# A Life-Cycle Model of Entrepreneurial Choice: Understanding Entry into and Exit from Self-Employment\*

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#### Abstract

Data from the 1979 cohort of the National Longitudinal Survey of Youth (NLSY79) show that self-employment (nonfarm or nonprofessional) accounts for as high as 7 percent of all yearly labor supplies by young white males (ages 20-39 in years 1979-2000). On the other hand, nearly 30 percent of individuals in the data have at least one year of experience as a self-employer in the covered years. The goal of this paper is to give a coherent framework that accounts for these two contrasting figures which together suggest the importance of understanding not only entry into but exit from self-employment as well. Specifically, I present and estimate a life-cycle model of entrepreneurial choice and wealth accumulation, using a subsample of white males aged 20 to 39 from the NLSY79. The model also includes two basic components of human capital (educational attainment and labor experience) aimed at a better capturing of the observed patterns of labor supply as well as those of income profiles and wealth accumulation over the life cycle. The estimation results show that nonpecuniary benefits from continuing self-employment are large enough to justify the observed persistence of being self-employed. Policy experiments with the use of the estimated model, however, indicate that pecuniary factors also have large impacts on the formation and continuation of self-employed businesses. Specifically, I find that while both direct subsidies for self-employment and enhancement of the human capital specific to self-employment only encourage entries with short durations, relaxation of borrowing constraints, on the other hand, encourages entries into self-employment and makes the average duration longer, especially for the non-college educated.

Keywords: Self-Employment; Entry and Exit; Human Capital; Borrowing Constraints JEL classification numbers: J21 (Labor Force and Employment, Size, and Structure); J24 (Human Capital; Skills; Occupational Choice; Labor Productivity); L26 (Entrepreneurship)

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## 1 Introduction

Self-employment constitutes a sizeable portion of the labor force in the United States.<sup>1</sup> Data from the 1979 cohort of the National Longitudinal Survey of Youth (NLSY79) show that self-employment (nonfarm or nonprofessional)<sup>2</sup> accounts for as high as 7 percent of all yearly labor supplies by young white males (ages 20-39 in years 1979-2000). A more noticeable fact, however, is that nearly 30 percent of individuals in the data have at least one year of experience as a self-employer in the covered years. These two contrasting figures seem to suggest the unstable nature of entrepreneurship, and hence the importance of understanding both *entry* into and *exit* from self-employment in a coherent framework. Any evaluation of government policies (such as the U.S. Small Business Administration's loan programs and self-employment assistance programs) which are intended at encouraging entries of self-employment should also include the consideration of exits from it. This is because they may also increase the number of individuals who soon exit from self-employed businesses and thus may not change the overall portion of self-employers as is intended.

This paper aims to provide a framework to consider the above issue with the use of observational data. Specifically, it presents and estimates a life-cycle model of entrepreneurial choice and wealth accumulation, using a subsample of white males aged 20 to 39 from the NLSY79. The main target of estimation is to well replicate the observed patterns of entry into and exit from self-employment as well as those of income profiles and wealth accumulation over the life cycle. The estimated model is then used to conduct three policy experiments that are intended to encourage the formation and the continuation of self-employed businesses: (i) relaxation of borrowing constraints, (ii) lump-sum capital subsidies for self-employment, and (iii) enhancement of the human capital specific to self-employment (training for entrepreneurial skill). These policy experiments can help the government determine the effective policies to encourage stable self-employment.

My dynamic model is a natural extension of Evans and Jovanovic's (1989) static model of entrepreneurial choice to a competitive labor supply model in a life-cycle framework.<sup>3</sup> In my model, an individual, as either non-college or college educated, starts decisions after he finishes schooling. In each period (calender year), an individual, after observing shocks to his preference and income opportunities, decides on the mode of employment and obtains

<sup>&</sup>lt;sup>1</sup>In this paper, the empirical counterpart of someone starting a business is becoming his or her own self-employer, and the words "self-employment" and "entrepreneurship" are used interchangeably throughout. The definition of self-employers in U.S. surveys such as the Current Population Survey (CPS) and the one used in the present study (NLSY79) is "those who work for profit or fees in their own business, profession, trade or operate a farm." The use of this definition for doing a business, instead of another definition that is also widely used (business ownership), is partly because of this paper's emphasis on the labor side with the aim of highlighting the role of human capital in entrepreneurship. In addition, the majority of new businesses are likely to start as self-employed businesses. An evidence from the Panel Study of Entrepreneurial Dynamics (PSED) indicates that about seventy five percent of business startups are self-employed ones: almost one-half of the nascent entrepreneurs plan to start as a sole legal owner of the new firm, and one-quarter of them expect to be partnerships. Only one-fifth of them consider a form of corporation. Since the data I use for this study does not contain such information, I may be missing some entrepreneurs who start their business in the form of a coroporation, counting them as "wage workers". I may also be missing changes in the legal status: some successful self-employers may become a wage worker when they change the legal form of their firms to corporation, though the data in the present paper does not include such detailed information, either.

<sup>&</sup>lt;sup>2</sup>I exclude professionals (doctors, lawers and accountants) and farmers from this study. See Subsection 5.1 for details.

<sup>&</sup>lt;sup>3</sup>I do not explicitly model labor market frictions in a framework of, for example, job search. Rather, the "bare-bones" framework I adopt is a dynamic model of competitive labor supply, and such factors as possible frictions in the labor marker are modeled as unobserbable residuals.

income from the job. He then determines the amount of consumption out of the sum of the income from working and the returns from the accumulated asset. He obtains utility from consumption as well as disutility from working. The objective of each individual is to maximize the expected present discounted value of utility over a finite horizon from the first decision period to the last. The main difference between self-employment and paid employment is in functional forms of income opportunities. That is, I assume that functional forms of one's income opportunities depend on whether he works as a self-employer ("becomes his own boss") or is employed by someone else.

A key feature of the proposed life-cycle model, which has not been focused on much in the literature, is the addition of human capital (educational attainment and labor experience) to the analysis of self-employment. The main motivation for incorporating labor experience into the model is to explain the observed increases in self- and paid employment incomes over the life-cycle (see Subsubsection 5.2.3 for details). Significant differences between the non-college educated (high-school graduates and dropouts) and the college educated (those with some college education) in self- and paid-employment also motivate me to incorporate a variable for educational attainment into the model. Table 1 shows that the "college premium" in annual income is almost the same both for self-employment (40.9%) and full-time paid-employment (42.3%).

Table 2 displays the differences, other than the income, between the non-college educated and the college educated. In comparison with the college educated, non-college educated workers are more likely to have self-employment experience until age 39 (31.1% rather than 27.5%, called Key Fact (1)), and they spend more years before they become a selfemployer for the first time (62.7\%, rather than 74.6\%, of first entries into self-employment take place in the first eight decision periods for the non-college educated, called Key Fact (2)). The third item in Table 2 shows that they are more likely to leave self-employment after the first year (called Key Fact (3)). These numbers seem to suggest that for the non-college educated self-employment is more likely to be a "forced" or "temporary" option compared to the paid-employment, and that for the college educated it is more like a "committed" task. The inclusion of human capital (education as well as experience) in a model that explicitly considers decisions over the life cycle is thus expected to make it possible to better measure gains and the opportunity costs associated with the occupational decisions over the life-cycle. The above points constitute the major focus of the present paper. In constructing the model, I explicitly consider the heterogeneity among individuals which is not observable in the data. More specifically, through the assumption of an exogenously given (discrete) distribution of an unobserved "type" variable, I am able to treat the possible unobserved differences among individuals that may affect decisions on labor supply as well as wealth accumulation.

Given the richness of the structural life-cycle model presented below, there will be no closed-form solution for the optimal path of decisions over time. Therefore, to empirically implement the model, it is first solved numerically. Using the decision rules as in Section 4, I simulate the data and use the simulated maximum likelihood (SML) method to estimate the model parameters. The empirical data I use for the study is the NLSY79. The proposed life-cycle model yields plausible parameter estimates and shows a good fit to the main empirical patterns of entry into and exit from self-employed businesses as well as the age profiles of the labor supplies, income and net worth. The estimation results show that non-pecuniary benefits from continuing self-employment are relatively large, thus, culminating in the observed persistence of being self-employed. Using the estimates of the life-cycle model,

I perform the three aforementioned policy experiments. Since my approach explicitly solves an optimization problem and thus makes predictions about how individuals behave, I can quantify the effects on entrepreneurial decisions as well as the outcomes of the alternative values of the parameters.

The first experiment is to relax the borrowing constraints for all individuals. I find that a moderate relaxation of the borrowing constraints has large impacts on the formulation and continuation of self-employed businesses. Specifically, with \$30,000 as a lower bound on asset holdings (the estimated one is between \$10,000 and \$18,000 for most of the state variables), the average percentage (over the years covered in the actual data) that self-employment occupies of all yearly labor supplies increases nearly 50 percent (7 percent to 11 percent). At the same time, the percentage of non-employment decreases while the one for full-time paid employment does not change much. These results seem to suggest that the indirect effect from the relaxation of the borrowing constraints that makes individuals more likely to choose non-employment is dominated by the direct effect that improves consumption smoothing over time and hence makes individuals more eager to do self-employment despite being a riskier choice than wage employment. The average duration of self-employment also becomes longer. Nearly 90 percent of self-employers continue self-employment next year while in the actual data the number is 78 percent. Focusing on educational differences, I find that the effects of relaxing the borrowing constraints are larger for the non-college educated.

The second and the third experiments are more direct interventions: capital subsidies and enhancement of the human capital specific to self-employed work. I find that both policies induce more individuals to enter into self-employment, though they make the average duration of self-employment shorter. The results from the three policy experiments show that the relaxation of borrowing constraints encourages entries into self-employment with longer durations, whereas both direct and indirect incentives only encourage entries with short durations. In conclusion, the relaxation of borrowing constraints would be the most effective of the three policy experiments in encouraging stable self-employment.

The rest of the paper is organized as follows. Following the review of the related literature in the next section, in Section 3 I present a structural model for entrepreneurial choice and wealth accumulation over the life-cycle. Because of the richness of the model, it does not permit an analytical solution. Section 4 thus explains how the model is numerically solved. I then describe the data that is used for estimation in Section 5. After describing the method of estimation, the estimation results are presented in Section 7, followed by discussions of the model fit and implications of the parameter estimates. Section 8 then outlines the results from the three policy experiments. Section 9 concludes the paper.

### 2 Related Literature

The literature on self-employment and entrepreneurship is vast. Here I confine my attention to the studies that are closely related to this paper.<sup>4</sup>

Evans and Jovanovic (1989) is the first study that gave parameter estimates of a structural model of entrepreneurial choice. One of their main findings is that the decision to become an entrepreneur depends positively on wealth, and they interpret this as evidence

<sup>&</sup>lt;sup>4</sup>For studies that do not explicitly use behavioral models, see e.g. Holtz-Eakin, Joulfaian, and Rosen (1994a,b), Dunn and Holtz-Eakin (2000) and Hurst and Lusardi (2004). Evans and Leighton (1989) is the first study that reports empirical findings of dynamic aspects of self-employment, making use of longitudinal data.

of the significance of borrowing constraints.<sup>5</sup> In addition, according to their estimates, the probability of someone being a constrained self-employer is much higher (62.5 times) than the probability of him being a unconstrained self-employer, suggesting that the borrowing constraints are significant and it may be binding for almost all starting self-employers. This result leads to the following two predictions. First, the borrowing constraints prevent some individuals from entering into self-employment. If it were removed, the average probability of someone becoming a self-employer would increase by 34 percent. Second, the borrowing constraints limit investment in business by someone who is already a self-employer. According to their estimates, this is especially so for those with a higher ability and a lower level of asset.<sup>6</sup>

Evans and Jovanovic's (1989) structural model is, however, static, and hence may be missing some important factors that are related to dynamic incentives over life cycle. They use an older version of the National Longitudinal Survey of Young Men, and their way of estimation is whether a white male in the sample in 1976 that consists of wage workers became a self-employed worker or remained as a wage worker in 1978. To assess as precisely as possible the significance of borrowing constraints on entry into self-employment, one needs to know about how wealth is accumulated up to the point of entry. This consideration motivates me to propose and estimate a dynamic model of entrepreneurial choice and wealth accumulation. Another important omission from Evans and Jovanovic (1989) is the exclusion of the role of educational attainment in self-employment. Although they state that "work experience and education were not substantively or statistically significant determinants of entrepreneurial earnings" (pp.821-2), this simplification may cause overprediction of entrepreneurial skills on the performance of self-employment. To capture as precisely as possible the effects of observed and unobserved characteristics on entrepreneurial choice and wealth accumulation, I incorporate two components of human capital (education and ) into earnings opportunities from self-employment as well as from paid-employment.

This paper is not the first one that structurally models the dynamics of self-employment, though. Buera (2008a) and Mondragon-Velez (2006) are two attempts that estimate structural parameters of a dynamic model of entrepreneurship.<sup>7</sup> In their dynamic models, asset accumulation is endogenously determined (model individuals decide on how much they consume and save in each period). Buera (2008a) is a synthesis that offers both analytical characterization in a continuous-time setting and structural estimation. Using the PSID

<sup>&</sup>lt;sup>5</sup>In a related issue, entrepreneurship in the presence of borrowing constraints (and precautionary saving) is also studied to better explain the observed heavy right tail of the aggregate wealth distribution in the United States. The common idea is that adding borrowing constraints in starting a business to a model economy creates a more skewed wealth distribution than precautionary savings motive alone can do. See, e.g., Quadrini (1999,2000), Castañdeda, Díaz-Giménez, and Ríos-Rull (2003), Cagetti and De Nardi (2006) and Terajima (2006). For other issues on self-employment in the macro contexts, see e.g. Li (2003), Fernández-Villaverde, Galdón-Sánchez, and Carranza (2003), and Meh (2008). These papers' focus is not on explaining transitions (entry into and exit from self-employment) at individual's level in a life-cycle framework, which is the main subject of the present paper.

<sup>&</sup>lt;sup>6</sup>In a follow-up paper, Xu (1998) corrected one puzzling finding in Evans and Jovanovic (1989) that entrepreneurial ablity and wealth are negatively correlated. Xu (1998) points out the negative correlation resulted from a downward bias in the original data, because a postive correlation is found with a less-biased wealth data.

<sup>&</sup>lt;sup>7</sup>For studies that use behavioral dynamic models with financial market imperfection to analyze different issues from the one in the present paper, see, e.g., Rosenzweig and Wolpin (1993) and Fafchamps and Pender (1997) (farmers in developing countries), Keane and Wolpin (2001) (financing for higher education), Redon (2006) (job search), Pavan (2008) (collateralized debt in consumption smoothing), and Schündeln (2006) (small manufacturing firms in depeloping countries).

(Panel Study of Income Dynamics), he finds undercapitalization of individuals who are already entrepreneurs.

In Buera's (2008a) model, human capital is not incorporated: talent that augments entrepreneurial income is treated unobserved, determined in the beginning and permanently fixed. In consideration of the fact that much effort has been devoted in the human capital literature to study how education and experience enhance one's market wage in paid employment, it is surprising that most of the literature on self-employment does not focus on human capital, treating a pool of current and to-be self-employers as homogenous (other than unobservable factors). By incorporating human capital accumulation into a dynamic framework, Mondragon-Velez (2006) estimates the model to replicate earnings and fractions of self-employers by age-education groups. Mondragon-Velez (2006) augments Buera's (2008a,b) non-monotonic (hump-shaped) relationship between the probability of transition to entrepreneurship and accumulated wealth: Because the opportunity cost of entrepreneurship (wage increases due to accumulation in human capital) becomes larger as he gets older, a larger scale of business capital is necessary to attract an individual to entrepreneurship. In this way, the relationship between the propensity to be a self-employer and accumulated wealth is non-monotonic.

In this paper, I focus on an important aspect of entrepreneurship that is not paid attention in Buera (2008a) or in Mondragon-Velez (2006): exit from self-employment. In Buera's (2008a) model, an individual remains an entrepreneur once he becomes one. When he estimates his dynamic model, Buera (2008a) only uses cross-sectional information of income and ratios of entrepreneurs to wage workers. Mondragon-Velez (2006) does not much focus on the dynamic aspects of entrepreneurship, though his model is potentially able to do so. In addition, Mondragon-Velez (2006) uses age as a dynamic component in the human capital function rather than (endogenously) accumulated experience, and does not include non-employment as a choice on labor supply, and hence does not distinguish between self-employment experience and wage experience. In the present paper, because my life-cycle model allows exit from self-employment, I can examine the dynamic aspects of self-employment.

In a close spirit to the present paper, Schjerning (2006) focuses on entry into and exit from entrepreneurship by developing and calibrating an infinite-horizon model of occupational choice and wealth accumulation. His dynamic model also incorporates human capital accumulation. Schjerning's (2006) calibration results seem to suggest the more important experience in self-employment over experience in paid-employment is in the productivity in self-employment, the stronger the effects of borrowing constraints are on the cycling between self-employment and paid-employment. There are two important differences between his model and the one in the present paper. First, while Schjerning (2006) assumes the sta-

<sup>&</sup>lt;sup>8</sup>A few exceptions that focus on the effects of human capital one entrepreneurship include Bates (1990) and Kawaguchi (2003). Bates (1990), by estimating a logit model, finds that schooling (years of education) is the most significant human capital variable that explains the longevity of small businesses: businesses owned by college educated individuals survive longer. Kawaguchi (2003), by considering a two-period model of human capital accumulation under the income risk, finds that experience-earnings profiles are flatter for self-employed workers than wage workers.

<sup>&</sup>lt;sup>9</sup>Using the 1976-2006 March CPS (Current Population Survery), Rissman (2007) calibrate a model to generate steady-state transition rates across three employment states (self-employment, paid employment, and unemployment). Her results suggest that start-up costs are not important determinants of the steady state level of self-employment because a doubling of business startup costs changes the simulated transition rates very little. By its nature, her model is not a life cycle model. She abstracts from wealth accumulation and does not incorporate the borrowing constraints into the model.

tionarity of the model environment, I employ a finite-horizon (life-cycle) model so that I can consider life-cycle aspects of labor choice and savings. Second, in my formulation, switching costs are modeled as nonpecuniary components in the utility function.

## 3 Model Structure

In this section, I present a life-cycle model of an individual's decisions on entrepreneurial choice and on wealth accumulation. The general structure is a standard one that can been seen as a natural extension of Evans and Jovanovic's (1989) static model of entrepreneurial choice: in each calender year, an individual, after observing shocks to his preference and income opportunities, decides on the mode of employment and obtains income from the job. He then determines the amount of consumption out of the sum of the income from working and the returns from the accumulated asset, obtaining utility from consumption as well as disutility from working. The objective of the individual is to maximize the expected present discounted value of utility over a finite horizon from the first decision period to the last. The rest of the section gives a formal description of the model.

### 3.1 Timeline, Choice and State Variables

The discrete decision periods are assumed to be calender years, indexed by t. The individual's sequential decision-making problem begins one year after when he has completed his education  $(t=1)^{10}$  and ends at t=T. I denote his age in decision period t by  $age_t \in \{\underline{age}, ..., \overline{age}\}$ , where  $\underline{age}$  is the first year after he completed schooling<sup>11</sup> and  $\overline{age}$  is the last decision period. I assume the retirement age is 65 for all individuals so that I set  $\overline{age} = 64$ . Two variables that characterize the individual's permanent heterogeneity are (i) his level of completed schooling (denoted by educ) and (ii) his type (denoted by type). Throughout this section the dependence of variables on educ and type notionally suppressed.

At the beginning of each decision period t, the individual first observes shocks

$$\widetilde{\epsilon}_t^l = (\widetilde{\epsilon}_t^{ls}, \widetilde{\epsilon}_t^{lw}) \in \mathbb{R}^2$$

to his preference  $u_t$  (more precisely to labor disutility; see below) where  $\tilde{\epsilon}_t^l$  is distributed according to  $N(0, \Sigma^l)$ , and shocks

$$\widetilde{\epsilon}_t^y = (\widetilde{\epsilon}_t^{ys}, \widetilde{\epsilon}_t^{yw}) \in \mathbb{R}^2$$

to his earnings opportunities for the current period  $y_t$  (see Subsection 2.3), where  $\tilde{\epsilon}_t^y$  is distributed according to  $N(0, \Sigma^y)$ . I assume that  $\tilde{\epsilon}_t^l$  and  $\tilde{\epsilon}_t^y$  are serially uncorrelated and independently distributed.

After observing the shocks and the potential amount of business scale in his self-employment, he decides on the mode of employment (non-employed, paid-employed or self-employed). If

<sup>&</sup>lt;sup>10</sup>In this paper, I do not model schooling decisions and assume that the individual's education level is exogenously given. This simplifying assumption may lead to overstatement of college premium in self-employment because the schooling decision may be partly motivated by some unobservable factors that relate to productivity in self-employment.

<sup>&</sup>lt;sup>11</sup>In the data, the starting age varies among individuals as a result of differences in last years of schooling. I excluded those individuals whose first period is 14 years, or 26 years old or older. Following Imai and Keane (2004), I assume that the earliest age when decisions start is 20. So, the first age ranges from 20 to 25 in the constructed data. See B.2 in Appendix B for details.

he has decided to work for a paid job, he can choose full or part-time. For self-employment, he can only choose to work or not to work.<sup>12</sup> Specifically, a choice element of labor is written by

$$l_t = (l_t^s, l_t^w) \in \{Zero, SE\}$$
  
  $\times \{Zero, Part\text{-}time\ PE, Full\text{-}time\ PE\}$ 

and as a result of labor choice he obtains income from working.<sup>13</sup>, <sup>14</sup> Since I assume that full-time work is equivalent to working for 2000 hours and part-time work is to 1000 hours, I occasionally use the alternative notation:

$$l_t = (l_t^s, l_t^w) \in \{0, 2000\} \times \{0, 1000, 2000\}.$$

He also determines how much to save for next period out of the sum of the current income and the accumulated asset (denoted by  $\Delta a_{t+1} = a_{t+1} - a_t$ , where  $a_t$  is the amount of financial net worth in age t). The residual is consumption,  $c_t$ . I assume that he chooses an absolute change in financial net worth for next period from a discretized set  $\{\underline{\Delta a}, ..., \overline{\Delta a}\}$ , that is

$$\Delta a_{t+1} \in \{\underline{\Delta a}, ..., \overline{\Delta a}\}.$$

He obtains per-period utility from consumption as well as gets disutility from working:  $u_t = u(c_t, l_t^s, l_t^w; \epsilon_t^{ls}, \epsilon_t^{lw})$ . The objective of the individual is to maximize the expected present discounted value of utility over a finite horizon from the first decision age to the last (see next subsection).

Beside age index  $age_t$  itself, there are five moving state variables in each decision age t: (i) whether he has ever experienced self-employment until period t-1,  $h_t^s$ , (ii) how many years he has been a self-employer in a row,  $\tau_t^s$ , (iii) accumulated labor experience in paid-employment,  $h_t^w$ , (iv) labor experience in paid-employment in the previous period,  $l_{t-1}^w$ , and (v) financial net worth,  $a_t$ . The initial values for labor experience,  $(h_1^s, h_1^w)$  and for net worth,  $a_1$ , are exogenously given.

Any individual before observing shocks and starting decisions is, therefore, characterized by

$$\bar{s}_1 = ((h_1^s, \tau_1^s, h_1^w, l_0^w, a_1), (educ, type, age)),$$

where  $h_1^s = 0$ ,  $\tau_1^s = 0$ ,  $h_1^w = 0$ ,  $l_0^w = \phi$  (null), and  $a_1$  may be positive or negative (or zero). Regarding experience in self-employment, I employ the following transitions:

$$h_{t+1}^s = \begin{cases} 1 \text{ if } \exists t' \le t \text{ such that } l_{t'}^s = SE \\ 0 \text{ otherwise} \end{cases}$$

for any  $t \in \{1, ..., T\}$ , and

$$\tau_{t+1}^s = \begin{cases} \tau_t^s + 1 \text{ if } l_t^s = SE \\ 0 \text{ otherwise} \end{cases}$$

<sup>&</sup>lt;sup>12</sup>The reason why I do not distinguish between full- and part-time self-employment is that the number of individuals choosing part-time self-employment in each age is small. See Subsubsection B.4.3 in Appendix B for details. Notice here that by definition I am excluding such issues as "overwork" and "flexibility" on hours worked in self-employment.

