i$  where  $c_L < c_M < c_H$ . We assume that each country's market is segmented. Then our previous analysis is the one just focusing on an individual country's domestic market.

As we have discussed, each country as an importer has an incentive to choose the exporting country with the greater marginal cost, so that countries  $H$  and  $M$  want to accept each other as the FTA partner but country  $H$ , though desiring a FTA with country  $M$ , cannot form any FTA. Even from the viewpoint of an exporter, countries  $H$  and  $M$  would prefer a FTA between  $H$  and  $M$ . This is because when either forms a FTA with country  $L$  with the least marginal costs, it faces the more aggressive competition with the smaller profits than under the FTA with the other country.

## 5.3 Directions for Further Research

We have explored the FTA formation among the countries trading a homogeneous good. Among the limitations of the approach, the greatest one is due to our partial equilibrium approach. A country, trading various types of commodities and services, cannot decide its trade policy on any specific good without taking account of the possible effects on the trade of other goods. Whether the markets are perfectly or imperfectly competitive, it is necessary to incorporate this feature of interdependence in trade, i.e., substitution and complementarity among the traded goods.<sup>21</sup>

There have already been many studies dealing this issue, but, to my best knowledge, most of them depend on the model specification, often assuming symmetric among the countries, which facilitates computation of equilibria and welfare without shedding lights on what motivates each country's choice of the partner for FTA formation or economic integration in general. There is still much to be done.

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<sup>20</sup>For example, Yi (1996) and Yi (2000) build a general equilibrium model of reciprocal dumping and discuss the welfare change due to a country's participating in a FTA or a CU by taking account of the gains as the exporter, though the countries are all symmetric.

<sup>21</sup>Hwang and Mai (1991) discusses the problem of tariff discrimination for product differentiation by using a quadratic utility function. They explore how the cross substitution term in the linear demand affects the tariff levels and its difference between the two exporting countries.

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