<sup>&</sup>lt;sup>13</sup>Note that he makes a decision, observing a vector of earnings "offer." In other words, the value for all income alternatives have already "realized" when he is making a decision.

<sup>&</sup>lt;sup>14</sup>Campbell and DeNardi (2007) find that a large proportion of nascent entrepreneurs are employed in the wage and salary sector at the time they are starting their own business.

<sup>&</sup>lt;sup>15</sup>The reason his work status in the previous period,  $(\tau_{t-1}^s, l_{t-1}^w)$  is introduced is that the persistence effect in the employment modes is captured to explain better the patterns in the empirical data.

for any  $t \in \{1, ..., T\}$ . Regarding labor experience accumulation in paid-employment, I employ the following transitions:

$$h_{t+1}^w = h_t^w + 0.5 \cdot I(l_t^w = Part\text{-}time\ PE) + I(l_t^w = Full\text{-}time\ PE)$$

for any  $t \geq 1$ , where  $I(\cdot)$  is an indicator function that assigns one if the term inside the parenthesis is true and zero otherwise. Notice that two state variables  $l_{t-1}^w$  and  $a_t$  are also decision variables.

#### 3.2 The Individual's Problem and Constraints

In each decision period t, the individual is assumed to maximize the present discounted value of lifetime utility from the current period to the terminal age. The subjective discount factor is denoted by  $\beta \in (0,1)$ . Then, in each period t, he solves

$$\max_{\{l_{t'}, \ \Delta a_{t'+1}\}_{t'=t}^T} E \left[ \sum_{t'=(age-19)}^{(\overline{age}-19)} \beta^{t'-t} u_t \right]$$

where  $u_t = u(c_t, l_t^s, l_t^w; \epsilon_t^{ls}, \epsilon_t^{lw})$ , subject to the budget and borrowing constraints, which are specified in the rest of this subsection.

First, letting  $y_t$  denote the earned income, the budget constraint is given by

$$c_t + a_{t+1} = y_t + (1 - \delta)k_t + (1 + r)(a_t - k_t)$$

where  $y_t = y_t^w + y_t^s$  and  $k_t$  is the amount of business capital invested in the self-employed business, which is positive if and only if he worked as a self-employer (see next subsection),  $\delta \in (0,1)$  is the rate of capital depreciation of business capital, and r > 0 is the rate of return from savings, which is assumed to be the same as the unit cost of business capital. The opportunity cost for  $k_t$  arises because he could have saved  $k_t$  in a bank. Here I assume, as in the standard neoclassical growth model, that business capital,  $k_t$ , can be completely divested (cashed out) after production and that there is no additional adjustment cost other than depreciation. In addition, consumption in any period t cannot be below some level, which is called consumption floor and is denoted by  $c_{\min}$  (implicitly assumed is the existence of such (unmodeled) public welfare systems as unemployment insurance and bankruptcy protection), so that

$$c_t \geq c_{\min}$$
.

Second, he (as a consumer) faces the borrowing constraint due to (unmodeled) imperfections in the financial market. That is, in each period t, (unmodeled) creditors impose a lower bound that prevents the individual's net financial asset  $a_{t+1}$  from falling below a lower

<sup>&</sup>lt;sup>16</sup>Notice here that the interest rate is not dependent on t. If one wants to consider the time dependency of the interest rate in a consistent manner to a dynamic model, she needs to introduce the individual's forecasting rule in the model. In this paper, I just assume that the individual in the model regards the interest rate as some constant during his life. Hence, I do not consider macro schocks from the aggregate economy, either. For an analysis of the macro effects on self-employment, see Rissman (2003, 2006).

<sup>&</sup>lt;sup>17</sup>Such papers as Quadrini (2000), Cagetti and De Nardi (2006), Buera (2008a,b), Mondragon-Velez (2006) and Schjerning (2006) that study the role of borrowing constraints in entrepreneurship also employ the same assumption and thus business capital does not constitute a state variable in their models.

bound,  $\underline{a}_t$ :18,19

$$a_{t+1} \geq \underline{a}_{t+1}$$
.

Because of this borrowing constraint the individual cannot always perfectly smooth consumption.

### 3.3 Earnings Opportunities

Differences between self-employment and paid-employment are expressed as those in functional forms of earnings opportunities: I assume that functional forms of someone's earnings opportunities depend on whether he works independently ("becomes his own boss") or is employed by someone else.<sup>20</sup> I begin with the case of paid-employment because it uses a familiar formulation from the existing literature on human capital.

#### 3.3.1 Income from Paid-Employment

Hourly Market Wages Following the literature on human capital (e.g. Mincer (1958) and Ben-Porath (1967)), I assume that the market hourly wage for effective labor is the product of the rental price of human capital ( $R^f$  for full-time paid-employment and  $R^p$  for part-time paid-employment) and the level of (sector-specific) human capital for paid-employment,  $\Psi_t^w$ . I assume that  $\Psi_t^w$  is the product of the deterministic part of the human capital ( $\overline{\Psi}_t^w$ ) and the idiosyncratic productivity shock ( $\exp(\epsilon_t^{yw})$ ):

$$w_t^j = R^j \cdot \Psi_t^w$$
  
=  $R^j \overline{\Psi}_t^w \exp(\epsilon_t^{yw}) \ (\equiv w^j (\overline{\Psi}_t^w, \epsilon_t^{yw}))$ 

which leads to the following Mincerian wage equation:

$$\ln w_t^j = \ln R^j + \ln \overline{\Psi}_t^w + \epsilon_t^{yw},$$

for j = f, p.

**Annual Income** Annual income from paid-employment,  $y_t^w$ , is then the hourly market wage multiplied by hours worked. Specifically, it is given by

$$y_t^w = \begin{cases} w_t^f \cdot 2000 \text{ if } l_t^w \text{ is "full-time"} \\ w_t^p \cdot 1000 \text{ if } l_t^s \text{ is "part-time"} \\ 0 \text{ if } l_t^s \text{ is "zero"}, \end{cases}$$

where the variation in income reflects only the variation in hourly market wages. $^{21}$ 

<sup>&</sup>lt;sup>18</sup>The lower bound,  $\underline{a}_t$ , can be negative. This is motivated by the empirical observations: in most of ages that are covered by the data for estimation, the lower 10% have negative net worth.

<sup>&</sup>lt;sup>19</sup>I do not allow the individual to default. See Pavan (2008) and Herranz, Krasa and Villamil (2007) for estimable dynamic models that allow for default.

<sup>&</sup>lt;sup>20</sup>In the present paper, I assume away one important difference that a self-employed worker has to pay fringe benefits out of his earnings while a wage worker receives these as part of earnings, but they are not added into the earnings data of the wage worker. I also do not consider business transfers. See Holmes and Schmitz (1990,1995) for this issue.

<sup>&</sup>lt;sup>21</sup>This is also the way of constructing data on income from paid-employment. See Appendix B.4.4.

#### 3.3.2 Income from Self-Employment

**Entrepreneurial Production Function** I assume that production contribution by the individual as a self-employer separable from that by other individuals who work with him (if any). The individual's production ability when he works as a self-employer is assumed to be captured by following the Harrod-Neutral Cobb-Douglas *entrepreneurial production function*:

$$y_t^s = f([\overline{\Psi}_t^s l_t^s], k_t, \epsilon_t^{ys}; \alpha, \rho)$$
$$= [\overline{\Psi}_t^s l_t^s]^{1-\alpha} k_t^{\alpha} \exp(\epsilon_t^{ys}),$$

which leads to

$$\ln y_t^s = (1 - \alpha) \ln[\overline{\Psi}_t^s l_t^s] + \alpha \ln k_t + \epsilon_t^{ys},$$

where  $\overline{\Psi}_t^s$  is the (deterministic) value of human capital for self-employment,  $l_t^s$  is hours worked for self-employment,  $k_t$  is business capital, and  $\alpha \in (0,1)$  is a constant. Following the human capital literature on heterogenous skills (e.g. Willis and Rosen (1979), Heckman and Sedlacek (1985), and Keane and Wolpin (1997)) I distinguish the (deterministic) value of human capital for self-employment ( $\overline{\Psi}_t^s$ ) and that for paid-employment ( $\overline{\Psi}_t^w$ ). The difference is, however, that, I assume that there does not exist a price of human capital for self-employment (such  $R^f$  and  $R^p$  as in the case of paid-employment) because the lack of the market for it. Notice also that different from paid employment, the idiosyncratic productivity shock ( $\exp(\epsilon_t^{ys})$ ) is not multiplied by deterministic part of the human capital ( $\overline{\Psi}_t^s$ ) only but by the component including the scale of business,  $k_t$ .

Now, I assume, following Evans and Jovanovic (1989), Buera (2008a,b), Mondragon-Velez (2006) and many others in the literature on entrepreneurship, that the individual (as a self-employer) faces the following borrowing constraint:

$$0 \le k_t \le a_t - \underline{a}_t.$$

Notice here that if the borrowing constraint is binding, then accumulated net worth  $a_t$  determines the level of business capital (together with the lower bound for financial net worth,  $\underline{a}_t$ ). Or, anticipating this, he may be able to overcome the borrowing constraint by accumulating enough amount of wealth beforehand. This is the mechanism of how wealth accumulation may affect entrepreneurial choice through the presence of the borrowing constraint. Even if an individual anticipates that the borrowing constraint is not likely to bind, wealth accumulation may matter to entrepreneurial choice though precautionary saving motive: if income from self-employment fluctuates more than from paid-employment, then it gives potential and current self-employers.

$$y_t^s = f([\overline{\Psi}_t l_t^s], k_t; \omega, \alpha)$$
$$= \omega \cdot [\overline{\Psi}_t l_t^s]^{1-\alpha} k_t^{\alpha}$$

where  $\omega$  is assumed to be related to entrepreneurial/managerial talent (see e.g. Lucas (1978)). Notice that in my model, "entrepreneurial/managerial talent" is incorporated in  $\overline{\Psi}_t^s$ .

 $<sup>^{22}</sup>$ In the present paper, when estimating the model, I capture heterogeneity in  $\alpha$  by considering differences in the level of schooling. This is because, as Mondragon-Velez (2007) points out in other dataset, there are significant differences in industries of self-employers by the level of schooling. See Subsection A.4 in Appendix A for details.

<sup>&</sup>lt;sup>23</sup>An alternative modeling for the entrepreneurial production function would be to assume homegenous human capital  $(\overline{\Psi}_t \equiv \overline{\Psi}_t^s \equiv \overline{\Psi}_t^w)$  and thus

**Annual Income** Since I have judged that information on business capital  $k_t$  is not reliable enough<sup>24</sup> due to the small number of observations in the NLSY79 and the ambiguity of the definition of "business capital" in early processes of business formation, I follow Evans and Jovanovic (1989) to substitute the chosen  $k_t$  into the entrepreneurial production function in the following way. When he has decided works as a self-employer with  $l_t^s = 2000$  hours worked, he chooses his business capital  $k_t$  by solving

$$\max_{k_t \in [0, a_t - \underline{a}_t]} \exp(\epsilon_t^{ys}) [\overline{\Psi}_t^s l_t^s]^{1 - \alpha} k_t^{\alpha} - (1 + r) k_t,$$

subject to the borrowing constraint above, so that the chosen amount of business capital is

$$k_t^{\$} = k_t^{\$}(2000, \epsilon_t^{ys}, a_t) = \min\{k_t^{*}(2000; \epsilon_t^{ys}), a_t - \underline{a}_t\}.$$

where

$$k_t^*(2000, \epsilon_t^{ys}) = \left(\frac{\alpha \cdot \exp(\epsilon_t^{ys})}{1+r}\right)^{\frac{1}{1-\alpha}} \left[\overline{\Psi}_t^s \cdot 2000\right]$$

is derived from the first-order condition for the optimal value without the borrowing constraints.<sup>25</sup>

Annual income from self-employment,  $y_t^s$ , is thus given by

$$y_t^s = \begin{cases} \exp(\epsilon_t^{ys}) [\overline{\Psi}_t^s \cdot 2000]^{1-\alpha} [k_t^{\$}(2000, \epsilon_t^{ys}, a_t)]^{\alpha} & \text{if } l_t^s \text{ is "work"} \\ \\ 0 & \text{if } l_t^s \text{ is "zero"}, \end{cases}$$

where, because of the borrowing constraint, the realization is affected by the current net worth,  $a_t$ .

# 4 Solving the Model

Although its structure is not conceptually complicated, the life-cycle model described above does not seem to permit an analytical solution for the optimal decision rule that yields the path,  $\{(l_t)^*, (\Delta a_{t+1})^*\}_{t=1}^T$ , even if parametric forms for the functions are given. In this section, I explain how my life-cycle model becomes computationally solvable.

#### 4.1 Descretization

Notice that the structural model is presented as a discrete choice problem.<sup>26</sup> In the current formulation, the number of grids for absolute change in net worth for next period is 12, <sup>27</sup> so that the choice set contains 72 (=  $6 \times 12$ ) elements.

$$\{\underline{\Delta a},...,\overline{\Delta a}\}=\{\pm\{20000,10000,7500,5000,1500\},+500,+40000\}.$$

<sup>&</sup>lt;sup>24</sup>Evans and Jovanovic (1989) reached the same judgement, stating that "[s]ince our data do not contain precise enough information on how much is invested, ..." (p.814)

<sup>&</sup>lt;sup>25</sup>This operation is justified because I assume that  $k_t$  does not appear in a transition equation or it is not a state variable. In Schündeln (2006), who considers adjustment costs of capital but assumes away human capital accumulation, does the same operation for labor input.

<sup>&</sup>lt;sup>26</sup>Another formulation would allow savings choice to be *continuous*. See, e.g, Cagetti (2003), Imai and Keane (2004), and van der Klaauw and Wolpin (2006), who numerically solve the Euler equation for the optimal consumption/savings path. Obviously, this formulaion would be more demading in computation.

<sup>&</sup>lt;sup>27</sup>The set of the actual grids that are used in the current formulation is

Variables that characterize the individual's permanent heterogeneity (educ, and type) are also discretized. First, education level takes one of two values. That is, educ = 0 if the individual is a high-school dropout (his year of schooling is less than 12) or a graduate (his year of schooling is 12), educ = 1 if he obtained some college degree (his year of schooling is equal to or greater than 13 and equal to or less than 15) or if he is a college graduate (his year of schooling is equal to or greater than 16). I also assume that type takes value 0 or 1.

### 4.2 Recursive Formulation

Notice that the problem of the individual can be recast in a recursive formulation. In addition, the dynamic problem ends in a finite horizon. Thus, the model can be solved backward, starting from the terminal decision period T. At this last age, the continuation value is exogenously given as a function of the state variable at that period. I do not normalize it to be zero because if I do so the individual consumes all the income in this last period, which may significantly affect the pattern of the optimal path.<sup>28</sup> The details are as follows.

First, let j-th element of the choice set in each period be denoted by

$$d_t^j \in \{Zero, SE\}$$

$$\times \{Zero, Part\text{-}time\ PE, Full\text{-}time\ PE\}$$

$$\times \{\underline{\Delta a}, ..., \overline{\Delta a}\}$$

and the utility associated with that choice as  $u_t^j$ . In addition, letting the state space at t be denoted by  $S_t$ , state point in period  $t, s_t \in S_t$ , is given by

$$s_t = ((h_t^s, \tau_t^s, h_t^w, l_{t-1}^w, a_t), (educ, type, age), (\epsilon_t^{ls}, \epsilon_t^{lw}, \epsilon_t^{ys}, \epsilon_t^{yw})),$$

where the generic element of the *predetermined* part of  $S_t$  is written by  $\overline{S}_t$  whose generic element is

$$\overline{s}_t = ((h_t^s, \tau_t^s, h_t^w, l_{t-1}^w, a_t), (educ, type, \underline{age})).$$

Note that the part  $(h_t^s, \tau_t^s, h_t^w, l_{t-1}^w, a_t)$  is a result of past decisions (up to t-1), and that the element  $(educ, type, \underline{age})$  is the part of the state points that is permanently fixed.<sup>29</sup> Note also that actual age  $age_t$  is implicitly included in  $\overline{s}_t$  because it is determined by t and the age in the first decision period  $(\underline{age})$ , that is,  $age_t = \underline{age} + (t-1)$ . Exogenous to the decisions but moving across t's are  $(\epsilon_t^l, \overline{\epsilon_t^y})$  and  $age_t$ .

In constructing the asset space for each period, Starting with t=1 (with 5 grids), I recursively expand grids for next period by adding all  $\Delta a \in \{\underline{\Delta a},...,\overline{\Delta a}\}$  to all the grids in the current period, starting with the initial period. For those who start working at age 20 the initial grids are set to be  $\{-4240,704,2424,6136,96496\}$ , and for others they are  $\{-19154,1840,5932,12492,296400\}$ .

 $<sup>^{28}</sup>$ In the actual implementation, I use the quasi-terminal period,  $T^*$ , which is set to be 30 for all individuals, not T, to ease computational burden. Under this simplification, model individuals live up to age 49 (for those with  $\underline{age} = 20$ ) to 54 (for those with  $\underline{age} = 25$ ). As explained in Appedix B, the highest age observed in the data  $\underline{age}$  is 39, so this simplification  $\underline{does}$  not lose information from the empirical data.

<sup>&</sup>lt;sup>29</sup>In the data,  $(h_t^s, h_t^w, l_{t-1}^s, l_{t-1}^w, a_t)$  is not always (across t's and the sample individuals) observed, and  $(educ, \underline{age})$  is observed for all of the sample individuals. Note that type is the variable to caputure unobserved hetertogeneity.

Thanks to the Bellman representation, the value function at any period t,  $V_t$ , is written in a recursive way by

$$V_t(s_t) = \max_{d_t^j} u_t^j + \beta E_t[V_{t+1}(s_{t+1})|s_t]$$
  
= \text{max}[V\_t^1(s\_t), ..., V\_t^J(s\_t)]

where  $E_t$  is the expectations operator at the beginning of period t, and

$$V_t^j(s_t) = u_t^j + \beta E_t[V_{t+1}(s_{t+1})|d_t^j = 1, s_t]$$

for j=1,2,...,J. The expectation is taken over the joint distribution of the stochastic shocks in next period,  $\tilde{\epsilon}_{t+1}^l = (\tilde{\epsilon}_{t+1}^{ls}, \tilde{\epsilon}_{t+1}^{lw})$  and  $\tilde{\epsilon}_{t+1}^y = (\tilde{\epsilon}_{t+1}^{ys}, \tilde{\epsilon}_{t+1}^{yw})$ . This alternative-specific value function assumes that future choices are optimally made for any given current decision. For t=1,...,T, let the part  $E_t[V_{t+1}(s_{t+1})|d_t^j=1,s_t]$  be denoted by  $Emax_t$ . Notice that this is a function that assigns each element of the predetermined state space and decisions (i.e,  $\overline{s}_t \in \overline{S}_t$  and  $d_t^j$ ) to some value.<sup>30</sup>

When the individual in the model (as well as the econometrician) wants to optimally choose a decision element in period t, he needs to know this function to compare  $\{V_t^j(s_t)\}$  across j. He can do so in the following way. Consider the last period T. Then, for each  $s_T \in S_T$ , he has the following system of J equations:

$$\begin{cases} V_T^1(s_T) = u_T^1 + \beta V_{T+1}(d_T^1 = 1, s_T) \\ \dots \\ V_T^J(s_T) = u_T^J + \beta V_{T+1}(d_T^J = 1, s_T), \end{cases}$$

where  $V_{T+1}(d_T^j, s_T)$ , or  $Emax_T$ , is the terminal value that he obtains by choosing  $d_t^j = 1$  when the state is  $s_T$ .<sup>31</sup> So, if this terminal value is given for all  $d_T^j$  and all  $s_T$ , it is then possible to compute  $Emax_{T-1}$  by taking expectations of  $V_T(s_T) = \max[V_T^1(s_T), ..., V_T^J(s_T)]$ , given the distribution of  $\epsilon_T$ . He can then solve for  $Emax_t$  for all t by recursively solving the simple static optimization problems of discrete choice that is a system of linear equations. Once  $Emax_t$  functions are known, the optimal path of decisions,  $\{(l_t)^*, (\Delta a_{t+1})^*\}_{t=1}^T$ , can be determined as follows: conditional on the deterministic part of the state space  $S_t$ , the probability that an individual is observed to choose option j takes the form of an integral over the region of the space of the five errors such that j is the preferred option.

As the decision period approaches the final period, however, the dimension of the predetermined state space  $\overline{S}_t$  becomes too huge for the econometrician to obtain the optimal decision path in a computationally reasonable manner (in terms of both memory allocation and running time), especially if there are many total number of decision periods as in this study.

To deal with this problem, I use an approximation method that was proposed by Keane and Wolpin (1994) and applied by the same researchers (1997, 2001) and many others, in which the  $Emax_t$  functions are expressed polynomials of the state variables.<sup>32</sup> Specifically, starting with T, for each type, I randomly select many points,  $\{h_T^s, \tau_T^s, h_T^w, l_{T-1}^w, a_T, educ,$ 

<sup>&</sup>lt;sup>30</sup>In determining the decision in period t, he observes initial shocks  $\epsilon_t$ , and he uses this information. However, because of the independence between  $\epsilon_t$  and  $\epsilon_{t+1}$ , this information does not affect  $Emax_t$ .

<sup>&</sup>lt;sup>31</sup>Note that there is no need to take expectations over the next period's shocks in the last period.

 $<sup>^{32}</sup>$ I use the second degree polynomial, including all interactions between the state variables. The variables  $\epsilon_t^{ls}$ ,  $\epsilon_t^{lw}$ ,  $\epsilon_t^{ys}$  and  $\epsilon_t^{yw}$ do not have to be incorporated in Emax calculation because of their serial uncorrelation.

 $\underline{age}$ ,  $^{33}$  and for each of these points, I calculate  $V_T(s_T)$ , given  $Emax_T$ .  $^{34}$  I obtain estimates for the polynomial coefficients by regressing  $\{V_T(s_T)\}$  on the polynomial, and then interpolate the  $Emax_{T-1}$  polynomial by using these estimated coefficients. This interpolated  $Emax_{T-1}$  is used to calculate the one in period T-1. After period T-1 and on, for each  $t \in \{T-1,..,2\}$ , I use Monte Carlo integration over the distribution of the disturbance in period t ( $\tilde{\epsilon}_t^l = (\tilde{\epsilon}_t^{ls}, \tilde{\epsilon}_t^{lw})$ ) and  $\tilde{\epsilon}_t^y = (\tilde{\epsilon}_t^{ys}, \tilde{\epsilon}_t^{yw})$ ) for a randomly selected subset of  $S_t$  to obtain the approximated expected value of the maximum of the alternative-specific value functions at those state points,  $Emax_{t-1}$ . This procedure continues to decision period 2, where the interpolated  $Emax_1$  is calculated.

To computationally implement the above procedure, I need to specify parametric functional and model distributional assumptions. Appendix A shows the exact functional forms. I now turn attention to the data that is used for estimation.

## 5 Data

The data for estimation of the life cycle model is constructed from the 1979-2000 waves of the 1979 youth cohort of the National Longitudinal Survey of Youth (NLSY79). Conducted every year for 1979 to 1993 and once two years for 1994-2004, the NLSY79 contains a nationally representative sample of 12,686 individuals (with 6,403 of them being males) who were 14-21 years old as of January 1, 1979. It contains a core random sample and oversamples of blacks, Hispanics, economically disadvantaged non-black/non-Hispanics, and members of the military. As of the 2000 interview round, all the individuals became 35-43 years old. In this study, I use the white male part in the core random sample.<sup>36</sup> This reduces the initial sample size 12,686 to 2,439. The further restriction the dimension of individuals is explained in the following subsection.<sup>37</sup>

#### 5.1 Data Construction

I first exclude individuals who have military experience (268 individuals) and then those who are judged to be professionals or farmers (102 individuals). Both professionals and farmers characterized by high rates of self-employment. Why I exclude these people is that the workings of labor markets for them may be quite different from those for nonprofessional, nonfarmers, and hence the decision to become a farm or professional self-employer may depend on different factors than the decision to become a nonfarm, nonprofessional self-employer. I then follow each white man of these 2,068 individuals after the (calender) year when he is considered to have finished schooling, no matter how long it takes for him to finish it. I drop, however, those who are judged to have started working too late (i.e. 26 years

<sup>&</sup>lt;sup>33</sup>Notice that  $age_t$  takes only one particular value given  $\underline{age}$  and t, so it cannot be a component of the randomly chosen subset.

<sup>&</sup>lt;sup>34</sup>This function has a parametric form and its parameters are the target of estimation. The actual parametric form is given in Appendix A.7.

 $<sup>^{35}</sup>$ I use 1500 state points and 49 (22 if t=2) variables for the approximations of the  $Emax_t$  functions. The number of random draws for Monte Carlo integration is 30. The goodness of fit is assessed by the adjusted coefficients of determination: with the estimated parameter values they range from 99.84 to 99.98.

<sup>&</sup>lt;sup>36</sup>Future research would include studying issues of self-employment among non-whites (racial discrimination) and women (fertility and child rearing).

<sup>&</sup>lt;sup>37</sup>Appedix B describes the details on the sample inclusion criteria and on how variables in my data are created.

old or older) or too early (i.e. 14 years old). The total number of these people is 82. Also excluded are those who are judged to have temporally left for adult schooling in the midst of their work career (24 individuals). Some individuals have to be excluded if it is difficult to determine the first decision period, or if no survey years are covered when working (47 individuals). All money values in the paper are expressed in 2000 dollars. My final sample consists of 1,916 white males with a total of 32,166 person-year observations (which is an unbalanced panel).

Let the constructed data be denoted by  $X = \{X_i\}_{i=1}^N$ , where N is the number of individuals in the data and  $X_i$  is data for individual i. Using the notation in the dynamic model presented in Section 2, I can write the actual form of  $X_i$  as

$$X_i = \{(l_{i,t}^s, l_{i,t}^w), (y_{i,t}^s, w_{i,t}), a_{i,t+1}, age_{i,t}\}_{t=1}^{\widehat{T}_i}, a_{i1}, educ_i\},\$$

where  $\hat{T}_i$  is the last period when individual i's information is available (note the difference between  $\hat{T}_i$  and  $T_i$ ),  $age_{i,1}$  is actually equal to  $\underline{age_i}$  (so that both variables will be used interchangeably), and N is the number of individuals in the sample. Note also that consumption can be calculated up to period  $\hat{T}_i - 1$ . So, essentially, I do not use data observations in period  $\hat{T}_i$ . For the schooling variable  $educ_i$ , I consider only two categories, "High-school dropouts or graduates (H)" (called non-college educated hereafter), and "Some college degree or higher (C)" (called college educated hereafter), mainly because of the small numbers of the self-employment experienced. While  $educ_i$  and  $age_i$  are observed for any i, the amount of initial asset  $a_{i1}$  is not necessarily observable for all i's. The hourly wage,  $w_{i,t}$ , is observed constructed only when individual i worked as a paid worker. Similarly,  $y_{i,t}^s$  is observed only when individual i worked as a self-employer in period t.

The NLSY79 has detailed information on the self-employed themselves, but very limited information on the businesses they run.<sup>40</sup> This limited information on the financial side of self-employment, however, would not be too restrictive because modeling that part is kept to minimum in this study. We also no information on how many workers each self-employer employs in his firm. Remember, however, that I have assumed that production contribution by the self-employed is separable from that by his employees, so this data limitation is not restrictive to this study, either.

 $<sup>^{38}</sup>$ Regarding the risk-free interest rate (r), I first computed for each year from 1979 to 2000 the difference between the nominal annual rate of federal funds and the next year's realized inflation rate (as a substitute for the expected inflation rate). I then impute the yearly average, 3.5%, to r (r = 0.035). I also use a constant rate of business capital depreciation ( $\delta$ , and it is taken as a data input: as in Cagetti and De Nardi (2006), it is set to be 6.0% ( $\delta = 0.060$ ).

<sup>&</sup>lt;sup>39</sup>I carefully constructed "income from self-employment" in my data to capture the "returns to capital" as precisely as possible. In particular, I compared Income Information from the "Income Section" with from the "Employer Supplement Section" in the NLSY79. The downside of using the "Income Section" is that after 1995 income information is obtained once in every two years, which reduced the number of observed income. However, by comparing labor earnings calculated from the "Employer Supplement Section" with total income (the sum of wage/salary income and business income) calculated from the "Income Section", I found, for income from self-employment, the former appears to have downward bias especially for higher percentiles, while for income from paid-employment, both are surprisingly similar. So, I use the "Income Section" to calculate income from self-employment while the "Employer Supplement Section" is used to calculate income from paid-employment. See Appendix B for the details.

<sup>&</sup>lt;sup>40</sup>Currently, at the US Census Bureau, effort are undertaken to integrate business and household data (the Longitudinal Employer-Household Dynamics (LEHD) program) and employer-employee data (the Integrated Lonitudinal Business Database (ILBD)). See Davis, Haltiwanger, Jarmin, Krizan, Miranda, Nucci, and Sandusky (2007) for details.

### 5.2 Descriptive Statistics

In this subsection, I explain key descriptive statistics of the constructed sample X.

# 5.2.1 Initial Conditions ( $\underline{age_i}$ , $educ_i$ and $a_{i1}$ ) and Information on Individual-Period Observations in the Pooled Data

Panel 1 in Table 3 shows the initial conditions of the sample individuals. First, remember that the earliest age for decisions is set to 20.<sup>41</sup> About 60 percent of the individuals start decisions at age 20, and 94 percent of them start decisions until age 23. Next, as for schooling attainment, 63 percent of the individuals are non-college educated and the remaining individuals are college educated. In the joint distribution of initial age and schooling (not shown), nearly 90 percent of the individuals in the non-college educated group start decisions at age 20, while about 50 percent of the college educated individuals start decisions at age 22 or 23. With respect to net worth that each individual owns at his first age of decisions, the considerable difference between the mean and the median suggest the skewness of the wealth distribution even in early 20s. As is expected, the joint distribution of initial net worth and schooling (not shown), both the mean (13,062 versus 9,505 dollars) and the median (5,495 versus 1840 dollars) are higher for the college educated.

Panel 2 in Table 3 displays information on individual-period observations in the pooled data. The average (and the median) age is 29. As is mentioned in Introduction, of all the observations on labor supply decisions, 7 percent are provided as self-employed work while 80 percent are as either full- or part-time paid-employed work. The average accumulated years of experience as a wage worker is 6.3 (excluding years as a self-employer). The mean income from self-employment (51,351 dollars) is considerably higher (56 percent higher) than that from full-time paid-employment (32,932 dollars). The median difference is much smaller: the median income from self-employment is 29 percent higher than that from full-time paid-employment (36,900 versus 28,560 dollars). The mean income from part-time paid employment is 57 percent lower than that from full-time paid-employment. Lastly, the average net worth is 57,312 dollars while the median is 20,008 dollars.

# 5.2.2 Labor Supply Decisions: Age Profiles $(\{l_{i,t}^s, l_{i,t}^w\})$ , Transitions, and Entry into and Exit from Self-Employment

Table 4 and Figure 1 show the marginal distribution of labor supply decisions by age. At age 20, only 2.4 percent of the white men are self-employed. Then, the rate increases rapidly until age 25 (7.3 percent). After that, it remains stable with a slight increase (9.5 percent at age 38). The rates of full-time paid employment are highest and stable over all the ages. Starting with 58.9 percent, the percentage grows to 77.9 percent at age 27. After that age, the number declines slightly (65.7 percent at age 31), and then it grows again. Corresponding to the slight decline in full-time paid employment, the rate of part-time paid-employment starts go up at age 27 after the decline since age 20, reaching 14.3 percent at age 31. Lastly, the percentage of the non-employed decreases rapidly in their early 20s: 22.8 percent at age 20 to 5.8 percent at age 27. Then, after age 28 the rates are stable with a slight increase (between 7.3 and 9.7).

Some key differences of self-employment by schooling have been already presented in Tables 1 and 2. In what follows, we look at details of life-cycle aspects of labor supply

<sup>&</sup>lt;sup>41</sup>Note also that the ealiest age when information on asset is available is age 20.

decisions. Table 5 shows the percentages of the individuals for the numbers of entries into self-employment. First, we find self-employment experience is not rare: 28.3 percent of individuals (543 out of 1916 individuals) have at least one year of self-employment experience. Second, we do not observe too many trials by the same young individual, however: 94.1 percent of them enters only once or twice in the data periods. As was already mentioned, the non-college educated is more likely to have self-employment experience than the college educated do. Figure 2 shows an important difference in the timings of first entries into by schooling. Although the means and the medians of the first entries for both types of schooling are quite similar (8.2 (mean) and 7 (median) for the non-college educated, and 8.6 (mean) and 8 (median) for the college educated), the two distributions do not look similar: the highest percentage is attained at decision periods 5-8 for the college educated, while it is attained at decision periods 1-4 for the non-college educated.

The left panel of Table 6 shows one-period transition rates of labor supply decisions for both schooling levels. The first number in each cell is the percentage of transitions from origin to destination (row %) while the second is the percentage in a particular destination who started from each origin (column %). The table shows persistence in self-employment and in full-time paid-employment: 75.4 (73.6) percent of the non-college (college) educated self-employers in one year do self-employment the next year, and 85.4 (89.5) percent of the non-college (college) education who worked full-time as a wage worker in one year work as a full-time wage worker the next year. The age pattern of the self-employment and full-time paid employment is also worth attention. The left panel of Table 7 implies that self-employment in twenties is likely to end earlier than that in thirties: the transition rate of self-employment in twenties is 69 percent while that in thirties is 80 percent.

# 5.2.3 Age Profiles of Income $(\{y_{i,t}^s, y_{i,t}^w\})$ and of Net Worth $(\{a_{i,t}\})$

As is already seen in Table 2, the self-employed earn more, on average, than the paid-employed do, and across the two groups of education levels, income from self-employment is higher than income from paid-employment (both for the mean and for the median). Table 8 and Figure 3 display age-specific mean real incomes from self-employment, from full-time and from part-time paid-employment. Real incomes rise with age in all the three modes of employment. The percentage difference between income and income from full-time paid-employment at early twenties is about 40 to 50 percent. It grows with age: at late thirties it becomes about 60 to 70 percent.

Table 9 and Figure 4 show the age profile of the mean and median net assets of all individuals. As is seen, the mean grows faster then the median does, and as a result, he mean net worth at late thirties is about 14 times larger than that at early twenties. The wealth distribution is thus more skewed in later ages.

 $<sup>^{42}</sup>$ Remember that my data contains only nonprofessional white males in nonagricultural sectors. Excluded are 40 lawers/accountants and 23 doctors. This seems the reason of a low self-employment rate among category "College or higher" because college degree is necessary to be a professional of these kinds. If these 63 individuals are added to the self-employment cell, then the rate of self-employment rate for the college educated will be 31.4% (=(182+63)/(717+63)).

<sup>&</sup>lt;sup>43</sup>I define year of *entry* into self-employment t by  $l_{i,t}^s = SE$  and  $l_{i,t-1}^s = Zero$ , and define year of *exit* from self-employment t by  $l_{i,t}^s = SE$  and  $l_{i,t+1}^s = Zero$ . The duration of a SE spell is defined by the difference between the exit year and the entry year.

## 6 Estimation Method

Using data X that is explained in the previous section, I estimate the parameters of the life-cycle model of employment mode decisions and wealth accumulation. Now, given the approximated values for  $Emax_t$ , it is possible to simulate individual behavior from the first decision period (one year after he finished schooling) to age 65, with an arbitrary pair of model parameters. I simulate individual choices (choice on labor and asset) and income opportunities (including ones not chosen by the individual). The level of education and the initial amounts of net worth are taken as exogenous. At the initial decision period, any individual has no experience both for self-employment and for paid-employment.

Conditional on the deterministic part of the state space  $\overline{S}_t$ , the solution of the dynamic programming problem gives the conditional probability that an individual chooses option d, as the product of the type probabilities and a five-dimensional integral over the vector of shocks so that choice d is indeed optimal. If all variables in the state space were observed, then the conditional likelihood could be constructed as the product, over time and individuals, of these probabilities.

However, a serious problem is that endogenous state variables in  $S_t$  are not always observed. In particular, as was explained in Section 3, the NLSY79 started collecting information on asset in 1985, and since 1994 it has been collecting the asset information biannually.<sup>44</sup> Calculating the conditional choice probabilities would require one to integrate out all possible choices over the distribution of the unobserved elements. This would, however, be comutationally burdensome. I therefore adopt the method of simulated maximum likelihood developed by Keane and Wolpin (2001).<sup>45</sup> Notably, this method allows one to avoid computing the conditional probabilities, and only unconditional probabilities are used in estimation. The idea is that all observed outcomes are measured with error and model parameters are so chosen that the "distance" between simulated ("true") and observed outcomes is minimized.<sup>46</sup>,<sup>47</sup>

Specifically, I first fix a trial vector of parameters  $\theta \in \Theta$  and type = 1, ..., 4. In each sim-th simulation (sim = 1, ..., M), a period-by-period random shock  $\epsilon_t^{sim}$  is generated for each decision period t. As a solution of the dynamic choice problem, starting with the initial level of asset  $\widetilde{a}_1^{sim}$  (see below), for each permanent state (except type) ( $educ, \underline{age}$ ), I generate outcome histories of (i) choice realizations  $\{(\widetilde{l^s}_{e,t}^{sim}, \widetilde{l^w}_{e,t}^{sim}), \widetilde{\Delta a}_{e,t+1}^{sim}\}_{t=1}^T$ , and (ii) the resulting realizations of income ( $\widetilde{y^s}_{e,t}^{sim}, \widetilde{y^w}_{e,t}^{sim}$ ), and asset realizations for the next period  $\widetilde{a}_{e,t+1}^{sim}$ .

<sup>&</sup>lt;sup>44</sup>In addition, other endogenous variables (labor choice and income) are sometimes missing.

<sup>&</sup>lt;sup>45</sup>For technical issues of this method, see Keane and Sauer (2007). In particular, they argue that the method is not only computationally practical but has good small sample properties.

<sup>&</sup>lt;sup>46</sup>A byproduct of this method is that one does not have to discretize all continuous outcome variables. In this study, I do not have to discretize values for income. This is because in the presense of (normally distributed) measurement error any observed outcome history is able to be generated by any simulated outcome history with a nonzero probability.

<sup>&</sup>lt;sup>47</sup>In constructing the log liklihood function, Rendon (2006) focuses only on the path of state variables afer the year 1985 (when collection on asset information started). In particular, his log likelihood function is constructed conditional on the observation in the year 1985. After obtaining the behavioral parameters, Rendon (2006) goes on to recover the initial asset distribution by using the data from the initial decision period to the year 1985. The way he does so is to update the uniform prior on initial assets by conditional on subsequent behavior.

<sup>&</sup>lt;sup>48</sup>Notice here that the model components that have no counterpart in the actual data, realized income opportunities for the current period  $\{\widetilde{f}_{e,t}^m, \widetilde{w}_{e,t}^m\}_{t=1}^T$  and the level of human capital in the next period  $\widetilde{\Psi}_{e,t+1}^m$ , are also generated by simulation.

denote the sim-th simulated data (outcome history) for individual i in case his type is type by

$$\widetilde{X}_{i,type}^{sim} = (\{(\widetilde{l^s}_{i,type,t}^{sim}, \, \widetilde{l^w}_{type,t}^{sim}), \, (\widetilde{y^s}_{i,type,t}^{sim}, \, \widetilde{y^w}_{i,type,t}^{sim}), \, \widetilde{a}_{i,type,t+1}^{sim}, \, \widetilde{k}_{i,type,t}^{sim}, \, age_{i,type,t}^{sim}\}_{t=1}^T, \, \widetilde{a}_{i,1}^{sim}, educ_i),$$

where  $age_{i,type,t}^{sim}$  is actually independent of sim or tupe (determined by  $\underline{age}$  and t). I assume that  $educ_i$  and  $age_i$  (and hence  $age_{i,t}$ ) are observed without error for any individual i.

Now, let the probability of the observed history of individual i conditional on the simulated history be  $\Pr(X_i|\widetilde{X}_{i,type}^{sim})^{.49}$  The novel feature of the estimation method used in the present paper is that the calculation of  $\Pr(X_i|\widetilde{X}_{i,type}^{sim})$  does not depend on the state variables at any decision period t. This property enables me to construct the (unconditional) likelihood from the distributions of the measurement and classification errors (and the assumption that each error is independently distributed over individuals and time).

Specifically, I first obtain, by simulating M outcome histories, the unbiased simulator of the probability of  $X_i$ 

$$\widehat{\Pr}(X_i|\theta) = \frac{1}{2M} \sum_{type=1}^{2} \sum_{sim=1}^{M} \Pr(X_i|\widetilde{X}_{i,type}^{sim}) \frac{\Pr(type)}{M},$$

where Pr(type)/M is interpreted as the proportion of individuals with type in all the simulated histories. The log likelihood is then given by

$$\log \mathcal{L}(\theta | \{X_i\}_{i=1}^N) = \sum_{i=1}^N \log(\widehat{\Pr}(X_i | \theta))$$

and the estimate for  $\theta$  is so chosen that it maximizes the log likelihood.<sup>50</sup> Appendix C offers the actual functional form of  $\log \mathcal{L}(\theta|\{X_i\}_{i=1}^N)$ . In the current implementation, I choose M=5N=9580. Standard errors are calculated using the outer product of numerical first derivatives.

## 7 Estimation Results

In this section, I discuss the fit of the estimated model to the key empirical moments as well as the interpretation of the estimated parameters.

#### 7.1 Model Fit

To evaluate the fit of the estimated model, I artificially generated 9580 (5 times 1916) individual life-cycle paths to age 50 for each age of the first decision period (ages 20-26) using the estimated parameters.<sup>51</sup>

<sup>&</sup>lt;sup>49</sup>With the notation here, what is explained in Footnote 46 is now stated that for an arbitrary  $\widetilde{X}_e^m$ ,  $\Pr(X_i|\widetilde{X}_e^m) > 0$  for any  $X_i$  thanks to (adequately modeled) classification and measurement errors.

<sup>&</sup>lt;sup>50</sup>While some model parameters have their own structural relationships, thus are possible to be estimated independently from the other part of the model structure (e.g. the relationship between observed income and modeled income opportunities), the entire set pf model parameters enters the likelihood through the choice probabilities that are computed from the solution of the dynamic programming problem. Thus, I estimate all the parameters by maximixing the log likelihood function of probabilities of outcome histories.

<sup>&</sup>lt;sup>51</sup>In obtaining any information, simulated data for each invidual is used up to his last period that was covered.

Table 10 compares the three key statistics about entry into and exit from self-employment in the actual data with those in the simulated data (the left part is a reproduction of Table 1). All the three characteristics are underpredicted both for the non-college and the college educated. In particular, entries into self-employment take place in later ages in the simulated data than in the actual data. It, however, seems to well capture the differences by schooling on entry into and exit from self-employment.

Figures 5-8 compare simulated age profiles of labor supply decisions (self-employed, full-time paid-employed, part-time paid-employed and non-employed) with actual ones. The model does a good job in replicating the age pattern of self-employment: the rate of the selfemployed increases until age 25 and then it becomes moderately stable in the remaining ages. As for the other modes of employment, the simulated profiles resemble the actual profiles reasonably well, except few ages around early thirties. In the right panel of Table 6, the predicted one-period transition matrix is presented. The diagonal four transition rates of staying in the same mode of employment are reasonably replicated, though the one for parttime paid employment for the non-college educated and the one for non-employment for the college educated seem relatively overpredicted. The observation that the percentage from full-time paid-employment to self-employment is lower than that from non-employment is not well captured by the model. The right panel of Table 7 display the two transition matrices that correspond to age group 20-29 and to age group. The predicted numbers well capture the stronger persistence of self-employment for ages 30-39, though they show that the estimated model is less successful in explaining the transitions around part-time paid employment and non-employment.

Figures 9-14 display age profiles of annual income for each mode of employment. The model does a good job in replicating the age patterns of income as well. Figure 15 shows the age profile of the mean net worth. The model well captures the growth of the mean by age, though it is under predicted for most of ages, and is also less successful in replicating the skewness of the wealth distribution.

Overall, the estimated model reasonably fits the main features of the actual data, though there are some discrepancies between the empirical observations and the model predictions. More improvement is expected in future work.

#### 7.2 Parameter Estimates

A full list of the model's estimated parameters is given in Appendix D. Here I discuss main characteristics of the estimates.

#### 7.2.1 Preference

The estimated rate with which all individuals discount utility values a year ahead is 97.56%. This means that the annual discount rate is 2.50%. Now, I turn attention to the CRRA coefficient.<sup>52</sup> With the CRRA form of utility,  $u = c^{1-\mu_0}/(1-\mu_0)$ , the coefficient of relative risk aversion is  $\mu_0$ , the intertemporal elasticity of substitution in consumption is  $\mu_0^{-1}$ . The typical estimated value for  $\mu_0$  in the literature is around -2. The estimated CRRA constants both for Type 1 and for Type 2 are much lower (0.483 and 0.472, respectively) than those in the macro literature, which is consistent with the recent studies that use micro data to estimate

 $<sup>^{52}</sup>$ Evans and Jovanovic (1989) assume that individuals are risk neutral, while Buera (2008a,b) and Mondragon-Velez (2007) consider the CRRA utility. None of these papers takes into account labor disutility.

the parameter (e.g. Keane and Wolpin (2001), Gourinchas and Parker (2002), Keane and Imai (2004)). In these studies, the estimated values typically range between 0.5 and 2. Interestingly, this paper's estimate for  $\mu_0$  is also close to Goeree, Holt, and Palfrey's (2002), who estimate the CRRA coefficient by laboratory experiments of generalized matching pennies games  $\hat{\mu}_0 = 0.440$ . This low value for risk aversion also affects the individual's propensity to become a self-employer presumably because the estimated variance of income from self-employment is much higher than that from (full-time) paid-employment. If compared with the studies on entrepreneurship, my CRRA constant implies less risk averse individuals: In his estimation, Buera (2008) does not estimate  $\mu_0$  (in his notation  $\sigma$ ) and sets  $\mu_0 = 1.50$  throughout.<sup>53</sup> Mondragon-Velez (2006) gives the estimate,  $\hat{\mu}_0 = 1.03$  (in his notation  $\sigma$ ).

My estimation results imply that nonpecuniary factors are important in explaining observed patterns of labor choice. The estimated value for disutility from self-employed work in the first year of any spell (317.3 for Type 1 and 334.9 for Type 2) is twice as large as that from (full-time) paid work (164.9 for Type 1 and 179.9 for Type 2). Notice also that the estimated values for benefits from continuing self-employment are also high: they are as half as the values for labor disutility from self-employment. These large values are necessary to well replicate the observed persistence of self-employment. In the previous studies on selfemployment, there were no estimates on nonpecuniary costs/benefits of entrepreneurship. Hamilton (2000) gives empirical findings that support the idea that self-employment offers significant nonpecuniary benefits. Specifically, in the data he uses (constructed from the 1984 panel of the Survey of Income and Program Participation (SIPP)), Hamilton (2000) finds that many self-employers experience lower earnings growth than wage workers do as well as lower earnings in initial periods of self-employment. He also finds little evidence that suggests that the earnings differential reflects the selection of low-ability individuals into self-employment. In the present study, I observe the higher mean and median incomes from self-employment than those from full-time paid-employment for each age in the age profiles of income. This finding is in contrast to Hamilton's (2000), though nonpecuniary benefits play important roles in replicating the age patterns of labor supply.<sup>55</sup> Mondragon-Velez 's (2006) unsatisfactory high estimates for entrepreneurial earnings may result from his exclusion of nonpecuniary factors. Without incorporating nonpecuniary costs/benefits of entrepreneurial work into a dynamic model, it may be very difficult to well capture dynamic aspects of self-employment in terms of both labor supply and income realization.

#### 7.2.2 Entrepreneurial Production Function

My formulation allows for the coefficient of capital returns in the entrepreneurial production function to differ by schooling. The estimated value for the college educated is 0.16  $(= \hat{\alpha}_0 + \hat{\alpha}_1)$  while that for the non-college educated is 0.17  $(= \hat{\alpha}_0)$ . This finding is consistent

<sup>&</sup>lt;sup>53</sup>In his study on effects of borrowing constraints on small manufacturing owner-firms in Ghana, Schündeln (2006)  $\mu_1 = 0.50$ .

<sup>&</sup>lt;sup>54</sup>Mondragon-Velez (2007) does not consider heterogeneity in risk attitude.

<sup>&</sup>lt;sup>55</sup>This finding is also consistent with recent studies that show empirical evidence suggesting that self-employment may derive procedural utility (see e.g. Frey and Benz (2008) and Fuchs-Schündeln (2008)). The idea of procedural utility is that people may care not only about the outcomes but about the procedures that lead to them, and in this paper's context, independent work in self-employment may give workers more satisfaction (the main difference of the two papers is that the latter allows for preference heterogeneity). Kawaguchi (2008), using job satisfaction scores in the NSLY79 and controlling for heterogeneity (in self-reporting one's own job satisfaction) at individual level, also finds evidence that self-employment gives workers more satisfaction than wage-employment does.

with an observation is that college educated self-employers are more likely in the service industry while in non-college educated self-employers are more likely in the construction industry (Mondragon-Velez (2005)). The estimates for capital returns in the previous literature are much higher than those obtained here. This is presumably because I incorporate the component of human capital accumulation into the entrepreneurial production function. In contrast, Evans and Jovanovic (1989), Buera (2008) and Mondragon-Velez (2006) estimate the following entrepreneurial production function:

$$y_t^s = A_t k_t^{\alpha}$$

where  $A_t$  is a compound component of nonstochastic and stochastic factors and human capital accumulation is not taken into account. The estimate of  $\alpha$  by Evans and Jovanovic's (1989) is 0.22 (it is 0.23 in Xu's (1998) reestimation). As in the present study, Mondragon-Velez (2006) considers differences in capital returns by education (non-college and college). His estimates are:  $\widehat{\alpha}$ (non-college) = 0.27 and  $\widehat{\alpha}$ (college) = 0.36.

#### 7.2.3 Human Capital

Next, consider the estimated income opportunities. The contributions of college education to the human capital component are 25.2% for self-employed work (=  $\hat{\gamma}_1^s$ ) and 24.0% for wage work (=  $\hat{\gamma}_1^w$ ). These values seem higher estimates if compared with the literature on college premium in the Mincerian wage equation (see, e.g., Heckman, Lochner and Todd (2008)). The difference between self-employment and paid-employment is small. The first one-year experience of full-time paid-employment increase the human capital component by  $0.9 \ (= \widehat{\gamma}_6^s - (\widehat{\gamma}_7^s/100))$  percent for self-employment and  $8.4 \ (= \widehat{\gamma}_6^w - (\widehat{\gamma}_7^w/100))$  percent for paid-employment. These two contrasting numbers are consistent with Kawaguchi's (2003) main finding that experience-earnings profiles were flatter in the human capital function for self-employment. Note, however, that Kawaguchi (2003) does not distinguish between experience of self-employment and that of wage employment. I distinguish these two, and the result is that in any spell, the first one-year of self-employment enhances the human capital component for self-employment by 7.5 (=  $\hat{\gamma}_4^s - \hat{\gamma}_5^s/100$ ) percent. In contrast, ever experience of self-employment enhances the human capital component only by 0.8 (=  $\hat{\gamma}_3^s$ ) percent for self-employment and decreases the human capital component slightly for paid-employment  $(-0.3 \ (= \widehat{\gamma}_5^w) \ \text{percent}).$ 

#### 7.2.4 Lower Bound for Net Worth

Evans and Jovanovic (1989), Xu (1999), Buera (2008a) and Mondragon-Velez (2006) using the common notation in the literature  $k_t \in [0, \lambda a_t]$  to express the borrowing constraints. The estimates of Evans and Jovanovic (1989), of Xu (1999) and of Buera (2008) are  $\hat{\lambda} = 1.75$ ,  $\hat{\lambda} = 2.01$  and  $\hat{\lambda} = 1.01$ , respectively. Mondragon-Velez (2006) does not estimate  $\lambda$  but compare various levels of  $\lambda$  ( $\lambda = 1.0$ , 1.25, 1.50, 1.75 and 2.0). In this paper,  $\lambda$  is not a constant, but a function of state variables. Specifically, the estimate for  $\lambda$  is given by

$$\widehat{\lambda} = \widehat{\lambda}(a_t, h_t^s, h_t^w, age_t, educ, type; \widehat{\zeta})$$

$$\equiv 1 - \frac{\widehat{a}_t}{a_t}$$

$$= 1 - \frac{\underline{a}(h_t^s, h_t^w, age_t, educ, type; \widehat{\zeta})}{a_t}$$

By incorporating the parameter estimates into the above equation, we have

$$\begin{split} \widehat{\lambda}(a_t, h_t^s, \, h_t^w, age_t, educ, type; \widehat{\zeta}) \\ &= 1 + \frac{1}{a_t} \cdot (\exp[9.256 + 0.201 \cdot I(educ = college) + 0.355 \cdot I(h_t^s = 1) \\ &+ 0.063 \cdot h_t^w - 0.357 \cdot \frac{(h_t^w)^2}{100} - 0.028 \cdot (age_t - 20) + 0.207 \cdot \frac{(age_t - 20)^2}{100}] \bigg) \,. \end{split}$$

As a example, this value becomes  $\hat{\lambda} = 1.62$  if I plug into the function  $h_t^w = 6$  (the median for years of paid employed work; see Table 3),  $age_t = 29$  (the median age) and  $a_t = 20008$  (the median net worth) for the non-college educated who has never become a self-employer.

#### 7.2.5 Type and the Propensity to Become a Self-Employer

It is interesting to notice that Type 1 individuals (comprising 28.0% of the simulated sample) and Type 2 individuals (comprising 72.0% of the simulated sample) are not much different in terms of risk attitude: the difference between the estimated values of Type 1's CRRA constant and of Type 2's is very small. Hence, heterogeneity in risk attitude seems to play a limited role in explaining the observed characteristics of the actual data. The positive values of the estimated  $\gamma_2^w$  and  $\gamma_2^w$  suggest that Type 1 individuals are less productive both as a self-employer and as a wage worker. Type 2 individuals, who are more productive both in self-employment and in wage employment, are more likely to become a self-employer. Looking at Table 11 that shows the transition rates for Type 1 and for Type 2, we find that the transition rates from and to self-employment and from and to full-time paid employment are higher for Type 2 individuals. The persistence of part-time paid employment, however, is higher while there is little difference as to the persistence of non-employment.

## 8 Policy Experiments

One of the attractive features of using a dynamic structural model in empirical studies is that they can be used to predict the effects of (ex ante) counterfactual/policy changes. In this section, I conduct three policy experiments to see their effects on the formation and continuation of self-employment. For each experiment, I first simulate behavior under the appropriately defined scenario, and then compare counterfactual behavior with the baseline behavior.

## 8.1 Experiment 1: Relaxing the Borrowing Constraints

The first experiment is to relax the estimated borrowing constraints to evaluate the extent to which they affect self-employment. Specifically, I make the asset floor  $\underline{a}_t$  negatively very large to see the effects (1) on the percentage of those with experience of self-employment during the same periods that are covered by the NLSY79, (2) on the distribution of decision period when first entry into self-employment occurs, and (3) on the one-period transition rates. I consider the case of  $\underline{a}_t = -\$30,000$  for any state (Experiment 1).<sup>56</sup>

Column "Exp.1" in Table 12 displays how the change affects the three key statistics in Table 1. Interestingly, relaxing the borrowing constraints weakens the propensity to enter

<sup>&</sup>lt;sup>56</sup>The estimated lower bound is between \$10,000 and \$18,000 for most of state variables.

into self-employment both for the non-college educated and for the college educated. This result presumably comes from the fact that there are two effects of relaxing the borrowing constraints: one is the direct effect that improves consumption smoothing over the life-cycle, and the other is the indirect effect that makes individuals more likely to be non-employed. If we look at the age profiles of labor supply under the Baseline and under Experiment 1 in Table 13, we find that the rates of non-employment under Experiment 1 are likely to be higher before age 30 but are likely to be lower after age 30. Table 13 also compares the predicted age profile of self-employment with the one under the Baseline and under Experiment 1. The proportions of self-employers are now higher from the average 7 percent in the simulated sample to around 9 to 10 percent for the two experiments. The rates of increase are 30 to 40 percent, which is comparable to Evans and Jovanovic's (1989) results.

Turning back to Table 13, it is noteworthy that college-educated self-employers are now likely to enter into self-employment later than under the Baseline while non-college educated self-employers are likely to enter into self-employment earlier. The exit rates after the first year from self-employment improves more for the non-college educated while the effects on the college educated is weaker. These results together seem to suggest the differences of the effects of borrowing constraints by the level of schooling. Relaxation of borrowing constraints facilitates both the formation of and the continuation of self-employed businesses especially for the non-college educated. Lastly, Figures 16-19 show that there are no significant differences between incomes under the Baseline and those under Experiment 1.

### 8.2 Experiment 2: Capital Subsidies

In this experiment, self-employers are subsidized through capital enhancement. Specifically, some amount of subsidy is given every year as long as individuals continue to be self-employed, and thus the amount of capital for self-employed is  $(k_t^{\$} + subsidy)$  rather than  $k_t^{\$}$  under the Baseline. I consider the case of subsidy = \$30,000.<sup>57</sup>

Column "Exp.2" in Table 12 displays how the subsidy scheme affects the three key statistics in Table 1. In comparison to the Baseline and Experiment 1, the ratios of those who ever experience self-employment for both schooling levels increase. While the college educated are now likely to enter into self-employment slightly later in their life, the non-college educated start self-employment earlier under the this subsidy scheme. The third item, however, shows that the subsidy scheme actually increases entries with shorter duration. In particular, nearly 50 percent of non-college educated self-employers exit in the first year.

Figures 20-23 show the changes in the age profiles of annual incomes of self-employment and of fullt-time paid employment. We find that increases of self-employment income are larger for the non-college educated. It is interesting to see that the mean incomes from full-time paid employment are now greater both for the non-college educated and for the college educated. This is presumably due to the decreases in the ratios of wage workers in the age profile of labor supply (Table 14).

<sup>&</sup>lt;sup>57</sup>This and next experiments should be taken as thought experiments rather than as real policy experiments because the main program conducted today by the U.S. Small Business Administration (SBA) to support small businesses is by loan guarantees, and the SBA does not provide direct loans to start or expand a business.

# 8.3 Experiment 3: Enhancing Self-Employment-Specific Human Capital (Training for Entrepreneurial Skill at School)

Most existing programs aims to assist unemployed workers to become self-employers through training. The next experiment is the one that gives indirect incentives for self-employment before entering the labor force. Specifically, it sees the effects of enhanced entrepreneurial skill (by, for example, training offered to improve skills that are useful for self-employed work). Conceptually, it corresponds to changing  $\hat{\gamma}_0^s = 1.839$  to a higher value. I set it equal to the constant part for the wage-sector specific human capital,  $\hat{\gamma}_0^w = 2.322$  (Experiment 3).

Column "Exp.3" in Table 12 displays how the policy affects the three key statistics in Table 1. The directions in the changes by this policy are similar to those by Experiment 2: it induces more individuals to enter into self-employment earlier in their life-cycle, but they are likely to exit from self-employment sooner. Figures 24-27 show that the directions in the changes in the mean incomes are also similar with Experiment 2. The changes in the age profile of labor supply are also similar (not shown) with slightly higher ratios of the self-employed.

## 9 Concluding Remarks

In this paper, I have proposed and estimated a life-cycle model of entrepreneurial choice and wealth accumulation. The data for estimation is taken from the cohort of young white males from the NLSY79. The inclusion of nonpecuniary benefits from being self-employed is important to well replicate the age patterns of labor supply. The estimated model is used to evaluate policy experiments. My results suggest that both a reasonable amount of subsidy and an enhancement of human capital specific to self-employment would have a small impact on the percentage of self-employment in the dimensions both of age profile and of ever-experience till age 39. In contrast, a moderate relaxation of the borrowing constraints encourages entries into self-employment with the average duration longer. Although experiments in this paper are conducted with the use of the U.S. data, insights from the experiments would be useful to think about what a government in post-communist or developing economies can and cannot do in promoting entrepreneurship.

The sample I have used for this study consists of white males. Public assistance programs for self-employment are more crucial to those in the minority who are seeking for a self-employment opportunity. They may face severer borrowing constraints. Self-employment assistance programs sometimes target specific groups; for example, structurally unemployed or displaced workers, and social assistance recipients. The framework in the present paper can be extended to study nonwhite self-employment.

As a first step toward structural estimation, the present study has considered the model of a single agent. It would be interesting and important to study various issues on self-employment by extending Blau's (1987) two-sector (entrepreneurial and corporate) general-equilibrium model to a dynamic one.<sup>58</sup> A more fundamental question is what entrepreneurial

<sup>&</sup>lt;sup>58</sup>Blau's (1987) time series regression analysis finds the following six effects could explain most of the increase from 1973 to 1982 in the proportion of male workers that were self-employed (in order of importance): an increase in a self-employment factor productivity index, a decrease in the marginal tax rate at \$7000 real income, an increase in the social security benefit level, a decrease in the real minimum wage, and a decrease in the age of the male labor force.

skills are.<sup>59</sup> Family background would also play an important role.<sup>60</sup> These and other interesting questions about self-employment are left for future research.

# Appendix A Exact Functional Forms Used to Simulate the Model

In this appendix, I show the exact forms of functions as they are used in *simulating* the life-cycle model. Essentially, when trying to match the model predictions to the empirical patterns in many dimensions, I am concerned about disentangling as precisely as possible unobserved heterogeneity from such effects as the life-cycle and the hysteresis effects on labor choice and saving decisions. Age variables and lagged choice variables in the utility function and the human capital functions are thus added to prevent the overstatement of the unobserved heterogeneity.

To estimate the model (by the simulated unconditional maximum likelihood method), I need parameterization for classification and measurement to connect simulated data and the observed data. I also need to determine the rule on how to fill in missing initial asset observations. The exact specification for these parts is given in Appendix C. The total number of the parameters in the current specification that are necessary for simulation (given an initial condition) is 75. In what follows,  $I(\cdot)$  is an indicator function that assigns one if the term inside the parenthesis is true and zero otherwise.

<sup>&</sup>lt;sup>59</sup>Lazear (2005) finds, using data from a list of MBA alumni at a business school, that those who have experience of self-employment (in an incorporated business) on average took courses from a broader area of specialties. The difference between the number of courses taken in the student's specialty and the average number of courses taken in other fields. White, Thornhill and Hampson (2006), using data collected from 31 MBA students with significant prior involvement in new venture creation and from 79 other student subjects with no new venture start-up experience, testosterone (an endocrine hormone) effect upon behavior (new venture creation) is partially mediated by the psychological (risk propensity).

<sup>&</sup>lt;sup>60</sup>For example, Hundley (2006) finds evidence that while both parental self-employment and family income significantly increase a man's propensity to become a self-employer, the former effect is amplified by the latter.

# A.1 Preference: Time Discount Factor, $\beta$ and the Utility Function, $u(\cdot; \epsilon_t^{ls}, \epsilon_t^{lw}; \mu)$ (27 Parameters)

I assume that  $\beta$  is a common constant for all individuals. The utility function is given as the following CRRA form augmented by  $\tau_t^s$ ,  $l_{t-1}^w$  and  $age_t$ :

$$\begin{array}{ll} u_t &=& u(c_t, l_t^s, l_t^w, \tau_t^s, l_{t-1}^w, age_t, \, type; \epsilon_t^{ls}, \epsilon_t^{lw}; \mu) \\ &=& \frac{c_t^{1-\mu_0(type)}}{1-\mu_0(type)} \\ &- \underbrace{\left[\mu_{1,s}(type, \tau_t^s) + \epsilon_t^{ls}\right] \cdot I(l_t^s > 0)}_{\text{disutility from self-employment}} \\ &- \underbrace{\left[\mu_{1,w}(type) + \epsilon_t^{lw}\right] \cdot \left[I(l_t^w \text{ is } full\text{-}time) + \mu_{1,w,part} \cdot I(l_t^w \text{ is } part\text{-}time)\right]}_{\text{disutility from paid-employment}} \\ &- \underbrace{\mu_{2,full}(type) \cdot I(l_t^s > 0 \,\&\, l_t^w \text{ is } full\text{-}time) - \mu_{2,part}(type) \cdot I(l_t^s > 0 \,\&\, l_t^w \text{ is } part\text{-}time)}_{\text{disutility from dual job holding}} \\ &+ \underbrace{\mu_{3,s \to s}(type, \tau_t^s) \cdot I(l_t^s > 0 \,\&\, \tau_t^s \geq 1)}_{\text{utility benefit from staving in SE}} \end{array}$$

where

$$\mu_0(type) = \mu_{00} + \mu_{01} \cdot I(type = 2)$$

is the parameter for relative risk aversion parameter ("prudence"),

$$\begin{cases} \mu_{1,s}(type, \tau_t^s) = \mu_{10,s} + \mu_{11,s} \cdot I(type = 2) + \mu_{12,s} \cdot \tau_t^s \\ \mu_{1,w}(type) = \mu_{10,w} + \mu_{11,w} \cdot I(type = 2) \end{cases}$$

are parameters for labor disutility and

$$\begin{cases} \mu_{2,full}(type) = \mu_{20,full} + \mu_{21,full} \cdot I(type = 2) \\ \mu_{2,part}(type) = \mu_{20,part} + \mu_{21,part} \cdot I(type = 2) \end{cases}$$

are additional disutility if he works as a self-employer and as a wage worker in the same period. Parameter  $\mu_{3,\cdot\cdot}$ , interpreted as utility benefits from staying in self-employment when he has been a for  $\tau_s^s$  years is

$$\mu_{3,s\to s}(type, \tau_t^s) = \mu_{40,s\to s} + \mu_{41,s\to s} \cdot I(type = 2) + \mu_{42,s\to s} \cdot \tau_t^s$$

# A.2 Constraints: Lower Bound for Financial Net Worth, $\underline{a}(\cdot;\zeta)$ , and the Consumption Floor, $c_{\min}$ , (8 Parameters)

The borrowing constraint requires that net financial assets not fall below some nonpositive lower bound. I allow the constraint to evolve as a function of the individual's level of education, work experience and (unobserved) type as well as age:

$$\underline{a}_{t} = \underline{a}(h_{t}^{s}, h_{t}^{w}, age_{t}, educ; \zeta) 
= -\exp[\zeta_{0} + \zeta_{1} \cdot I(educ = college) + \varsigma_{2} \cdot I(h_{t}^{s} = 1) 
+ \zeta_{3} \cdot h_{t}^{w} + \zeta_{4} \cdot \frac{(h_{t}^{w})^{2}}{100} + \zeta_{5} \cdot (age_{t} - 20) + \zeta_{6} \cdot \frac{(age_{t} - 20)^{2}}{100}]$$

for t = 2, ..., T.<sup>61</sup> The interpretation is that education, work experience and type serve (through human capital) to forecast future earnings potential. The dependence of the lower bound on age is in expectation of getting a better fit. Together with  $c_{\min}$ , which I assume is a common constraint for all individual, the lower bound gives the upper and lower bounds for  $c_t$  and for  $a_{t+1}$ :

$$\begin{cases} c_{\min} \le c_t \le y_t + (1 - \delta)k_t + (1 + r)a_t - \underline{a}_{t+1} \\ \underline{a}_{t+1} \le a_{t+1} \le y_t + (1 - \delta)k_t + (1 + r)a_t - c_{\min} \end{cases}$$

where  $c_t$  and  $a_{t+1}$  are related through the budget constraint:

$$c_t + a_{t+1} = y_t + (1 - \delta)k_t + (1 + r)a_t.$$

# A.3 Human Capital, $\overline{\Psi}^m(\cdot; \gamma^m)$ , m = w, s, and the Rental Price for Part-time Paid-Employment, $R^p$ (17 Parameters)

In the present study, I consider mode-specific human capital, that is, I distinguish human capital that is used for paid-employment  $(\overline{\Psi}_t^m)$  and that for self-employment  $(\overline{\Psi}_t^s)$ . For paid-employment, the market value of human capital is given by

$$R^{j} \cdot \overline{\Psi}_{t}^{w} = R^{j} \cdot \overline{\Psi}_{t}^{w} (h_{t}^{w}, l_{t-1}^{w}, h_{t}^{s}, age_{t}, educ, type; \gamma^{w})$$

$$= R^{j} \cdot \exp\left[\underbrace{\gamma_{0}^{w}}_{\text{constant}} + \underbrace{\gamma_{1}^{w} \cdot I(educ = college)}_{\text{schooling}} + \underbrace{\gamma_{2}^{w} \cdot I(type = 2)}_{\text{type}} + \underbrace{\gamma_{3}^{w} \cdot h_{t}^{w} + \gamma_{4}^{w} \cdot \frac{(h_{t}^{w})^{2}}{100}}_{\text{accumulated "own" experience}} + \underbrace{\gamma_{5}^{w} \cdot I(h_{t}^{s} = 1)}_{\text{ever experience in SE}} + \underbrace{\gamma_{6}^{w} \cdot (age_{t} - 20)}_{\text{age effect}}\right]$$

<sup>&</sup>lt;sup>61</sup>Remember that the initial financial net worth  $a_1$  must also satisfy  $a_1 \ge \underline{a}_1$ ; otherwise, the upper bound for  $k_1$ ,  $a_1 - \underline{a}_1$ , could be negative. In this paper, I simply look at the minimum of financial net worth in the first decision period for each cell in the following table.

age 20	-15840.0 (obs.no. = 138)
ages 21-23	-38308.0 (obs.no. = 177)
ages 24-25	-21864.0 (obs.no. = 72)

Why I do not collapse the table by education is that the numbers of observations with college for age 20 and of those with noncollege for ages 24-25 are very small. I simply assume that the lower bound,  $\underline{a}_1$ , for each age level is  $1.20 \times \text{minimum}$  (negative for all of the three case) of observations (-19008.0 for age 20, -45969.6 for ages 21 to 23 and -26236.8 for ages 24 and 25).

where  $R^j$  is the rental price for j-time paid employment. Since the relative price matters, I normalize  $R^f = 1$ . For self-employment, the value of human capital is given by

$$\begin{split} \overline{\Psi}^s_t &= \overline{\Psi}^s_t(h^s_t, \tau^s_t, h^w_t, age_t, educ, type; \gamma^s) \\ &= \exp[\underbrace{\gamma^s_0}_{\text{constant}} + \underbrace{\gamma^s_1 \cdot I(educ = college)}_{\text{schooling}} + \underbrace{\gamma^s_2 \cdot I(type = 2)}_{\text{type}} \\ &+ \underbrace{\gamma^s_3 \cdot I(h^s_t = 1)}_{\text{ever "own" experience}} + \underbrace{\gamma^s_4 \cdot \tau^s_t + \gamma^s_5 \cdot \frac{(\tau^s_t)^2}{100}}_{\text{accumulated "own" experience } in \ a \ row } + \underbrace{\gamma^s_6 \cdot h^w_t + \gamma^s_7 \cdot \frac{(h^w_t)^2}{100}}_{\text{accumulated experience in PE}} \\ &+ \underbrace{\gamma^s_8 \cdot (age_t - 20)}_{\text{age effect}}. \end{split}$$

As in the standard literature on human capital formation, the productivity of human capital for mode m=s,w in period t depends on his attained education ( $\gamma_{?}^{s}$  and ) and the quadratic form of his past experience in mode m ( $\gamma_{2,m'}^{m}$  and  $\gamma_{3,m'}^{m}$ ). Notice that the specification above assumes that unobserved heterogeneity with respect to entrepreneurial skills/talents is used only in self-employment ( $\gamma_{1,type}^{s}$ ). Additional terms are to capture an effect of work experience in the other mode ( $\gamma_{4}^{m}$ ), an age effect ( $\gamma_{5}^{m}$ ), a benefit from staying ( $\gamma_{6}^{m}$ ), and a first-year experience effect ( $\gamma_{7}^{m}$ ).

# A.4 Entrepreneurial Production Function, $f([\overline{\Psi}_t^s l_t^s], k_t, \epsilon_t^{ys}; \alpha)$ (2 Parameters)

As explained in the main text, the parametric form for f is

$$f([\overline{\Psi}_t^s l_t^s], k_t, \epsilon_t^{ys}; \alpha) = [\overline{\Psi}_t^s l_t^s]^{1-\alpha} k_t^{\alpha} \exp(\epsilon_t^{ys}),$$

where I consider the dependence of schooling on capital returns,  $\alpha$ :

$$\alpha = \alpha_0 + \alpha_1 \cdot I(educ = 1).$$

# A.5 Type Proportions, $Pr(type, initial\ conditions; \eta)$ (4 Parameters)

In the current specification, I assume that there are two unobserved types, type = 1,2. The type probabilities are logistic functions of the initial conditions. Specifically, they are written by

$$\Pr(type = 2; initial \ conditions, \ \eta) = \frac{\exp\left(\begin{array}{c} \eta_{0,2} + \eta_{1,2} \cdot I(educ = college) \\ + \eta_{2,2} \cdot \frac{a_1}{10000} + \eta_{3,2} \cdot I(\underline{age} \ge 23) \end{array}\right)}{1 + \exp\left(\begin{array}{c} \eta_{0,2} + \eta_{1,2} \cdot I(educ = college) \\ + \eta_{2,2} \cdot \frac{a_1}{10000} + \eta_{3,2} \cdot I(\underline{age} \ge 23) \end{array}\right)}$$

and  $Pr(type = 1; initial \ conditions, \eta) = 1 - Pr(type = 2; initial \ conditions, \eta).$ <sup>62</sup>

<sup>&</sup>lt;sup>62</sup>Variables related to family background and psychological characteristics could be included. In the present study I do not use them because I want to keep the numbers of individuals in the sample as large as possible so that the number of the self-employed does not become smaller in each age. For example, I need to drop 90 out of the current 1,916 individuals.

# A.6 Variances and the Covariances of the Period-by-Period Disturbance, $\sigma_{\epsilon}^2$ (6 Parameters)

The period-by-period disturbances to labor disutility,  $\epsilon_t^l = (\epsilon_t^{ls}, \epsilon_t^{lw})$  and  $\epsilon_t^y = (\epsilon_t^{ys}, \epsilon_t^{yw})$ , and to the borrowing constraint,  $\epsilon_t^a$ , are observed in the beginning of each period. I assume that  $\epsilon_t^l$ ,  $\epsilon_t^y$  and  $\epsilon_t^a$  are independently and identically distributed. For  $\epsilon_t^l$  and  $\epsilon_t^y$ , I assume serial independence across t, and I allow correlation between  $\epsilon_t^{ls}$  and  $\epsilon_t^{lw}$ . Specifically, I assume  $\epsilon_t^l \sim N(0, \Sigma^l)$ , where the variance-covariance matrix,  $\Sigma^l$ , is given by

$$\Sigma^l = \left( egin{array}{cc} \sigma^2_{\epsilon,ls} & \cdot \ \sigma_{\epsilon,(ls,lw)} & \sigma^2_{\epsilon,lw} \end{array} 
ight).$$

Similarly, I assume  $\epsilon_t^{ys} \sim N(0, \Sigma^y)$  where

$$\Sigma^y = \left( egin{array}{cc} \sigma^2_{\epsilon,ys} & \cdot \ \sigma_{\epsilon,(ys,yw)} & \sigma^2_{\epsilon,yw} \end{array} 
ight).$$

## A.7 Quasi-Terminal Emax Function, $Emax_{T^*}(\cdot; \kappa_{T^*})$ (5 Parameters)

To ease computational burden, the terminal period is set to be  $T^* < T$ .<sup>63</sup> I assume the following specification:

$$Emax_{T^*} = Emax_{T^*}(a_{T^*+1}, educ, h_{T^*+1}^s, h_{T^*+1}^w; \kappa_{T^*})$$

$$= \kappa_{T^*,1} \cdot a_{T^*+1} + \kappa_{T^*,2} \cdot \frac{(a_{T^*+1})^2}{10000}$$

$$+ \kappa_{T^*,3} \cdot I(educ = college)$$

$$+ \kappa_{T^*,4} \cdot h_{T^*+1}^s + \kappa_{T^*,5} \cdot h_{T^*+1}^w$$

Remember that this form of specification is one of many other alternatives. Future work should elaborate more on this issue.

# Appendix B Details on the Construction of the Data

The aim of this appendix is to show how the data for estimation,

$$X = \{X_i\}_{i=1}^{N}$$

$$= \{((l_{i,t}^s, l_{i,t}^w), (y_{i,t}^s, w_{i,t}), a_{i,t+1}, k_{i,t}, age_{i,t})_{t=1}^{\widehat{T}_i}, a_{i1}, educ_i\}_{i=1}^{N},$$

is constructed from the original 1979 cohort of the National Longitudinal Survey of Youth (NLSY79). $^{64}$  The first and last calender years for which information from data is utilized are 1979 and 2000. $^{65}$ 

Remember that the decision period in my life-cycle model is a *calender year* (job durations, for example, are measured in terms of years), while various information is available

<sup>&</sup>lt;sup>63</sup>Specifically, I set  $T^* = 30$  for all individuals.

<sup>&</sup>lt;sup>64</sup>All the original data was retrieved online at the "NLS Investigator" (http://www.nlsinfo.org/web-investigator/).

<sup>&</sup>lt;sup>65</sup>While I use the survey rounds up to 2002, I do not take 2002 as the final year because the year 2002 survey did not collect information on assets. The reason why I also use the year 2002 survey is that it covers weekly labor status information after the interview date in 2000.

on a weekly or monthly basis. So, the original data must be arranged to match the length of the decision period in the model. Other modifications are necessary to accommodate the data to the life-cycle model.

After showing the construction of the age variable in the next subsection, I show my rules on how to determine the first decision period for each individual in Subsection B.2. Subsection B.3 explains the restriction on the person dimension. I then give details on the construction of the main variables in Subsection B.4. For the sake of presentations, these processes are explained in order, but the actual process of data construction was not implemented in this order because, for example, the restriction on the person dimension needs some information on variables constructed in Subsection B.4.

### B.1 Constructing Age Variable, $age_{i,t}$

Respondent's data of birth was asked twice: in survey years 1979 and 1981. Although it is suspicious that there are some misreportings of birth year, <sup>66</sup> I simply use the 1979 information. First, I calculate an individual's age in months at each interview date by

interview date (month/year) - DOB (month/year) in the 1979 survey.

Then, I compute his age in months as of January of the interview year simply by

age at interview date (in months) - (interview month -1) (in months).

# B.2 Determining Age in the First Decision Period, $age_i$

Remember that schooling decision is not modelled in the life-cycle model. The individual in the model starts decisions one year after when he completed schooling. His year of schooling is taken as an exogenous variable in the dynamic model, and it does not change over time. To follow each individual in the data from his first decision period, I need to determine when he is considered to have finished schooling. Again, note that the decision period of my choice is a *calender* year. I must therefore be careful about the differences between calender years and *school* years, because it matters to the transition from schooling to work/non-work.

At each survey round, each respondent's school enrollment status as of May 1 of each year is available. I collapse the four categories in the original data into two as follows:

```
 \left\{ \begin{array}{l} {\rm Enrolled} \; \leftarrow \; {\rm ``Enrolled \; in \; high \; school" \; or \; ``Enrolled \; in \; college"} \\ {\rm Not \; Enrolled} \; \leftarrow \; {\rm ``Not \; enrolled, \; completed \; less \; than \; 12th \; grade"} \\ {\rm or \; ``Not \; enrolled, \; high \; school \; graduate."} \end{array} \right.
```

Using this information on "school enrollment status as of May 1st" (denoted by " $enrollment_{i,t}$ "), however, alone may not be precise. This problem is depicted as follows.

In most cases, we expect to observe patterns as shown in Figure? The horizontal arrow shows the timeline, and each partition corresponds to one period (t, t+1) and (t+1). For each period, the status of school enrollment (the first row) and the accumulated year of schooling (the second row) are observed. The story that would be the most plausible to the

<sup>&</sup>lt;sup>66</sup>I found 14 observations (out of the core while male sample; 2,439 observations) are suspected to have misreported his birth year. The number is small, so this problem should be minor. Also note that all original 2439 respondents answered the question in 1979. For details, see the documation attched to the data (will be available in due course).

information in this figure is the following. The individual graduated from school at some point after May 1st of period t, obtaining one more year of schooling. This is found by the information in period t+1: he is not enrolled in school and his year of schooling increased from the one in the previous year If that is the case, it is natural to assume that year t+1 is the first decision period.

Now, suppose that we observe a pattern as in Figure? In this case, it would be natural to assume that he stopped schooling in year t, even though he was reportedly enrolled in school year t+1 because he did not obtain one more year of schooling.

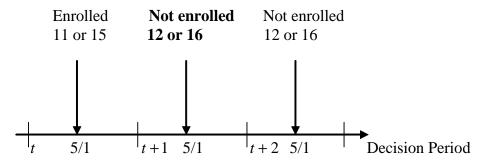


Figure ?: Typical Pattern of Transition from Schooling to Work/Non-Work

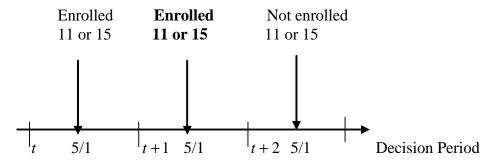


Figure ?: An Ambiguous Case of Transition

To avoid this type of ambiguity, I need to look at changes in his "Highest Degree Completed as of May 1st" (denoted by variable " $completed_{i,t}$ ") to determine the first decision period. Essentially, I want to find when his  $completed_{i,t}$  stopped to increase. The first decision period should be one year after the year when his  $completed_{i,t}$  firstly stopped to increase. When I see an individual's  $completed_{i,t}$  go up again after years of constant  $completed_{i,t}$ , I judge whether or not he is considered to have temporary left for additional schooling (see Restriction CS-4 in the next subsection). More formally, I adopt the following rules to determine when the first decision period is.

<u>Rule 1</u>. If individual i is not enrolled in school as of May 1st of year t (enrollment<sub>i,t</sub> = 0), then I say he is not enrolled in school in year t (in\_school<sub>i,t</sub> = 0).

<u>Rule 2</u>. If individual i is enrolled in school as of May 1st of year t (enrollment<sub>i,t</sub> = 1), then I say he is enrolled in school in year t (in  $school_{i,t} = 1$ ) if

$$completed_{i,t+1} > completed_{i,t}$$

and he is not enrolled in school year t ( $in\_school_{i,t} = 0$ ) if

$$completed_{i,t+1} \leq completed_{i,t}$$
.

In this way, for each individual, any calender year is categorized into "1" (attended school) or "0" (did not attend school), as long as "school enrollment status as of May 1" and "highest grade completed as of May 1" are available for that year. For most of individuals, "1"s appear in a row when young and "0"s in subsequent years. This case has no difficulty in determining the first decision period. For other individuals, I decided whether or not he is judged to have temporary left for additional schooling by looking at the computed hours worked and the monthly information on school enrollment.<sup>67</sup>

### B.3 Restriction on the Person Dimension, N

I employ the following steps to obtain individuals in the data used for this study. Table B-1 is a summary for the entire process to restrict on the person dimension (PD).

- <u>Restriction PD-1</u>. I extract the *white male* part in the *core random* sample.<sup>68</sup> This reduces the initial sample size 12,686 to 2,439.
- Restriction PD-2. Next, to drop individuals who have served in the *military*, I look at the "Weekly Labor Force Status" Section (from Week 0 in 1978 to Week 52 in 2000). If an individual's labor force status is "military" in any week since January 1, 1978, then he is excluded from the sample. I find 268 observations have ever been in the military (10.99%). This reduces the sample size 2,439 to 2,171.
- Restriction PD-3. Using the defined occupation for individual *i* in year *t* (see B.?.?. below), I exclude *professionals* and *farmers*. First, I exclude individuals who experienced any of the following occupations in any year *t*: "Accountants and auditors," "Lawyers and judges," "Health diagnosing occupations," and "Farming, forestry & fishing occupations." I then find, among the nonmilitary experienced, 361 observations have ever experienced professional or farmer. I put 259 of them back to the sample if they were a professional or a farmer before the first decision period, if they are judged to have temporally worked for such jobs, or if they were in such occupations as pharmacist and registered nurse. The number of excluded individuals is now 102 (4.70%). This process reduces the sample size 2,171 to 2,069.
- <u>Restriction PD-4</u>. I drop individuals who are judged to have temporary left for adult schooling (24 individuals),<sup>71</sup> to have started working late (26 years old or older; 80

<sup>&</sup>lt;sup>67</sup>Monthly attendance record is available after January, 1980.

 $<sup>^{68}</sup>$ One can retrive all necessary data online by filitering "R0173600  $\leq$  2" ("R0173600" is the sample identification code).

<sup>&</sup>lt;sup>69</sup>The 1979 year survey covers weekly labor status in 1978 as well.

<sup>&</sup>lt;sup>70</sup>Among those already excluded in Restriction CS-2, 26 observations have ever experienced professional or farmer.

<sup>&</sup>lt;sup>71</sup>I made judgment by looking at calculated hours worked, changes in the highest degree completed, and the monthly school enrollment information.

individuals) as well as 2 individuals whose first decision period is judged 14 years old. I also exclude individuals if it is difficult to determine the first decision period (6), or if no survey years are covered when working (41). The number of excluded individuals is 153 (7.39%), and this process reduces the sample size 2.069 to 1.916.

My final sample consists of 1,916 white males with a total of 32,166 person-year observations.

#### **B.4** Construction of the Main Variables

In this subsection, I show how the main variables are constructed from the NLSY79. First, I utilize the weekly information is available whether or not someone was self-employed.

#### B.4.1 Defining Self-Employment and Wage-Employment

To obtain information on whether an individual is a self-employer or a wage worker in a year, I look at the "Class of Worker" section (up to 2002 survey year). For each "job" (up to five jobs for each survey year) a respondent reports whether he<sup>73</sup>

- (1) worked/works for a private company or individual for wages, salary, or commission,
- (2) was/is a government employee,
  (3) was/is self-employed in his/her own business, professional practice or farm, or
  (4) was/is working without pay in a family business or farm,

for that job. In the NLSY79, the respondent is classified (by his/her answers to the job classification questions) as self-employed if<sup>74</sup>

"he or she owned at least 50 percent of the business, was the chief executive officer or principal managing partner of the business, or was supposed to file a form SE for Federal income taxes"

or he or she identifies himself or herself as

an independent contractor, independent consultant, or free-lancer.

Using this information, I associate each job with information on whether the respondent worked as a self-employer or as a paid-worker for that job. Specifically, a job is attached to self-employment if it is categorized as (3), and is attached to paid-employment if it is categorized as (1) or (2). Category (4) will not be considered as "worked/works."

Not all the jobs listed in the NLSY79 can be identified either as self-employed or as paid-employed. This is because the "Class of Worker" information is collected only for the current (the CPS item) jobs<sup>75</sup> and ones for which the respondent worked for more than 10

<sup>&</sup>lt;sup>72</sup>All references to a "job" should be understood as references to an employer.

<sup>&</sup>lt;sup>73</sup>Category (1) includes individuals working for pay for settlement houses, churches, unions, and other private nonprofit organizations until 1994 when these begun to be independently coded.

<sup>&</sup>lt;sup>74</sup>See ftp://www.nlsinfo.org/pub/usersvc/NLSY79/NLSY79%202004%20User%20Guide/79text/cow.htm.

<sup>&</sup>lt;sup>75</sup>In 1994, the occupation, industry and class of worker information for 353 CPS employers were not collected. This error would be innocuous for my study because these CPS employers were either less than 9 weeks in duration since the last interview, or were employers for whom the respondent worked less than 10 hours per week. For more information on this editing error, see http://www.nlsinfo.org/nlsy79/nlsy79 errata.php3.

(after 1988) or 20 (prior to 1988) hours a week and for more than 9 weeks since the last interview. This limited form of information should be innocuous for this study, however, because in the actual estimation these "temporary" jobs will not be counted as worked due to the discretization of the variable "hours worked." in Subsubsection B.4.2.<sup>76</sup>

For each job, we also have information (if provided) on labor market opportunities (the weekly average of hours worked<sup>77</sup> and the weekly average of hourly rate of pay). These items are used in the following calculation of the actual hours worked and the diecretization.

One caveat is that owners of incorporated businesses may or may be excluded if they draw a salary from their businesses and interpret this behavior as the one of a wage worker. Thus, the above definition of self-employers refers essentially to sole proprietors and partners of unincorporated businesses.

### B.4.2 Mode of Employment and Work Intensity, $(l_{i,t}^s, l_{i,t}^w)$

I look at the "Weekly Labor Force Status" Section and the "Dual Jobs" Section (1979-2000)<sup>78</sup> and the job characteristics information obtained above. For each individual, information on weekly labor force status is available up to the date that the last interview that he responded covers. So, the last year when the information is available is the one right before the year when "0" ("no info reported for week") appears in an array.

For each individual  $i \in \{1, ..., N\}$ , I know (if information is provided) whether job j (j = 101, ..., 105, 201, ..., 1905, 2001, ..., 2005)<sup>79</sup> is attached to self-employment or to paid-employment. I compute <math>i's total hours worked for job j in calender year t,  $total\_hours\_worked_{i,t}^j$ , by

$$total\_hours\_worked_{i,t}^j$$
, =  $weekly\_hours\_worked_i^j \times weeks_{i,t}^j$ ,

where  $weekly\_hours\_worked_i^j$  is individual i's weekly average of hours worked and  $weeks_{i,t}^j$  is the number of weeks he worked for job j in year t. Both of them are available in the NLSY79.

I then aggregate jobs according to whether they are attached to self- or to paid-employment. I calculate total hours worked for m-mode employment ( $m \in \{self, paid\}$ ) in year t,  $total\_hours\_worked_{i,t}^l$ , by

$$total\_hours\_worked^m_{i,t} = \sum_{j \in m} total\_hours\_worked^j_{i,t}.$$

Remember that I assume that the individual in the model chooses descretized hours worked. Specifically, I employ the following descretization that allows natural interpretation: in year t, individual i

 $\begin{cases} \text{did } not \text{ work as a self-employer if } 0 \leq total\_hours\_worked_{i,t}^{self} < 700 \text{ (} = 20 \text{ hours} \times 35 \text{ weeks),} \\ worked \text{ as a self-employer if } total\_hours\_worked_{i,t}^{self} \geq 700. \end{cases}$ 

<sup>&</sup>lt;sup>76</sup>Note that week-by-week information on hours worked and hourly rate of pay is collected for almost all jobs appearing in the data. So, if we do not care about the class of worker, we can well grasp total hours worked and wage earnings in any week.

<sup>&</sup>lt;sup>77</sup>In the 1988 survey round, the NLSY79 started asking hours worked at home separately for each job. By hours worked, I mean the sum of hours worked at workplace home and those at home.

<sup>&</sup>lt;sup>78</sup> "Weekly Labor Force Status" information is available (since January 1, 1978) on whether a respondent was (a) working, (b) associated with an employer, (c) unemployed, (d) out of the labor force, (e) not working, or (f) in active military duty.

<sup>&</sup>lt;sup>79</sup>Remember each calender year covers up to 5 jobs and we have 20 calender years; the first one or two digits correspond to survey years and the last digit to the job number.

and he

```
did not work as a wage earner if 0 \le total\_hours\_worked_{i,t}^{paid} < 700, worked as a part-time wage earner if 700 \le total\_hours\_worked_{i,t}^{paid} < 1400 (= 40 hours × 35 weeks), and worked as a full-time wage earner if total\_hours\_worked_{i,t}^{self} \ge 1400.
```

I do not consider the possibility that an individual decides on how many hours he works, and assume that if he works in self-employment or in full-time paid-employment, his hours worked is 2000, and if he works as a part-time wage worker they are 1000.80

The reason why I do not distinguish between full-time and part-time self-employment is that the number of individuals who choose part-time self-employment is very small for each age that is covered in the data. I say that he was non-employed in year t if he did work in both modes of employment. Note that as Table? In the main text shows, "dualemployment" (worked as a self-employer and as a wage earner in the same year) is observed with small fractions. One reason why one is self-employed and is a wage worker in the same year would be that he works for an employer during the day and runs his own business in the evenings. Another possible reason is that he worked as a wage worker early in the year and worked as self-employer late in the year.

#### B.4.3 Net Worth, $a_{i,t}$

Collecting information on assets began in survey year 1985, 81 with exceptions of survey years 1991 and 2002. Assets are measured at interview dates. To calculate financial net worth, I follow Keane and Wolpin (2001), Imai and Keane (2004) and many others who use asset information in the NLSY79: I first add up the following variables to construct total positive assets:82,83

- (1) "Market value of residential property the respondent or his spouse (R/S) owns"

- (2) "Total market value of vehicles including automobiles R/S owns"
  (3) "Total amount of money assets like savings accounts of R/S"
  (4) "Total market value of all other assets each worth more than \$500" and
  (5) "Total market value of farm/business/other property the R/S owns".

Then, to construct total debts, I add up the following items:

- (1) "Amount of mortgages & back taxes R/S owes on residential property"

- (1) "Amount of mortgages & back taxes R/S owes on residential property"
  (2) "Amount of other debts R/S owes on residential property"
  (3) "Total amount of money R/S owes on vehicles including automobiles"
  (4) "Total amount of other debts over \$500 R/S owes" and
  (5) "Total amount of debts on farm/business/other property R/S owes".

<sup>&</sup>lt;sup>80</sup>Under this categoralization, the mean hours worked for self-employment, for full-time paid-employment, and for part-time paid-employment over the ages covered in the data (20-39) are, 2056.2, 2315.5, and 1061.4, respectively. The hours worked for and for full-time paid-employment increase moderately over age, and the ones for part-time paid-employment are stable. This assumption thus seems innocuous.

<sup>&</sup>lt;sup>81</sup>Remember that this implies that the earliest age at which I have information on assets is essentially 20. <sup>82</sup>For Item (3), the total market value of stocks/bonds/mutual funds became distinguishable in 1988, and the total amount of money holdings like IRA/Keogh, 401k/403b and CDs became distinguishable in 1994.

<sup>&</sup>lt;sup>83</sup>If the respondent does not report at least one of the items, I set the assets variable to "missing." I do the same to the debts items.

I subtract the total debts from the total assets and call it *net worth*. I exclude top and bottom 1% of financial net worth (greater than \$653,755.7 and less than -72,600, respectively). The numbers of excluded observations are 181 and 180, respectively.

#### B.4.4 Income in Self-Employment and Wage in Paid-Employment, $(y_{i,t}^s, w_{i,t})$

Difficulties in measuring and interpreting income from self-employment are well known. If an individual i works for self-employment  $(l_{i,t}^s > 0)$  with a positive amount of business capital  $(k_{i,t} > 0)$ , then his income both from his entrepreneurial production function should be a combination of income from labor and from capital. The issue is whether or not the self-reported income from self-employment includes the returns to business capital,  $k_{t,t}$ . In the following, I explain the problem and how I mitigate it.

First, there are two sources of information on income in the NSLY79:

- (1) Information on "wage/salary" is obtained from the event history (in the Employer Supplement Section) on reported jobs. For each reported job, the respondent is asked wage and the time unit of the wage.
- (2) In addition, the NLSY79 has global questions on the amounts of various types of "annual income" in the previous year. These are summarized in the Income Section. In particular, the Income Section asks separately about "wage/salary income" and "business or farm income (after expense)."

At first, it would seem that information source (2) works better than source (1) because the distinction between "wage/salary income" and "business or farm" is explicit in (2) while it is obscure in (1). So, suppose that I use information source (2). It is unclear, however, what corresponds to  $y_{i,t}^s$ . It seems safe to assume neither "wage/salary income" nor "business or farm" contains the depreciated capital,  $(1 - \delta)k_t$ . The reason is shown in Table B-3 for my final person-year observations: "(Business income)/ $k_t$ " does not seem constant over changes in percentiles.

Some respondents are still likely to mix the returns to labor and the returns to capital, even though the Income Section asks about both income sources separately. As Fairlie (2005, pp.43-44) points out, and as is verified with my final sample, about half of the self-employed with positive earnings report wage/salary income, but do not report business income. Fairlie (2005) ascribes this problem to the ordering of questions. In the NLSY79, respondents are asked, (1) "How much money did you get from the military?"; (2) "Excluding military pay, how much money did you get from wages, salary, commissions, or tips?"; and (3) "Excluding anything you already mentioned, did you receive any business income?" Some of the self-employed thus may have reported their income in the second question and did not correct their mistake.<sup>84</sup>

To overcome this issue, I decided to use the sum of "salary/wage income" and "business income" in the Income Section as income from self-employment,  $y_{i,t}^s$ . I trim outliers of the income observations to remove their effects on the results. Note here that I do not drop entire persons with outliers from the sample, but in estimation I treat outliers as missing values. Specifically, if the sum of wage/salary and business incomes from the Income Section

<sup>&</sup>lt;sup>84</sup>Another issue is on the accuracy or the reliability of the question. The exact sentence of the question is: "How much did you receive *after expences* from your farm or business in the past calender year?" One odd thing is that we have no observations with negative business income.

exceeds \$1,000,000, I treat both wage/salary and business incomes as missing. The number of such observations is 16.

For wage from paid-employment,  $w_{i,t}$ , I use information source (1).

#### B.4.5 Education $(educ_i)$

Each respondent's highest grade completed as of May 1 of each year is also available.<sup>85</sup> I keep an individual's year of education constant through his decision periods.<sup>86</sup> After imputation, I collapse "Highest Grade Completed" into:

$$\begin{cases} \text{High-school Dropout } (HD) \text{: education } < 12 \\ \text{High-school Graduate } (HG) \text{: education } = 12 \\ \text{Some College } (SC) \text{: } 13 \leq \text{education } \leq 15 \\ \text{College Graduate } (CG) \text{: education } \geq 16. \end{cases}$$

In the actual implementation, I consider two levels of schooling: schooling H (HD or HG) and schooling C (SC or CG). I define the education dummy by

$$educ_i = \begin{cases} 0 & \text{if } i \text{ is a high-school dropout or graduate} \\ 1 & \text{otherwise.} \end{cases}$$

## Appendix C Details on the Construction of the Log Likelihood

## C.1 Classification Error for Hours Worked, $E^s$ and $E^w$ (2 parameters)

The classification error for self-employment is characterized by parameter  $E^s$  in the following way:

$$\Pr((l_{i,t}^s)^{obs} = 1 | \widetilde{l}_{i,type,t}^{sim} = 1) = E^s + (1 + E^s) \widehat{\Pr}((l_{i,t}^s)^{obs} = 1)$$

$$\Pr((l_{i,t}^s)^{obs} = 1 | \widetilde{l}_{i,type,t}^{sim} \neq 1) = (1 - E^s) \widehat{\Pr}((l_{i,t}^s)^{obs} = 1)$$

where

$$E^s = \frac{\exp(E_0^s)}{1 + \exp(E_0^s)}$$

and

$$\widehat{\Pr}((l_{i,t}^s)^{obs} = 1) = \frac{1}{N} \sum_{i=1}^N I((l_{i,t}^s)^{obs} = 1).$$

Note here that

$$\begin{split} & \Pr((l_{i,t}^{s})^{obs} = 1) \\ & = \Pr((l_{i,t}^{s})^{obs} = 1 | \widetilde{l^{s}}_{i,type,t}^{sim} = 1) \widehat{\Pr}((l_{i,t}^{s})^{obs} = 1) \\ & + \Pr((l_{i,t}^{s})^{obs} = 1 | \widetilde{l^{s}}_{i,type,t}^{sim} \neq 1) [1 - \widehat{\Pr}((l_{i,t}^{s})^{obs} = 1)], \end{split}$$

<sup>&</sup>lt;sup>85</sup>I do not use AFQT in this study because among the 1916 individuals in the Restriction CS-4, scores of 154 individuals are missing.

<sup>&</sup>lt;sup>86</sup>It is known that there are issues of inconsistencies on information on the highest grade completed in the NLSY79. For example, we sometimes observe an individual's "Highest Grade Completed" suddenly jumps even if his "School Enrollment Status"s are zero around that year. See the NLSY79 User's Guide (p.143) for details. I used my own judgment to determine one's highest grade completed when I saw inconsistensies.

which is equal to  $\widehat{\Pr}((l_{i,t}^s)^{obs}=1)$ . The classification error for full-, part- and zero-time paid employment,  $E^w$ , is constructed similarly. That is,

$$E^w = \frac{\exp(E_0^w)}{1 + \exp(E_0^w)}.$$

## C.2 Measurement Error for the Continuous Variables, $\sigma_{\xi,\cdot}^2$ (4 parameters)

First, the measurement error in *financial net worth* is modeled as

$$(a_{i,t})^{obs} = \widetilde{a}_{i,type,t}^{sim} + \xi_t^a$$

where  $\xi_t^a \sim N(0, \sigma_{\xi,a}^2)$  and  $\sigma_{\xi,a} = \sigma_{\xi,a,0} + \sigma_{\xi,a,1} | (a_{i,t})^{obs} |$ . Similarly, the measurement error in *income* from self-employment is modeled in

$$\exp(\xi_t^{y^s}) = |(y_{i,t}^s)^{obs} - \widetilde{y}_{i,type,t}^{sim}|$$

where  $\xi_t^{y^s} \sim N(0, \sigma_{\xi, y^s}^2)$ , and the the one from j-time paid-employment is modeled in

$$\exp(\xi_t^{y^w}) = |(y_{i,t}^w)^{obs} - \widetilde{y_{i,type,t}^w}|$$

where  $\xi_t^{y^w} \sim N(0, \sigma_{\xi, y^w}^2)$ .

#### C.3 Parametric Form of the Likelihood Contribution

With the given specification of classification/measurement errors, the actual expression for the likelihood contribution for individual i in mth simulation is given by

$$\begin{split} & \Pr(X_i | \widetilde{X}_{i,type}^{sim}, \theta) \\ & = \begin{bmatrix} \frac{1}{\sqrt{2\pi\sigma_{\xi,a}^2}} \exp\left[-\frac{[(a_{i,t})^{obs} - \widetilde{a}_{i,type,t}^{sim}]^2}{2\sigma_{\xi,a}^2}\right] \end{bmatrix} I(a_{i,1} \ is \ observed) \\ & \times \prod_{t \mid l_{i,t}^s = 1 \ is \ observed} \Pr((l_t^s)^{obs} \ is \ self-employment) \\ & \times \prod_{t \mid l_{i,t}^s = 0 \ is \ observed} \Pr((l_t^s)^{obs} \ is \ self-employment) \\ & \times \prod_{t \mid l_{i,t}^s = 0 \ is \ observed} \Pr((l_t^s)^{obs} \ is \ full-time \ paid-employment) \\ & \times \prod_{t \mid l_{i,t}^s = 0 \ is \ observed} \Pr((l_t^s)^{obs} \ is \ part-time \ paid-employment) \\ & \times \prod_{t \mid l_{i,t}^s = 0 \ is \ observed} \Pr((l_t^s)^{obs} \ is \ part-time \ paid-employment) \\ & \times \prod_{t \mid l_{i,t}^s = 0 \ is \ observed} \Pr((l_t^s)^{obs} \ is \ zero \ paid-employment) \\ & \times \prod_{t \mid l_{i,t}^s \ is \ observed} \left[ \frac{1}{|(l_t^s)^{obs} - \widetilde{y}_{i,type,t}^s|\sqrt{2\pi\sigma_{\xi,y}^2}} \exp\left[ -\frac{[\log((y_{i,t}^s)^{obs}) - \log(\widetilde{y}_{i,type,t}^s|)^2}{2\sigma_{\xi,y}^2} \right] \right] \\ & \times \prod_{t \mid y_{i,t}^s \ is \ observed} \left[ \frac{1}{|(y_{i,t}^w)^{obs} - \widetilde{y}_{i,type,t}^w|\sqrt{2\pi\sigma_{\xi,y}^2}} \exp\left[ -\frac{[\log((y_{i,t}^w)^{obs}) - \log(\widetilde{y}_{i,type,t}^w|)^2}{2\sigma_{\xi,y}^2} \right] \right] \\ & \times \prod_{t \mid y_{i,t}^s \ is \ observed} \left[ \frac{1}{|(2\pi\sigma_{\xi,y}^2)^{obs} - \widetilde{y}_{i,type,t}^w|\sqrt{2\pi\sigma_{\xi,y}^2}} \exp\left[ -\frac{[\log((y_{i,t}^w)^{obs}) - \log(\widetilde{y}_{i,type,t}^w|)^2}{2\sigma_{\xi,y}^2} \right] \right] \\ & \times \prod_{t \mid a_{i,t+1} \ is \ observed} \left[ \frac{1}{\sqrt{2\pi\sigma_{\xi,a}^2}} \exp\left[ -\frac{[(a_{i,t+1})^{obs} - \widetilde{a}_{i,type,t+1}^{sim}]^2}{2\sigma_{\xi,a}^2} \right] \right]. \end{aligned}$$

## Appendix D Parameter Estimates

All the parameter estimates are presented below. The number of estimated parameters is 64. Numerical values in parentheses are standard errors.<sup>87</sup> The maximized value for the log likelihood is -4886.575.

## D.1 Preference: Time Discount Factor, $\beta$ and the Utility Function, $u(\cdot; \mu)$ (15 Parameters)

### D.1.1 Time Discount Factor $(\beta)$

• 
$$\beta = 0.9755769$$

 $<sup>^{87}</sup>$ Standard errors of the parameters that are transformed from the estimated parameters are calculated by the delta method.

#### D.1.2 CRRA Constant $(\mu_0)$

• 
$$\mu_{00} = 0.4826716$$

$$\rightarrow \text{(CRRA constant)} \left\{ \begin{array}{l} \mu_0(type=1) = \mu_{00} = 0.4826716 \\ \mu_0(type=2) = \mu_{00} + \mu_{01} = 0.4701598 \\ \text{(...)} \end{array} \right.$$

#### D.1.3 Labor Disutility ( $\mu_1$ and $\mu_2$ )

$$\bullet \ \mu_{10,s} = 317.2780$$

• 
$$\mu_{11,s} = 17.59601$$

• 
$$\mu_{12,s} = -3.305609$$

$$\rightarrow \left\{ \begin{array}{l} \mu_{1,s}(type=1,\tau_t^s) = \mu_{10,s} + \mu_{12,s} \cdot \tau_t^s = 317.2780 - 3.305609 \cdot \tau_t^s \\ \mu_{1,s}(type=2,\tau_t^s) = \mu_{10,s} + \mu_{11,s} + \mu_{12,s} \cdot \tau_t^s = 334.87401 - 3.305609 \cdot \tau_t^s \end{array} \right.$$

• 
$$\mu_{10,w} = 164.8727$$

• 
$$\mu_{11,w} = 14.99203$$

$$\rightarrow \left\{ \begin{array}{l} \mu_{1,w}(type=1) = \mu_{10,w} = 164.8727 \\ \mu_{1,w}(type=2) = \mu_{10,w} + \mu_{11,w} = 179.86473 \end{array} \right.$$

• 
$$\mu_{10,w,part} = 0.5377413$$

$$\rightarrow \left\{ \begin{array}{l} [\mu_{1,w}(type) + \epsilon^{lw}_t] \cdot [I(l^w_t \text{ is } \textit{full-time}) + \mu_{1,w,part} \cdot I(l^w_t \text{ is } \textit{part-time})] \\ = 0.5377413 \cdot [\mu_{1,w}(type) + \epsilon^{lw}_t] \end{array} \right.$$

• 
$$\mu_{20,full} = 1822.401$$

• 
$$\mu_{21,full} = 220.5993$$

$$\rightarrow \left\{ \begin{array}{l} \mu_{2,full}(type=1) = \mu_{20,full} = 1822.401 \\ \mu_{2,full}(type=2) = \mu_{20,full} + \mu_{21,full} = 2043.0003 \\ \end{array} \right.$$

$$\bullet \ \mu_{20,part} = 1424.098_{(...)}$$

• 
$$\mu_{21,part} = 197.5852$$

$$\rightarrow \left\{ \begin{array}{l} \mu_{2,part}(type=1) = \mu_{20,part} = 1424.098 \\ \mu_{2,part}(type=2) = \mu_{20,part} + \mu_{21,part} = 1621.6832 \\ \end{array} \right.$$

#### D.1.4 Benefits from Staying in the Same Mode of Employment $(\mu_3)$

• 
$$\mu_{40,s\to s} = 159.9276$$

• 
$$\mu_{41,s\to s} = 23.56863$$

• 
$$\mu_{42,s\to s} = 9.834752$$

$$\rightarrow \left\{ \begin{array}{l} \mu_{4,s \to s}(type=1,\tau_t^s) = \mu_{40,s \to s} + \mu_{42,s \to s} \cdot \tau_t^s = 159.9276 - 9.834752 \cdot \tau_t^s \\ \mu_{4,s \to s}(type=2,\tau_t^s) = \mu_{40,s \to s} + \mu_{41,s \to s} + \mu_{42,s \to s} \cdot \tau_t^s = 183.49623 - 9.834752 \cdot \tau_t^s \end{array} \right.$$

## D.2 Lower Bound for Net Worth, $\underline{a}(\cdot;\zeta)$ , and the Consumption Floor, $c_{\min}(8 \text{ Parameters})$

#### **D.2.1** Lower Bound for Net Worth $(\underline{a}(\cdot;\zeta))$

• 
$$\zeta_0 = 9.256721$$
 (constant term)

- $\varsigma_3 = 0.060926$  (accumulated years of paid-employment)
- $\zeta_4 = -0.358549$  (accumulated years of paid-employment squared, divided by 100)
- $\zeta_5 = -0.029473$  (age)
- $\zeta_6 = 0.205846$  (age squared, divided by 100)

## D.2.2 Consumption Floor $(c_{\min})$ ,

• 
$$c_{\min} = 129.3269$$

# D.3 Human Capital, $\overline{\Psi}^m(\cdot; \gamma^m)$ , m = w, s, and the Rental Price for Part-time Paid-Employment, $R^p$ (21 Parameters)

## D.3.1 Paid-Employment $(\overline{\Psi}^w(\cdot; \gamma^w))$

• 
$$\gamma_0^w = 2.311925 \text{ (constant term)}$$

• 
$$\gamma_1^w = 0.240281$$
 (dummy for the college-educated)

• 
$$\gamma_2^w = 0.006273$$
 (dummy for Type 2)

• 
$$\gamma_3^w = 0.086725$$
 (accumulated years of paid-employment)

- $\gamma_4^w = -0.272293$  (accumulated years of paid-employment squared, divided by 100)
- $\gamma_5^w = -0.003291$  (dummy for experience of self-employment))
- $\gamma_6^w = 0.007934 \text{ (age)}$

#### D.3.2 Rental Price for Part-time Paid-Employment $(R^p)$

•  $R^p = 1.1647760$ 

### **D.3.3** Self-Employment $(\overline{\Psi}^s(\cdot; \gamma^s))$

- $\gamma_0^s = 2.444152$  (constant term)
- $\gamma_1^s = 0.280044$  (dummy for the college-educated)
- $\gamma_2^s = 0.008961$  (dummy for Type 2)
- $\gamma_3^s = 0.008406$  (dummy for experience of self-employment)
- $\gamma_4^s = 0.096725$  (accumulated years of self-employment in a row)
- $\gamma_5^s = -0.170103$  (accumulated years of self-employment in a row squared, divided by 100)
- $\gamma_6^s = 0.028571$  (accumulated years of paid-employment)
- $\gamma_7^s = -0.110880$  (accumulated years of paid-employment squared, divided by 100)
- $\gamma_8^s = 0.0655306 \text{ (age)}$

## D.4 Entrepreneurial Production Function, $f(\cdot; \alpha)$ (2 Parameters)

- $\alpha_0 = 0.1744350$  (capital returns)
- $\alpha_1 = -0.0123996$  (dummy for the college-educated)

$$\rightarrow \text{(capital returns)} \begin{cases} \alpha(educ = non\text{-}college) = \widehat{\alpha_0} = 0.1744350 \\ \alpha(educ = college) = \widehat{\alpha_0} + \widehat{\alpha_1} = 0.1620354 \\ \dots \end{cases}$$

## D.5 Type Proportions, $Pr(\cdot; \eta)$ (4 Parameters)

- $\eta_{1,2} = 0.4519807$  (dummy for the college-educated)
- $\eta_{2,2} = 0.0000025$  (net worth)
- $\eta_{3,2} = 0.6448548$  (dummy for age when started working being greater than or equal to (...)

$$\to \begin{cases} \Pr(type = 1) = 0.3658664 \\ \Pr(type = 2) = 0.6341336 \end{cases}$$

# D.6 Variances and the Covariances of the Period-by-Period Disturbance, $\sigma_{\epsilon,\cdot}^2$ (6 Parameters)

- $\sigma_{\epsilon,ls} = 136.69850$  (disutility from self-employed work)
- $\sigma_{\epsilon,lw} = 47.039350$  (disutility from paid-employed work)
- $\sigma_{\epsilon,(ls,lw)} = 2.6065150$  (disutility correlation between self- and paid-employed)
- $\sigma_{\epsilon,yw} = 0.2127060$  (income from paid-employed work)
- $\sigma_{\epsilon,(ys,yw)} = 0.0823533$  (income correlation between self- and paid-employed)

## **D.7** Quasi-Terminal Emax Function, $Emax_{T^*}(\cdot; \kappa_{T^*})$ (5 Parameters)

- $\kappa_{T^*,1} = 0.0218159$  (net worth)
- $\kappa_{T^*,2} = -0.0004184$  (net worth squared, divided by 10000)
- $\kappa_{T^*,3} = 13662.890$  (dummy for college-educated)
- $\kappa_{T^*,4} = 4946.5890$  (dummy for experience of self-employment)
- $\kappa_{T^*,5} = 306.77500$  (accumulated years of paid-employment)

#### D.8 Measurement Error (6 Parameters)

- $E_0^w = 2.8493010$  (whether paid-employed or not)
- $\sigma_{\xi,a,0} = 0.9165500$  (net worth)
- $\sigma_{\xi,a,1} = 0.8819036$  (coefficient for the absolute value of net worth)
- $\sigma_{\xi,y^s} = 28.736100$  (income from self-employment)
- $\sigma_{\xi,y^w} = 26.189700$  (income from paid-employment)

### References

- [1] Bates, Timothy. 1990. "Entrepreneurial Human Capital Inputs and Small Business Longevity." Review of Economics and Statistics 72 (4), 551-559.
- [2] Ben-Porath, Yoram. 1967. "The Production of Human Capital and the Life Cycle of Earnings." *Journal of Political Economy* **75** (3), 352-365.
- [3] Blau, David M. 1987. "A Time-Series Analysis of Self-Employment in the United States." *Journal of Political Economy* **95** (3), 445-467.
- [4] Buera, Francisco J. 2008a. "A Dynamic Model of Entrepreneurship with Borrowing Constraints: Theory and Evidence." Unpublished manuscript, University of California, Los Angels.
- [5] —, 2008b. "Persistency of Poverty, Financial Frictions, and Entrepreneurship." Unpublished manuscript, University of California, Los Angels.
- [6] Cagetti, Marco. 2003. "Wealth Accumulation over the Life Cycle and Precautionary Savings." Journal of Business & Economic Statistics 21 (3), 339-353.
- [7] —, and Mariacristina De Nardi. 2006. "Entrepreneurship, Frictions, and Wealth." *Journal of Political Economy*, **114** (5), 835-870.
- [8] Campbell, Jeffrey R. and Mariacristina De Nardi. 2007. "A Conversation with 590 Nascent Entrepreneurs." Federal Reserve Bank of Chicago WP-2007-20.
- [9] Castañdeda, Ana, Javier Díaz-Giménez, and José-Víctor Ríos-Rull. 2003. "Accounting for the U.S. Earnings and Wealth Inequality." *Journal of Political Economy* **111** (4), 818-857.
- [10] Davis, Steven J., John Haltiwanger, Ron S. Jarmin, C.J. Krizan, Javier Miranda, Alfred Nucci, Kristin Sandusky. 2007. "Measuring the Dynamics of Young and Small Businesses: Integrating the Employer and Nonemployer Universes." NBER Working Paper 13226.

- [11] Dunn, Thomas, and Douglas Holtz-Eakin. 2000. "Financial Capital, Human Capital, and the Transition to Self-Employment: Evidence from Intergenerational Links." *Journal of Labor Economics* **18** (2), 282-305.
- [12] Evans, David S., and Boyan Jovanovic. 1989. "An Estimated Model of Entrepreneurial Choice under Liquidity Constraints." *Journal of Political Economy* **97** (4), 808-827.
- [13] —, and Linda S. Leighton. 1989. "Some Empirical Aspects of Entrepreneurship." American Economic Review 79 (3), 519-535.
- [14] Fafchamps, Marcel, and John Pender. 1997. "Precautionary Saving, Credit Constraints, and Irreversible Investment: Theory and Evidence from Semiarid India." Journal of Business and Economic Statistics 15 (2), 180-194.
- [15] Fairlie, Robert W. 2005. "Self-Employment, Entrepreneurship, and the NLSY79." Monthly Labor Review 128 (2), 40-47.
- [16] Fernández-Villaverde, Jesús, José Enrique Galdón-Sánchez, and Luis Carranza. 2003. "Entrepreneurship, Financial Intermediation and Aggregate Activity." Unpublished manuscript, University of Pennsylvania, Universidad Pública de Navarra, and Universidad de Navarra.
- [17] Frey, Bruno S. and Matthias Benz. 2008. "Being Independent is a Great Thing: Subjective Evaluations of Self-Employment and Hierarchy." *Economica* **75** (298), 362-383.
- [18] Fuchs-Schündeln, Nicola. 2008. "On Preferences for Being Self-Employed." *Journal of Economic Behavior and Organization*, Forthcoming.
- [19] Goeree, Jacob K., Charles A. Holt, and Thomas R. Palfrey. 2002. "Risk Averse Behavior in Generalized Matching Pennies Games." Games and Economic Behavior 45 (1), 97-113.
- [20] Gourinchas, Pierre-Olivier, and Jonathan A. Parker. 2002. "Consumption over the Life Cycle." *Econometrica* **70** (1), 47-89.
- [21] Hamilton, Barton H. 2000. "Does Entrepreneurship Pay? An Empirical Analysis of the Returns of Self-Employment." *Journal of Political Economy* **108** (3), 604-631.
- [22] Heckman, James J., Lance J. Lochner, Petra E. Todd. 2008. "Earnings Functions and Rates of Return." *Journal of Human Capital* 2 (1), 32-68.
- [23] —, and Guilherme Sedlacek. 1985. "Heterogeneity, Aggregation, and Market Wage Functions: An Empirical Model of Self-Selection in the Labor Market." *Journal of Political Economy* **93** (6), 1077-1125.
- [24] Herranz, Neus, Stefan Krasa and Anne P. Villamil. 2007. "The Impact of Entrepreneur Characteristics and Bankruptcy Rules on Firm Performance." Unpublished manuscript, University of Illinois at Urbana-Champaign.
- [25] Holmes, Thomas J., and James A. Schmitz, Jr. 1990. "A Theory of Entrepreneurship and Its Application to the Study of Business Transfers." *Journal of Political Economy* **98** (2), 265-294.

- [26] —, and —. 1995. "On the Turnover of Business Firms and Business Managers." *Journal of Political Economy* **103** (5), 1005-1038.
- [27] Holtz-Eakin, Douglas, David Joulfaian, and Harvey S. Rosen. 1994a. "Entrepreneurial Decisions and Liquidity Constraints." RAND Journal of Economics 25 (2), 334-347.
- [28] —, —, and —. 1994b. "Sticking It Out: Entrepreneurial Survival and Liquidity Constraints." Journal of Political Economy 102 (1), 53-75.
- [29] Hundley, Greg. 2006. "Family Background and the Propensity for Self-Employment." Industrial Relations 45 (3), 377-392
- [30] Hurst, Erik, and Annamaria Lusardi. 2004. "Liquidity Constraints, Household Wealth, and Entrepreneurship." Journal of Political Economy 112 (2), 319-347.
- [31] Imai, Susumu, and Michael P. Keane. 2004. "Intertemporal Labor Supply and Human Capital Accumulation." *International Economic Review* **45** (2), 601-641.
- [32] Kawaguchi, Daiji. 2003. "Human Capital Accumulation of Salaried and Self-Employed Workers." *Labor Economics* **10** (1), 55-71.
- [33] —. 2008. "Self-Employment Rents: Evidence from Job Satisfaction Scores." *Hitotsubashi Journal of Economics* **49** (1), 35-45.
- [34] Keane, Michael P., and Robert M. Sauer. 2007. "A Computationally Practical Simulation Estimation Algorithm for Dynamic Panel Data Models with Unobserved Endogenous State Variables," Mimeo, University of Technology Sydney and University of Southampton.
- [35] —, and Kenneth I. Wolpin. 1994. "The Solution and Estimation of Discrete Choice Dynamic Programming Models by Simulation and Interpolation: Monte Carlo Evidence." Review of Economics and Statistics 76 (4), 648-672.
- [36] —, and —. 1997. "The Career Decisions of Young Men." *Journal of Political Economy* **105** (3), 473-522.
- [37] —, and —. 2001. "The Effect of Parental Transfers and Borrowing Constraints on Educational Attainment." *International Economic Review* **42** (4), 1051-1103.
- [38] Lazear, Edward P. 2005. "Entrepreneurship." Journal of Labor Economics 23 (4), 649-680.
- [39] Li, Wenli. 2002. "Entrepreneurship and Government Subsidies: A General Equiilbrium Analysis." *Journal of Economic Dynamics & Control* **26** (11), 1815-1844.
- [40] Lucas, Robert E, Jr. 1978. "On the Size Distribution of Business Firms." *Bell Journal of Economics* **9** (2), 508-523.
- [41] Meh, Césaire A. 2008. "Business Risk, Credit Constraints, and Corporate Taxation." Journal of Economic Dynamics and Control 32 (9), 2971-3008.
- [42] Mincer, Jacob. 1958. "Investment in Human Capital and Personal Income Distribution." Journal of Political Economy 66 (3), 281-302.

- [43] Mondragon-Velez, Camilo. 2005. "Entrepreneurship Types, Transition and Returns in the U.S." Mimeo, Georgetown University.
- [44] —. 2006. "The Transition to Entrepreneurship: Human Capital, Wealth and the Role of Liquidity Constraints." Mimeo, Georgetown University.
- [45] Pavan, Marina. 2008. "Consumer Durables and Risky Borrowing: The Effects of Bunkruptcy Protection" Mimeo, University College Dublin.
- [46] Quadrini, Vincenzo. 1999. "The Imporrance of Entrepreneurship for Wealth Concentration and Mobility." Review of Income and Wealth 45 (1), 1-19.
- [47] —. 2000. "Entrepreneurship, Saving, and Social Mobility." Review of Economic Dynamics 3 (1), 1-40.
- [48] Rendon, Sílvio. 2006. "Job Search and Asset Accumulation under Borrowing Constraints." *International Economic Review* 47 (1), 233-263.
- [49] Rissman, Ellen R. 2003. "Self-Employment as an Alternative to Unemployment." Federal Reserve Bank of Chicago, WP-2003-34.
- [50] —. 2006. "The Self-Employment Duration of Younger Men Over the Business Cycle." Federal Reserve Bank of Chicago, *Economic Perspectives* **30** (3), 14-27.
- [51] —. 2007. "Labor Market Transitions and Self-Employment." Federal Reserve Bank of Chicago WP-2007-14.
- [52] Rosenzweig, Mark R., and Kenneth I. Wolpin. 1993. "Credit Market Constraints, Consumption Smoothing, and the Accumulation of Durable Production Assets in Low-Income Countries: Investments in Bullocks in India." *Journal of Political Economy* **101** (2), 223-244.
- [53] Schjerning, Bertel. 2006. "A Dynamic Model for Occupational Choice, Savings and Formation on Entrepreneurial Human Capital under Liquidity Constraints and Income Uncertainty." Unpublished manuscript, University of Copehagen.
- [54] Schündeln, Matthias. 2006. "Modeling Firm Dynamics to Identify the Cost of Financing Constraints in Ghanaian Manufaturing." Unpublished manuscript, Harvard University.
- [55] Terajima, Yaz. 2006. "Education and Self-Employment: Changes in Earnings and Wealth Inequality." Bank of Canada Working Paper No. 2006-40.
- [56] van der Klaauw, Wilbert, and Kenneth I. Wolpin. 2006. "Social Security and the Retirement and Savings Behavior of Low Income Households." Unpublished manuscript, Federal Researve Bank of New York and University of Pennsylvania.
- [57] White, Roderick E., Stewart Thornhill and Elizabeth Hampson. 2006. "Entrepreneurs and Evolutionary Biology: The Relationship between Testosterone and New Venture Creation" Organizational Behavior and Human Decision Processes 100 (1), 1–34.
- [58] Willis, Robert J. and Sherwin Rosen. 1979. "Education and Self-Selection." *Journal of Political Economy* 87 (5), S7-S36.

[59] Xu, Bin. 1998. "A Reestimation of the Evans-Jovanovic Model Entrepreneurial Choice Model." *Economics Letters* **58** (1), 91-95.

Table 1: Income Differences by Educational Attainment (NLSY79; White Males; Aged 20-39)

	Non-college educated	College educated
Mean annual income from self-employment	44978.7	63378.1
(No.Obs.)	(1359)	(720)
Mean annual income from full-time paid-employment	28464.6	40500.6
(No.Obs.)	(14019)	(8276)

Note 1: Monetary values are in terms of year 2000 dollars.

Table 2: Differences of Self-Employment by Educational Attainment (NLSY79; White Males; Aged 20-39)

	Non-college	College
	educated	educated
Ever experience of	31.78**	27.48
self-employment (%)		
(No.Obs.)	(1199)	(717)
First entry into	62.72***	74.62
self-employment occurs in		
less than or equal to first eight		
decision years (%)		
(No.Obs.)	(381)	(197)
Exit from self-employment	32.28*	28.57
in a year (%)		
(No.Obs.)	(550)	(287)

- Note 1: The data is constructed from the 1979 cohort of the National Longitudinal Survey of Youth (NLSY79). The sample includes 1916 white males. See Section 4 for details of the data.
- Note 2: "Non college-educated" individuals are highschool dropouts and highschool graduates, and "Colleged-educated" are individuals with some college education and more.
- Note 3: "Ever or never experience" is measured at the last periods observed in the data.
- Note 4: "Decision years" are calender years during which individuals are in the labor force.
- Note 5: \*\*\*,\*\* and \* indicate statistical difference at 1%, 5% and 10% levels of significance, respectively.

Table 3: Summary Statistics (NLSY79; White Males; Aged 20-39)

Variable	No.Obs.	Mean	Std.Dev.	Median	Max	Min
(Panel 1. Initial conditions)						
Age at the first decision period (%)						
20	1916	0.627	-	-	1	0
21	1916	0.114	-	-	1	0
22	1916	0.112	-	-	1	0
23	1916	0.083	-	-	1	0
24	1916	0.042	-	-	1	0
25	1916	0.022	-	-	1	0
Educational attainment (%)						
Non college-educated	1916	62.58	_	-	1	0
College-educated	1916	37.42	-	-	1	0
Net worth at the initial age of decisions	387	11940.8	39499.7	3952	576000	-38308
(Panel 2. Pooled)						
Age	32166	29.03	5.29	29	20	39
Labor supply (%)						
Self-employed	31494	0.069	_	-	1	0
Paid-employed, full-time	31494	0.705	_	-	1	0
Paid-employed, part-time	31494	0.099	-	-	1	0
Non-employed	31494	0.101	-	-	1	0
SE & full-time PE	31494	0.013	-	-	1	0
SE & part-time PE	31494	0.012	-	-	1	0
Experience of paid-employed work (years)	32166	6.27	4.65	6	19	0
Annual Income from self-employment	2079	51350.8	56971.4	36900	884801	64
Annual Income from paid-employment						
Full-time	22295	32932.4	23900.2	28560	990057	184
Part-time	3417	14256.8	10885.6	11900	228000	143
Net worth	17169	57312.4	118703.6	20008	2673988	-72600

Note 1: "Non college-educated" individuals are highschool dropouts and highschool graduates, and "College-educated" are individuals with some college education and more.

Note 2: "Years of paid-employed work experience" counts 1-year experience if an individual works as a full-time as a full-time wage worker, and 0.5-year experience if he works as a part-time wage worker.

Note 3: Monetary values are in terms of year 2000 dollars.

Table 4: Marginal Distribution of Labor Supply Decisions by Age

	Self-	Paid-		Non-	Dual-	
Age (No.Obs.)	employed	employed Full-time	Part-time	employed	employed SE & Full-time PE	SE & Part-time PE
20 (1172)	2.4%	58.8% 689	14.6% 171	22.9% 268	0.9% 10	0.5% 6
21 (1393)	3.4%	61.7% 859	12.8% 178	20.8%	0.6%	0.7%
22 (1609)	3.9% 62	64.3% 1035	12.0% 193	17.9% 288	1.1% 18	0.8%
23 (1751)	4.6% 81	66.1% 1157	11.3% 197	15.9% 278	1.0%	1.1%
24 (1820)	6.0%	74.7% 1359	8.6% 157	8.4% 153	1.2%	1.1%
25 (1848)	7.3% 134	76.5% 1409	7.8% 144	6.5% 121	1.2%	0.9% 17
26 (1829)	6.6%	77.6% 1419	6.8% 125	5.9% 108	2.0%	1.1%
27 (1826)	6.1%	77.9% 1422	7.3% 133	5.8% 106	1.6%	1.3%
28 (1817)	7.5% 136	73.3% 1331	9.0% 164	7.3% 133	1.8%	1.2%
29 (1795)	7.5% 134	67.9% 1218	13.3% 239	7.7% 138	1.9% 35	1.7%
30 (1780)	7.8% 139	67.7% 1205	13.5% 240	8.0% 143	1.4% 25	1.6%
31 (1750)	7.7% 134	65.8% 1151	14.2% 249	8.6% 151	1.8%	1.9%
32 (1735)	7.8% 136	68.2% 1183	12.2% 211	8.5% 148	1.6%	1.7%
33 (1708)	8.0% 137	69.1% 1181	11.0% 188	9.3% 158	1.5% 25	1.1% 19
34 (1686)	8.2% 138	69.0% 1164	10.6% 178	9.0% 152	1.5% 25	1.7%
35 (1636)	8.7% 143	69.9% 1143	9.7% 159	9.8% 160	1.0%	0.9% 15
36 (1446)	8.6% 125	73.1% 1057	7.5% 108	9.1% 132	0.8%	0.9%
37 (1199)	8.8% 106	76.6% 918	3.2%	9.1% 109	1.1%	1.3%
38 (956)	9.6% 92	77.2% 738	3.5%	8.6% 82	0.6%	0.5%
39 (738)	8.8% 65	77.9% 575	2.2% 16	9.3% 69	0.8%	0.9% 7

Note: Percentages and number of observations.

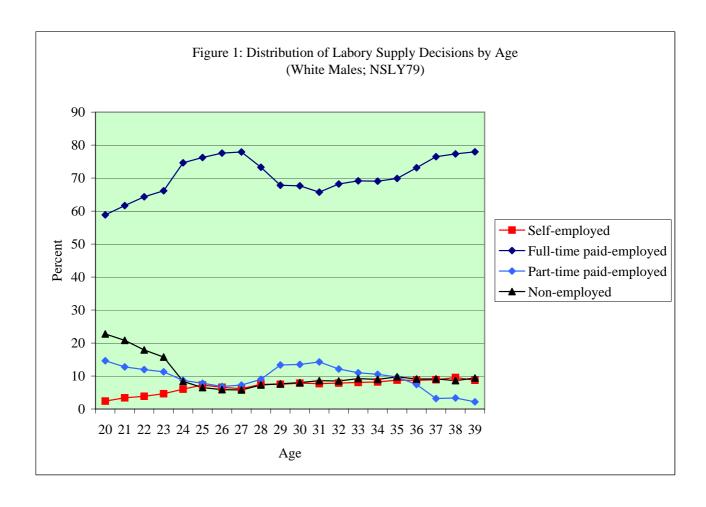


Table 5: Distribution (%) of the Number of Entries into Self-Employment

Number of			
entries into			
self-employment	All individuals	(Non-college)	(College)
0	69.8	68.2	72.5
1	19.5	20.8	17.4
2+	10.7	11.0	10.1
	100.0	100.0	100.0
(No.Obs.)	(1916)	(1199)	(717)

Note: Measured at the last periods observed in the data.

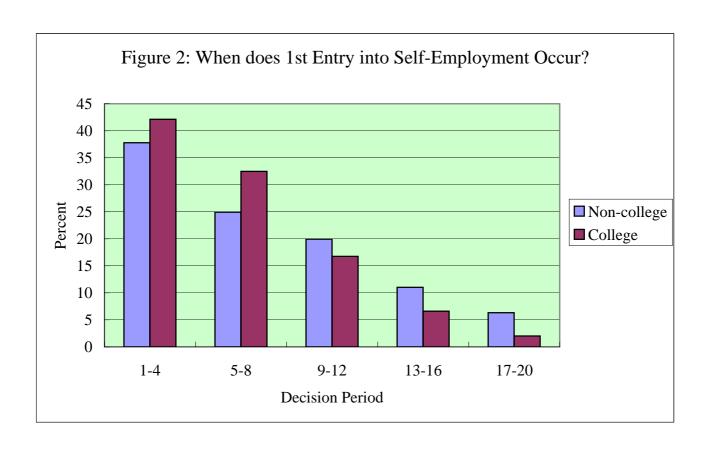


Table 6: Transition Matrices for Labor Supply Decisions (aged 20-39) by Schooling

Actual						Predicted				
Non-colle	ege	Labor supply (t)			Non-college		Labor supp	ly (t)		
		SE	PE	PE	NE		SE	PE	PE	NE
Labor supply (t-1)			Full-time	Part-time		Labor supply (t-1)		Full-time	Part-time	
SE						SE				
	Row %	75.4	7.2	2.6	6.2	Row %	83.0	10.3	0.9	5.8
	Column %	91.4	4.1	4.8	7.9	Column %	91.1	6.5	1.1	8.3
PE, Full-time						PE, Full-time				
	Row %	1.0	85.4	7.5	4.5	Row %	4.1	81.9	9.0	4.9
	Column %	1.2	49.2	14.1	5.7	Column %	4.5	52.3	11.0	7.1
PE, Part-time	e					PE, Part-time				
	Row %	1.7	51.1	28.0	18.4	Row %	2.2	49.0	43.3	5.5
	Column %	2.0	29.4	52.2	23.3	Column %	2.4	31.3	52.6	7.9
NE						NE				
	Row %	4.4	29.9	15.5	49.7	Row %	1.8	15.5	29.0	53.7
	Column %	5.4	17.2	28.9	63.1	Column %	2.0	9.9	35.3	76.7

Actual						Predicted				
College	_	Labor supply (t)				College		Labor supp	ly (t)	
	_	SE	PE	PE	NE		SE	PE	PE	NE
Labor suppl	ly (t-1)		Full-time	Part-time		Labor supply (t-1)		Full-time	Part-time	
SE						SE				
	Row %	73.6	8.4	3.3	4.2	Row %	85.8	8.7	1.1	4.3
	Column %	88.8	4.2	6.3	7.6	Column %	89.7	4.3	3.2	6.5
PE, Full-tin	ne					PE, Full-time				
	Row %	0.9	89.5	5.9	2.2	Row %	4.3	91.6	2.8	1.2
	Column %	1.1	45.5	11.3	4.0	Column %	4.5	45.4	7.9	1.9
PE, Part-tin	ne					PE, Part-time				
	Row %	2.9	56.0	27.8	12.5	Row %	4.1	69.7	19.2	7.0
	Column %	3.5	28.5	53.5	22.9	Column %	4.3	34.5	54.0	10.5
NE						NE				
	Row %	5.5	42.7	15.0	35.7	Row %	1.4	31.9	12.4	54.3
	Column %	6.6	21.7	28.9	65.5	Column %	1.5	15.8	34.9	81.1

Note 1: NE stands for non-employed, SE for self-employed, and PE for paid-employed.

Note 2: Rows labeled by "Row" contain the distribution of destinations (period t+1) conditional on origin (period t). Rows labeled by "Column" contain the distribution of origins conditional on destination. conditional on destination.

Note 3: "SE and full-time PE" and 'SE and part-time PS" are omitted, so the sums of the numbers across row or column are not 100.0.

Table 7: Transition Matrices for Labor Supply Decisions by Age Group

Actual				•	Predicted	•	•			
Aged 20-29	Labor supply (t)				Aged 20-29		Labor supply (t)			
	SE	PE	PE	NE		SE	PE	PE	NE	
Labor supply (t-1)		Full-time	Part-time		Labor supply (t-1)		Full-time	Part-time		
SE					SE					
Row %	69.8	10.7	3.5	5.3	Row %	87.3	9.4	2.3	1.1	
Column %	89.8	5.8	6.3	7.8	Column %	94.3	6.0	2.6	1.6	
PE, Full-time					PE, Full-time					
Row %	1.3	85.5	7.1	4.5	Row %	2.5	77.4	13.4	6.7	
Column %	1.7	46.0	12.9	6.6	Column %	2.7	50.0	15.4	10.2	
PE, Part-time					PE, Part-time					
Row %	2.5	52.0	26.8	17.9	Row %	2.1	50.4	47.1	0.4	
Column %	3.2	27.9	48.9	26.5	Column %	2.3	32.6	54.1	0.6	
NE					NE					
Row %	4.2	37.9	17.4	40.0	Row %	0.7	17.6	24.4	57.4	
Column %	5.4	20.4	31.8	59.1	Column %	0.7	11.4	28.0	87.6	

Actual Aged 30-39		Labor supply (t)			Predicted Aged 30-39		Labor supply (t)			
Ü	-	SE	PE	PE	NE	O	SE	PE	PE	NE
Labor supply (t-1)			Full-time	Part-time		Labor supply (t-1)		Full-time	Part-time	
SE						SE				
	Row %	79.4	4.7	2.2	5.8	Row %	83.8	9.7	0.1	6.4
	Column %	91.3	2.8	4.4	7.0	Column %	82.2	3.9	0.4	32.3
PE, Full-time						PE, Full-time				
	Row %	0.6	88.9	6.7	2.5	Row %	5.6	92.3	1.1	1.0
	Column %	0.6	52.2	13.4	3.1	Column %	5.5	36.7	4.2	4.9
PE, Part-ti	me					PE, Part-time				
	Row %	1.6	53.4	29.3	14.9	Row %	6.4	75.6	16.6	1.5
	Column %	1.8	31.4	58.3	18.3	Column %	6.3	75.6	61.4	7.5
NE						NE				
	Row %	5.4	23.4	12.0	58.5	Row %	6.2	73.8	9.2	10.9
	Column %	6.3	13.7	23.9	71.6	Column %	6.0	29.4	34.0	55.3

Table 8: Age Profiles of Mean Incomes by Labor Supply Decisions

	Self-			Paid-					
	employed			employed					
				Full-time			Part-time		_
Age		(std.dev.)	(no.obs.)		(std.dev.)	(no.obs.)		(std.dev.)	(no.obs.)
20	25479.4	3346.0	38	22086.9	336.1	694	9302.1	354.7	171
21	35048.4	5636.7	55	22819.5	316.8	863	10891.8	417.9	183
22	32257.9	3008.8	78	24716.4	325.3	1044	10601.5	366.4	200
23	40238.2	3843.4	105	26791.4	582.8	1164	13016.0	1313.4	215
24	37131.3	2607.6	129	27602.3	355.0	1363	11992.7	1043.6	176
25	40122.7	2776.5	153	29703.4	624.2	1415	12313.6	683.4	158
26	51498.5	7828.1	155	30816.8	683.0	1435	14001.5	875.2	142
27	46444.7	3553.9	140	31865.1	779.3	1433	13582.5	964.9	151
28	49377.0	4034.2	163	32530.4	578.2	1344	12751.8	465.4	182
29	52852.2	4196.9	166	34036.2	1015.2	1230	16071.5	704.7	266
30	54313.3	8016.5	142	33911.9	780.0	1206	16020.7	591.6	265
31	59283.8	6854.9	141	34311.0	584.3	1160	16416.3	795.8	275
32	52942.5	6308.6	134	35868.1	671.1	1183	15775.6	622.7	234
33	64065.8	6837.5	100	36102.0	584.0	1180	15953.5	846.3	202
34	69952.1	7038.6	113	37554.4	716.2	1161	17069.6	903.0	202
35	68146.2	11395.2	71	38395.4	694.1	1143	18845.6	879.1	165
36	63237.1	7187.5	69	39146.6	714.6	1060	16963.7	1038.1	119
37	74635.8	11327.1	52	40691.1	864.4	917	15458.6	2032.3	51
38	51499.3	5752.5	38	41868.1	987.1	730	12833.2	1144.4	38
39	64036.2	7761.4	37	42990.4	1315.7	570	-	-	-

Note 1: Numbers are in year 2000 dollars.

Note 2: Mean part-time income for age 39 is not shown because the number of observations is small (22).

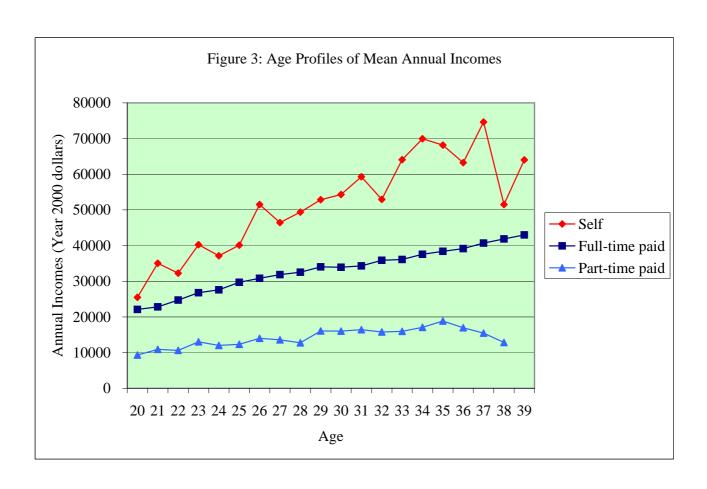


Table 9: Age Profile of Net Worth

Age							Percent
(No.Obs.)	Mean	Median	25%	75%	Min	Max	Negative
20	8829.1	2080	160	6840	-8480	184160	20.3
(138)							
21	14437.0	3611	628	11200	-21038	576000	19.9
(311)							
22	13556.3	4560	785	13860	-48165	769302	19.6
(588)	13330.3	4300	703	13000	-40103	707302	17.0
(0.00)							
23	15453.4	5768	970	18240	-52560	364802	19.2
(834)							
2.4	21721.0	7200	1074	22220	5,000,0	01.4722	17.0
(1078)	21731.9	7300	1274	22338	-56836	814722	17.9
(1078)							
25	26170.6	10640	2376	28576	-72336	679442	14.8
(1259)						****	
, ,							
26	35819.5	15985	3562	39672	-52820	742922	13.5
(1255)							
27	20412.2	1,000	2200	42016	71.420	012015	14.4
27 (1360)	38413.3	16800	3208	43916	-71438	912915	14.4
(1300)							
28	43644.7	19382	4049	51778	-63510	1128144	13.0
(1312)							
29	54481.7	25258	4620	61612	-60800	1905040	11.7
(1327)							
30	50657.0	26101	EE07	70702	50706	1126710	10.1
(1126)	59657.9	26101	5587	70702	-59796	1136710	12.1
(1120)							
31	71103.3	29304	6838	73780	-59860	2594100	10.4
(1123)							
32	79519.8	38080	6991	87115	-56100	2231799	10.5
(953)							
33	79702.4	37120	6100	93432	-59003	2579427	12.1
(925)	77702.4	37120	0100	73432	-37003	2317421	12.1
(>20)							
34	90289.1	48452	10681	111863	-69020	1217687	9.0
(836)							
25	100.622.2	50010	12005	110007	60000	2022712	10.2
35	100622.3	52910	13807	118985	-63800	2023543	10.2
(842)							
36	108198.7	60900	14160	141541	-49000	2673988	8.1
(651)							
37	105425.2	62948	14329	143285	-56500	1421460	11.4
(516)							
38	121247 6	71525	22722	160400	55120	706000	67
(436)	121347.6	71525	23723	160490	-55120	796098	6.7
(+30)							
39	134295.6	81000	20465	188400	-48760	816200	9.8
(297)							

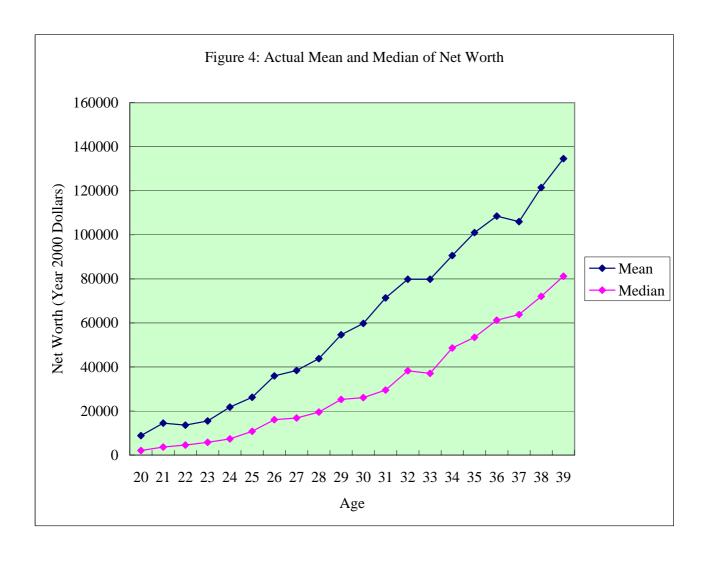
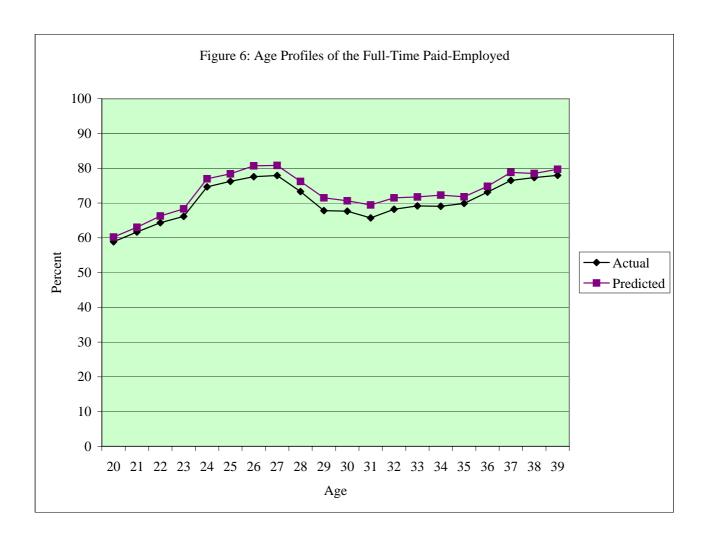
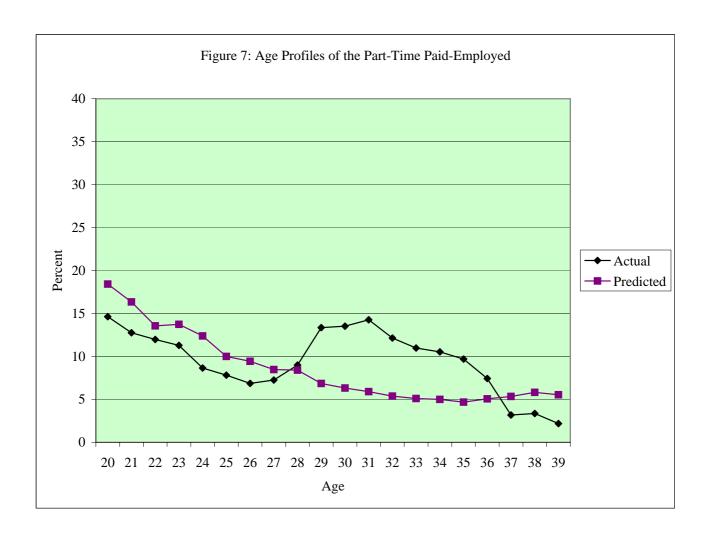


Table 10: Three Characteristics on Entry into and Exit from Self-Employment: Actual and Predicted

	Actual		Predicted	
	Non-college	College	Non-college	College
	educated	educated	educated	educated
Ever experience of self-employment (%)	31.78	27.48	26.76	24.43
First entry into self-employment occurs in less than or equal to first eight decision years (%)	62.72	74.62	59.34	69.20
Exit from self-employment in a year (%)	32.28	28.57	28.09	23.61

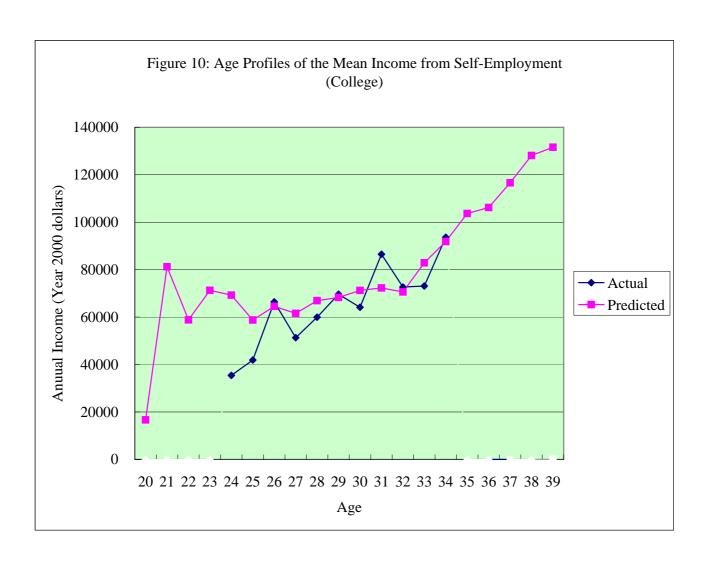


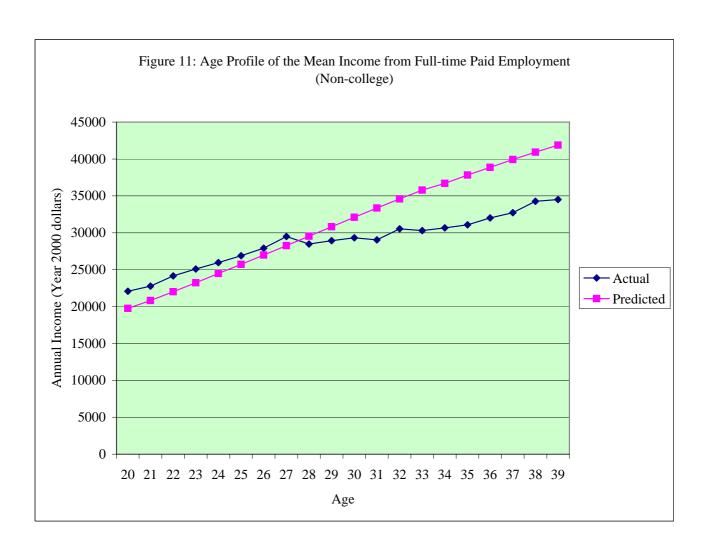


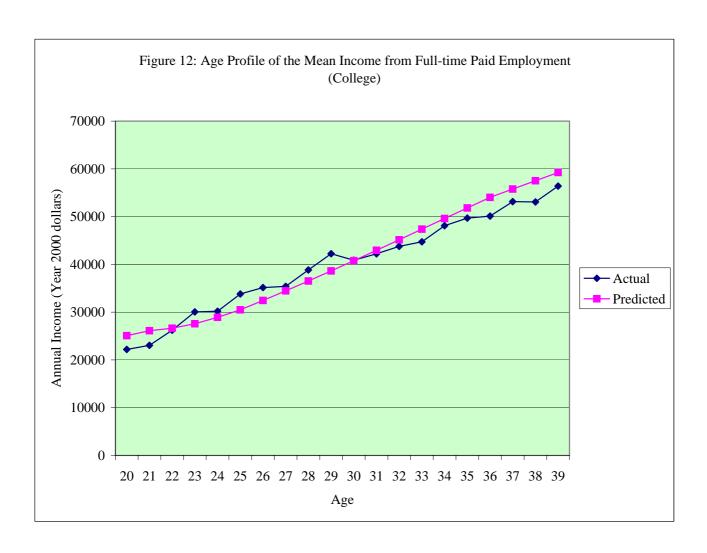




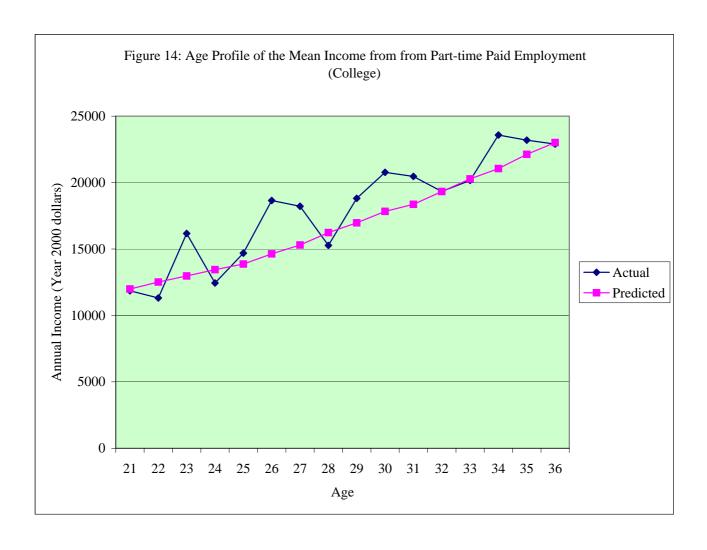












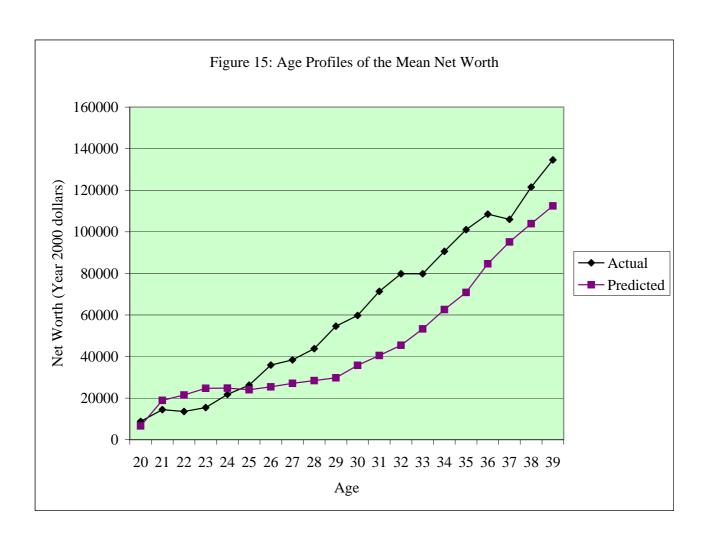


Table 11: Transition Matrices for Labor Supply Decisions by Type

Predicte	ed	·	·	·	·	
Overall		Labor supply (t)				
	' <u>-</u>	SE	PE	PE	NE	
Labor supply (t-1)			Full-time	Part-time		
SE						
	Row %	84.6	9.6	0.6	5.2	
	Column %	91.7	5.7	0.8	8.1	
PE, Full-tii	me					
	Row %	4.2	85.6	6.6	3.5	
	Column %	4.6	50.8	8.8	5.5	
PE, Part-tii	me					
	Row %	2.4	52.2	44.9	0.5	
	Column %	2.6	31.0	59.4	0.7	
NE						
	Row %	1.0	21.0	23.4	54.5	
	Column %	1.1	12.5	31.0	85.6	

Type 1		Labor supply (t)				Type 2		Labor supply (t)			
	·	SE	PE	PE	NE	_	SE	PE	PE	NE	
Labor supp	oly (t-1)		Full-time	Part-time		Labor supply (t-1)		Full-time	Part-time		
SE						SE					
	Row %	78.2	12.3	1.8	7.8	Row %	86.7	8.8	0.2	4.3	
	Column %	90.7	8.6	1.8	10.7	Column %	92.4	4.7	0.3	7.1	
PE, Full-time						PE, Full-time					
	Row %	4.3	72.7	11.4	11.7	Row %	4.2	90.2	5.0	0.7	
	Column %	5.0	51.2	11.5	16.0	Column %	4.4	48.8	8.2	1.1	
PE, Part-ti	PE, Part-time					PE, Part-time					
	Row %	2.8	42.6	54.1	0.5	Row %	2.0	62.0	35.5	0.5	
	Column %	3.3	30.0	54.6	0.6	Column %	2.1	33.6	58.5	0.8	
NE						NE					
	Row %	0.9	14.5	31.9	52.7	Row %	1.0	23.7	20.0	55.3	
	Column %	1.0	10.2	32.2	72.6	Column %	1.1	12.8	33.0	91.0	

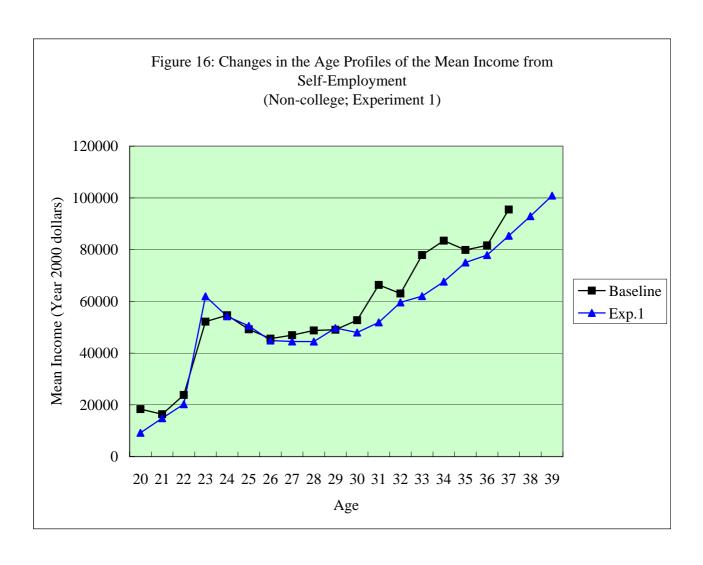
Table 12: Changes in the Characteristics on Entry into and Exit from Self-Employment (Experiments 1-3)

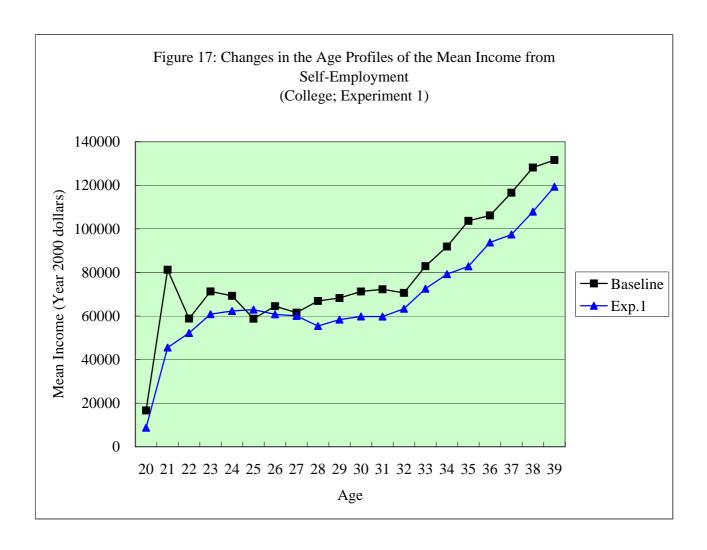
	Baseline		Exp. 1		Exp. 2		Exp. 3	
	NC	С	NC	С	NC	C	NC	С
Ever experience of self-employment (%)	26.76	24.43	23.77	21.76	34.40	31.54	51.51	47.82
First entry into self-employment occurs in less than or equal to first eight decision years (%)	59.34	69.20	65.97	64.55	69.31	67.29	84.49	87.86
Exit from self-employment in a year (%)	28.09	23.61	19.60	21.51	45.98	38.81	42.22	32.25

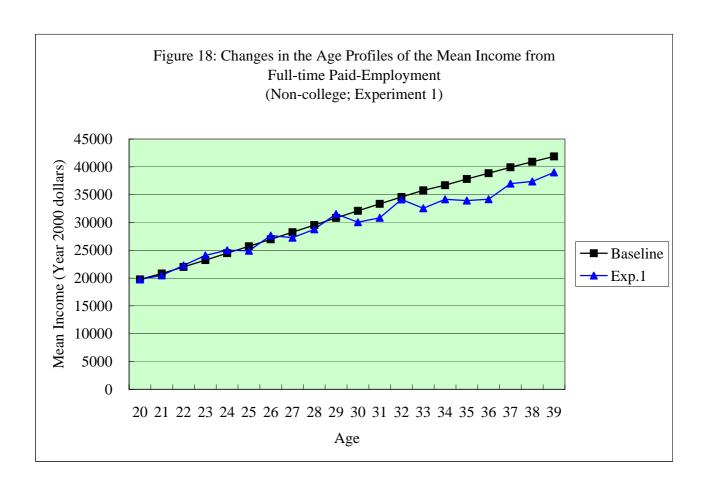
Note: "NC" ("C") denotes "non-college educated" ("college educated").

Table 13: Changes in the Age Profiles of Labor Supply (Experiment 1)

	Self-Employ	ment	Paid Employ	ment	Non-Employment		
Age		Exp. 1	Baseline	Exp. 1	Baseline	Exp. 1	
20	0.9	1.1	78.6	78.9	20.7	20.0	
21	3.5	2.2	79.4	78.4	16.6	19.4	
22	5.7	5.8	79.8	72.4	11.1	21.8	
23	7.4	6.2	82.1	76.6	9.4	17.2	
24	7.8	7.3	89.3	81.4	9.1	11.4	
25	7.2	6.9	88.4	83.6	7.2	9.5	
26	6.5	6.4	90.1	84.8	7.7	8.7	
27	6.7	6.5	89.3	84.2	8.3	9.3	
28	8.0	8.2	84.6	81.3	9.9	10.5	
29	7.7	8.0	78.4	81.6	9.8	10.4	
30	7.3	7.8	77.0	81.8	9.9	10.4	
31	7.1	7.8	75.4	81.5	10.7	10.7	
32	7.2	7.9	76.9	83.7	10.5	8.4	
33	7.5	8.2	76.9	84.5	10.8	7.4	
34	7.8	8.8	77.3	83.9	11.7	7.4	
35	7.2	9.5	76.5	84.3	12.9	6.2	
36	7.3	10.6	79.9	83.6	12.4	5.8	
37	7.3	11.5	84.2	83.4	13.3	5.1	
38	8.0	11.9	84.3	83.0	14.6	5.1	
39	8.4	12.6	85.3	82.2	15.3	5.2	







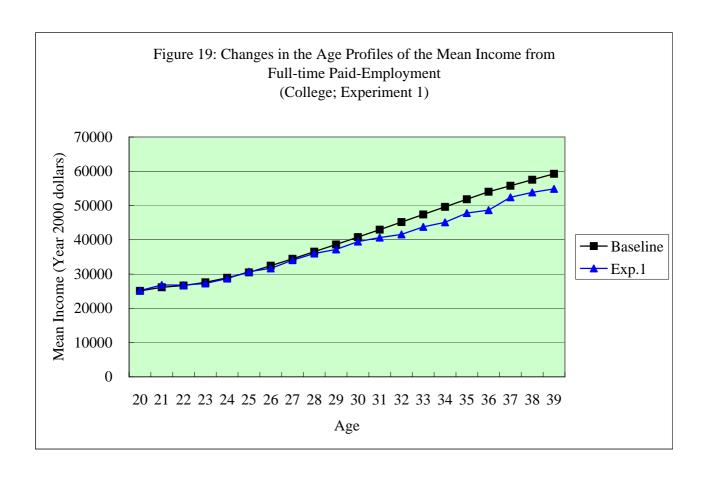


Table 14: Changes in the Age Profiles of Labor Supply (Experiment 2)

	Self-Employ	ment	Paid Employ	ment	Non-Employment		
Age	Baseline	Exp. 2	Baseline	Exp. 2	Baseline	Exp. 2	
20	0.9	1.3	78.6	78.8	20.7	19.9	
21	3.5	4.4	79.4	72.9	16.6	22.7	
22	5.7	6.4	79.8	79.5	11.1	14.1	
23	7.4	8.3	82.1	77.3	9.4	14.4	
24	7.8	9.0	89.3	77.7	9.1	13.3	
25	7.2	9.9	88.4	76.0	7.2	14.1	
26	6.5	8.9	90.1	80.6	7.7	10.5	
27	6.7	8.2	89.3	80.6	8.3	11.2	
28	8.0	8.0	84.6	78.7	9.9	13.3	
29	7.7	7.6	78.4	77.8	9.8	14.6	
30	7.3	6.7	77.0	78.5	9.9	14.8	
31	7.1	6.9	75.4	80.7	10.7	12.5	
32	7.2	6.4	76.9	80.3	10.5	13.3	
33	7.5	6.2	76.9	78.2	10.8	15.6	
34	7.8	6.7	77.3	75.3	11.7	18.0	
35	7.2	7.0	76.5	71.0	12.9	22.0	
36	7.3	7.6	79.9	71.1	12.4	21.3	
37	7.3	8.1	84.2	70.0	13.3	21.9	
38	8.0	8.7	84.3	70.6	14.6	20.8	
39	8.4	9.5	85.3	62.4	15.3	28.1	

